

# Improved rotation-activity-age relations in Sun-like stars

Jorge Meléndez, Leonardo A. dos Santos and Fabrício C. Freitas

Universidade de São Paulo, IAG, Departamento de Astronomia  
Rua do Matão 1226, 05508-090 São Paulo, SP, Brazil  
email: [jorge.melendez@iag.usp.br](mailto:jorge.melendez@iag.usp.br)

**Abstract.** The evolution of rotational velocity and magnetic activity with age follows approximately a  $t^{-1/2}$  relation, the famous Skumanich law. Using a large sample of about 80 solar twins with precise ages, we show departures from this law. We found a steep drop in rotational velocity and activity in the first 2-3 Gyr and afterwards there seems to be a shallow decrease. Our inferred rotational periods suggest that the Sun will continue to slow down, validating thus the use of gyrochronology beyond solar age. The Sun displays normal rotational velocity and activity when compared to solar twins of solar age. We also show that stars with exceedingly high stellar activity for their age are spectroscopic binaries that also exhibit enhanced rotational velocities and chemical signatures of mass transfer.

**Keywords.** Sun: activity, Sun: rotation, stars: activity, stars: rotation, techniques: spectroscopic

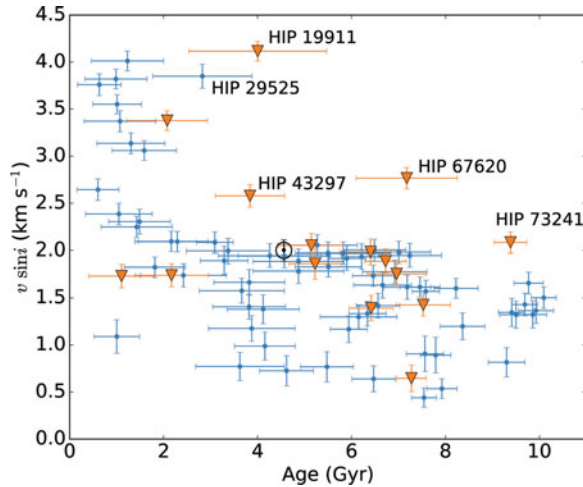
---

## 1. Introduction

Solar twins are defined as stars with effective temperatures within 100 K, and  $\log g$  and  $[\text{Fe}/\text{H}]$  within 0.1 dex around the Sun's values (Ramírez *et al.* 2014). The first solar twin, 18 Sco, was discovered in 1997 by Porto de Mello & da Silva (1997, see also Soubiran & Triaud 2004). Only in the mid-2000s new solar twins were identified and in the last decade their number has grown to about a hundred (Mahdi *et al.* 2016; Yana Galarza *et al.* 2016b; Porto de Mello *et al.* 2014; Datson *et al.* 2014, 2012; Ramírez *et al.* 2014; Meléndez *et al.* 2014b, 2009, 2006; do Nascimento *et al.* 2013; Takeda & Tajitsu 2009; Pasquini *et al.* 2008; Takeda *et al.* 2007; Meléndez & Ramírez 2007; King *et al.* 2005).

An important application of solar twins is to set the zero-point of fundamental calibrations in astrophysics (Datson *et al.* 2015, 2012; Casagrande *et al.* 2014, 2010; Ramírez *et al.* 2012; Meléndez *et al.* 2010), but many other studies have been possible thanks to the precise stellar parameters ( $\sigma(T_{\text{eff}}) \leq 10$  K,  $\sigma(\log g) \leq 0.02$  dex) and chemical abundances ( $\sigma \sim 0.01$  dex) that can be achieved in these stars (e.g., Nissen 2015; Bedell *et al.* 2014; Monroe *et al.* 2013; Kiselman *et al.* 2011). One landmark result of the first high precision studies showed that the Sun has a distinct abundance pattern (Meléndez *et al.* 2009; Ramírez *et al.* 2009, 2010). Strikingly, this peculiar pattern may be related to the formation of rocky planets in our solar system (Chambers 2010). In a related investigation, Tucci Maia *et al.* (2014) showed that the binary system of solar twins 16 Cyg displays chemical abundance differences likely due to planets, and other planet-hosting wide binary systems composed of solar-type stars also show distinct abundances probably due to planets (Teske *et al.* 2016a,b; Adibekyan *et al.* 2016; Saffe *et al.* 2016; Ramírez *et al.* 2015; Biazzo *et al.* 2015).

Solar twins have also been crucial to obtain reliable isochrone ages (Tucci Maia *et al.* 2016; Nissen 2015), determine improved mass and radius of benchmark planets (Bedell *et al.* 2016), study the possible effects of radioactive elements on rocky planet interior



**Figure 1.** Projected rotational velocities in solar twins vs. age. The Sun is shown with its usual symbol and the solar twins by blue points, except the spectroscopic binaries that are shown by inverted orange triangles (outliers are labeled). Figure from dos Santos *et al.* (2016).

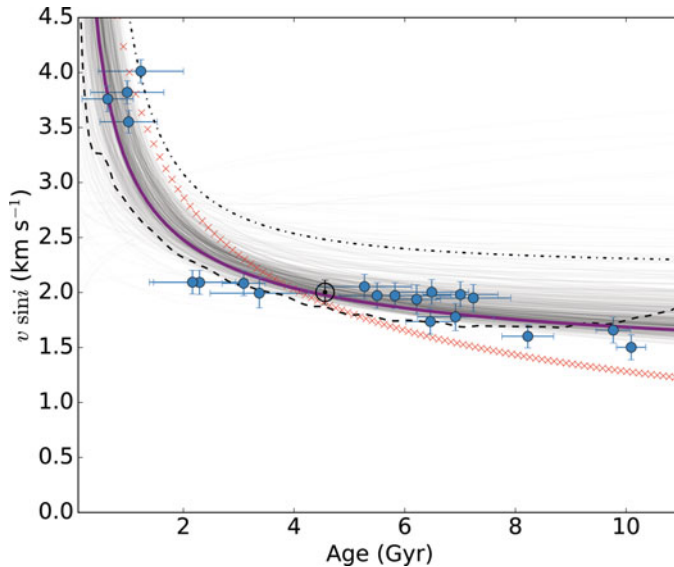
dynamics and habitability (Unterborn *et al.* 2015), infer the effects of mass transfer by the progenitors of white dwarfs (Desidera *et al.* 2016; Schirbel *et al.* 2015), observe stellar oscillations to constrain their masses and ages (Metcalf *et al.* 2012; Li *et al.* 2012; Bazot *et al.* 2011), inspire new stellar models including episodic accretion (Baraffe & Chabrier 2010), observe depletion of the light elements Li (Carlos *et al.* 2016; Monroe *et al.* 2013; Baumann *et al.* 2010) and Be (Tucci Maia *et al.* 2015) and model their decrease through non-standard stellar models (Andrássy & Spruit 2015; Castro *et al.* 2011; Denissenkov 2010; do Nascimento *et al.* 2009), develop chemical clocks through the [Y/Mg] and [Y/Al] ratios (Tucci Maia *et al.* 2016; Spina *et al.* 2016; Nissen 2016, 2015), and to uncover the nucleosynthetic history of our Milky Way empirically through cosmic phylogeny (Jofré *et al.* 2017) or through the detailed study of abundance ratios (e.g., Nissen 2016, 2015; Spina *et al.* 2016; Yana Galarza *et al.* 2016a; Meléndez *et al.* 2014a).

Since 2011 we have been monitoring about 70 solar twins for planets at the ESO La Silla Observatory (Meléndez *et al.* 2015; Ramírez *et al.* 2014), and have found a Jupiter-twin (Bedell *et al.* 2015) and a super-Neptune and super-Earth (Meléndez *et al.* 2017). Using the individual and combined HARPS spectra obtained for our sample, and additional spectra of 9 solar twins gathered by other ESO programs, we studied the evolution of rotational velocity and magnetic activity using about 80 solar twins with precise stellar ages measured by a differential comparison of our precise stellar parameters with isochrones (Tucci Maia *et al.* 2016). We also assess how common is the Sun by a comparison with solar twins.

## 2. The Skumanich law and the Sun among stars

More than four decades ago, Skumanich (1972) showed that there is a decline of rotational velocity ( $v$ ) and activity with age ( $t$ ), following approximately a  $t^{-1/2}$  relation, the famous “Skumanich law”. Impressively, this widely used relation was obtained using only a few data points.

Under some assumptions, the  $v \propto t^{-1/2}$  relation can be derived from the angular momentum loss due to stellar winds (e.g., Soderblom 1983; Kawaler 1988). However, there are evidences for departures from the Skumanich law. The work by Pace & Pasquini



**Figure 2.** Projected rotational velocities in solar twins of the selected sample vs. age. The Sun is shown with its usual symbol. Our best fit (solid line) and the Skumanich law (red symbols) are shown. Figure from dos Santos *et al.* (2016).

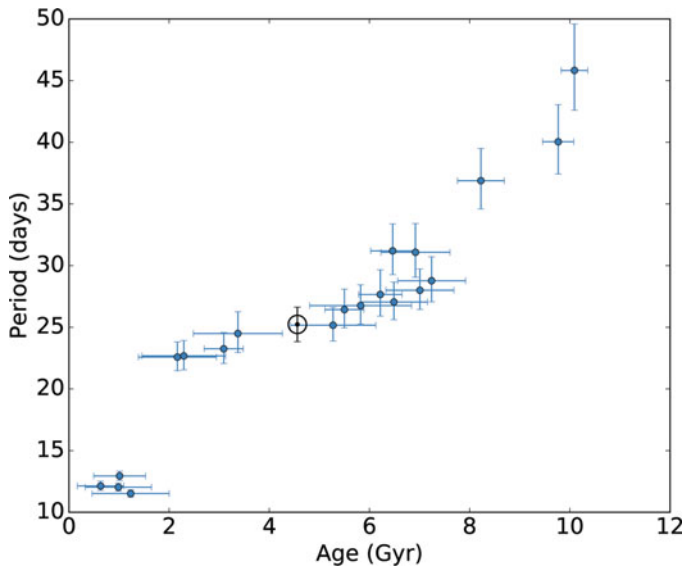
(2004) suggests a steep decline of rotational velocities and stellar activity in the first 1-2 Gyr and then a flat trend with age. Our large sample of solar twins is ideal to verify whether the decay of rotational velocity and activity is smooth, or if they behave as suggested by Pace & Pasquini (2004).

Many previous works sought to evaluate the place of the Sun among other stars (e.g., Gustafsson 2008, 1998; Shapiro *et al.* 2013). This is of fundamental importance because the Sun is used to validate stellar models, so we must know whether the Sun is a regular star or an oddball. Unfortunately, conclusions by previous studies could be hampered by biased samples, and the Sun has not been compared to strictly Sun-like stars (e.g., Robles *et al.* 2008). And, even when the Sun is compared to similar stars, there is the issue of systematics due to the observations of the Sun and the stars being carried out with different instruments. This is clearly shown in a recent study by Egeland *et al.* (2016), where the Sun's magnetic activity  $S$ -index is shown to be lower than previously estimated.

In our work the Sun and the comparison stellar sample are analysed using spectra obtained by the HARPS spectrograph at the ESO La Silla Observatory, all gathered with the same high resolution ( $R = 115000$ ) and at high signal-to-noise ratio ( $S/N$ ) for our planet search around solar twins (Meléndez *et al.* 2015). Furthermore, our reference sample of solar twins have approximately solar mass and metallicity, therefore they follow evolutionary paths similar to the Sun. Thus, our sample is ideal to verify if the Sun is normal in its activity level and rotational velocity.

### 3. Rotational velocities

In order to determine the projected rotational velocities in our sample, we fit the line profiles considering instrumental, rotational and macroturbulent broadening, as described in dos Santos *et al.* (2016).



**Figure 3.** Evolution of inferred rotational period vs. stellar ages in solar twins, using the rotational velocities from dos Santos *et al.* (2016) and taking into account the variation of stellar radius with age predicted by the solar model of do Nascimento *et al.* (2009).

We removed all spectroscopic binaries (Fig. 1), as some of them have anomalously high  $v \sin i$  for their age, likely due to interactions with their companions.

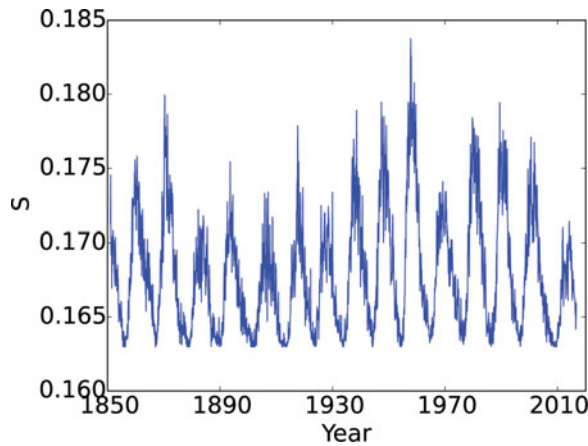
We divided the sample in bins of 2 Gyr and in each bin we only kept stars with  $v \sin i$  in the upper 30 %, because these stars have the highest chance of having  $\sin i$  above 0.9 (dos Santos *et al.* 2016). The selected sample is shown in Fig. 2. It is clear that the decay in rotational velocity in the first 2-3 Gyr is steeper than the Skumanich law, and that the further decline of rotational velocity with age is flatter than the Skumanich relation.

Using rotational periods from solar-type stars obtained from *Kepler* observations, it has been suggested that there is a weakened magnetic braking after the Sun's age (van Saders *et al.* 2016). We use our selected sample of solar twins with  $\sin i \sim 1$ , to evaluate the variation of rotational period ( $P$ ) with age.  $P$  is obtained from our rotational velocities and the predicted variation of the solar radius with age using the model by do Nascimento *et al.* (2009). Our results (Fig. 3) indicate that the Sun will keep slowing down, unlike the suggestion by van Saders *et al.* (2016) of weakened braking for old ages. If we obtain the stellar radius using the observed  $\log g$  and inferred mass, we obtain similar results but with a larger scatter. Thus, our analysis suggests that gyrochronology can be used to determine stellar ages based on observed rotational periods even for stars older than the Sun.

#### 4. Magnetic activity

We study the variation of magnetic activity with age using the Ca II H and K lines. We measured activity indexes using triangular filters in the core of the lines and flat filters in the continuum, as in Wright *et al.* (2004). Our indexes were calibrated to the  $S$ -index of the Mount Wilson system (e.g., Baliunas *et al.* 1995).

We used archival data of asteroid observations from other HARPS programs to obtain the reflected solar spectra covering different epochs of the solar cycle. This guarantees that the Sun and the stars are in the same system, eliminating thus potential systematic



**Figure 4.** Evolution of the  $S$ -index since 1850, inferred through a calibration of the  $S$ -index and International Sunspot Number. Figure from Freitas *et al.* (2017).

problems. In order to increase the time baseline of the solar data, we calibrated the  $S$ -index to the International Sunspot Number, estimating the  $S$ -index since 1850 (Fig. 4). This allowed us to infer an accurate average solar  $S$ -index, considering cycles of different amplitudes.

The  $S$ -index is converted to the  $\log R'_{\text{HK}}$  activity index following standard procedures (e.g., Wright *et al.* 2004). The average of this index as a function of stellar age is shown in Fig. 5. Our data departs from the Skumanich law, suggesting a steep decrease in activity in the first 3 Gyr and then a moderate decrease of stellar activity for increasing ages.

Some spectroscopic binaries present high stellar activity for their age (Fig. 5). These stars also show high rotational velocity (Fig. 1) and chemical signatures of mass transfer, as revealed by their high yttrium abundances (Tucci Maia *et al.* 2016).

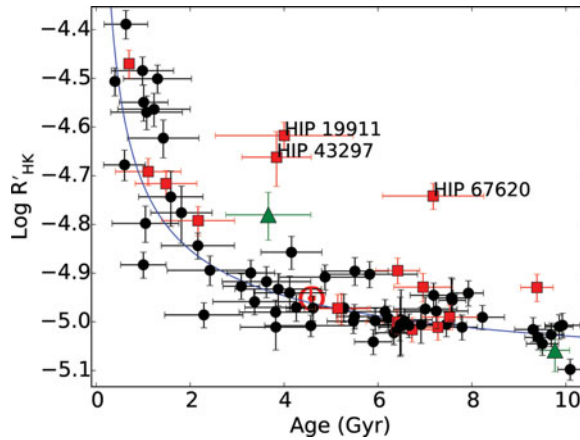
We obtained improved  $\log R'_{\text{HK}}$  values by using new calibrations based on  $T_{\text{eff}}$  rather than (B-V), as described in detail in Freitas *et al.* (2017). These improved values are plotted in Fig. 6. Qualitatively we obtain similar results for the decay of activity with age, but the activity-age correlation is somewhat improved, with a steep decline of activity in the first 3 Gyrs, and a shallower decrease for increasing ages. For comparison we show the relations by Donahue (1993) and Mamajek & Hillenbrand (2008), which do not reproduce well the pattern observed in solar twins.

## 5. Conclusions

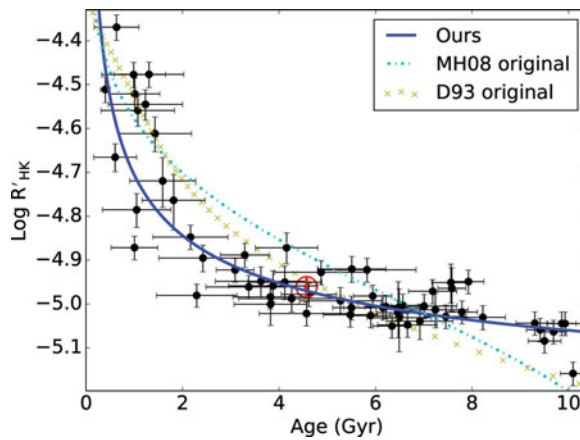
Our consistent analysis of solar twins and the Sun suggests that the evolution of rotational velocity and magnetic activity in the Sun depart from the widely used Skumanich law. The decay is steeper in the first 3 Gyr, with a slight decrease for older ages.

Our inferred longer rotation periods for increasing ages suggest that gyrochronology (e.g. Barnes 2007) is valid even beyond solar age. This result obtained with solar twins is in contrast to recent results based on solar-type stars from *Kepler* observations (van Saders *et al.* 2016). This shows the importance of having a proper comparison sample of solar twins, rather than solar-type stars that do not necessarily have the same properties as the Sun.

Furthermore, we show that the Sun is normal in rotational velocity and magnetic activity when compared to solar twins of the same age, validating thus the use of the Sun as a cornerstone calibrator in Astrophysics.



**Figure 5.**  $\text{Log } R'_{\text{HK}}$  activity index vs. age in solar twins (black circles). Spectroscopic binaries are shown by red squares (outliers are labeled). The Sun is shown with its usual symbol. Our best fit is shown. Figure from Freitas *et al.* (2017).



**Figure 6.**  $\text{Log } R'_{\text{HK}}$  activity index vs. age in solar twins (black circles) using our improved calibrations based on  $T_{\text{eff}}$  (see Freitas *et al.* 2017). Spectroscopic binaries are excluded. Our fit is shown by the solid blue line. The other lines correspond to the relations by Mamajek & Hillenbrand (2008) and Donahue (1993). Figure adapted from Freitas *et al.* (2017).

## References

- Adibekyan, V., Delgado-Mena, E., Figueira, P., *et al.* 2016, *A&A*, 591, A34  
 Andr assy, R. & Spruit, H. C. 2015, *A&A*, 579, A122  
 Baliunas, S. L., *et al.* 1995, *ApJ*, 438, 269  
 Baraffe, I. & Chabrier, G. 2010, *A&A*, 521, A44  
 Barnes, S. A. 2007, *ApJ*, 669, 1167  
 Baumann, P., Ram rez, I., Mel ndez, J., Asplund, M., & Lind, K. 2010, *A&A*, 519, A87  
 Bazot, M., *et al.* 2011, *A&A*, 526, L4  
 Bedell, M., Mel ndez, J., Bean, J. L., *et al.* 2014, *ApJ*, 795, 23  
 Bedell, M., Mel ndez, J., Bean, J. L., *et al.* 2015, *A&A*, 581, A34  
 Bedell, M., Bean, J. L., Melendez, J., *et al.* 2016, arXiv:1611.06239  
 Biazzo, K., Gratton, R., Desidera, S., *et al.* 2015, *A&A*, 583, A135  
 Carlos, M., Nissen, P. E., & Mel ndez, J. 2016, *A&A*, 587, A100  
 Casagrande, L., Ram rez, I., Mel ndez, J., Bessell, M., & Asplund, M. 2010, *A&A*, 512, A54  
 Casagrande, L., Portinari, L., Glass, I. S., *et al.* 2014, *MNRAS*, 439, 2060

- Castro, M., Do Nascimento, J. D., Jr., Biazzo, K., Meléndez, J., & de Medeiros, J. R. 2011, *A&A*, 526, A17
- Chambers, J. E. 2010, *ApJ*, 724, 92
- Datson, J., Flynn, C., & Portinari, L. 2012, *MNRAS*, 426, 484
- Datson, J., Flynn, C., & Portinari, L. 2014, *MNRAS*, 439, 1028
- Datson, J., Flynn, C., & Portinari, L. 2015, *A&A*, 574, A124
- Denissenkov, P. A. 2010, *ApJ*, 719, 28
- Desidera, S., D’Orazi, V., & Lugaro, M. 2016, *A&A*, 587, A46
- Donahue, R. A. 1993, Ph.D. Thesis,
- Do Nascimento, J. D., Jr., Castro, M., Meléndez, J., Bazot, M., Théado, S., Porto de Mello, G. F., & de Medeiros, J. R. 2009, *A&A*, 501, 687
- do Nascimento, J.-D., Jr., Takeda, Y., Meléndez, J., *et al.* 2013, *ApJ*, 771, L31
- dos Santos, L. A., Meléndez, J., do Nascimento, J.-D., Jr., *et al.* 2016, *A&A*, 592, A156
- Egeland, R., Soon, W., Baliunas, S., *et al.* 2017, *ApJ*, 835, 25
- Freitas, F. C., Meléndez, J., Bedell, M., *et al.* 2017, submitted
- Gustafsson, B. 1998, *Space Sci. Rev.*, 85, 419
- Gustafsson, B. 2008, *Physica Scripta*, Volume T 130, pp. 014036
- Jofré, P., Das, P., Bertranpetit, J., & Foley, R. 2017, *MNRAS*, 467, 1140
- Kawaler, S. D. 1988, *ApJ*, 333, 236
- King, J. R., Boesgaard, A. M., & Schuler, S. C. 2005, *AJ*, 130, 2318
- Kiselman, D., Pereira, T. M. D., Gustafsson, B., *et al.* 2011, *A&A*, 535, A14
- Li, T. D., Bi, S. L., Liu, K., Tian, Z. J., & Shuai, G. Z. 2012, *A&A*, 546, A83
- Mahdi, D., Soubiran, C., Blanco-Cuaresma, S., & Chemin, L. 2016, *A&A*, 587, A131
- Mamajek, E. E. & Hillenbrand, L. A. 2008, *ApJ*, 687, 1264
- Meléndez, J., Dodds-Eden, K., & Robles, J. A. 2006, *ApJ*, 641, L133
- Meléndez, J. & Ramírez, I. 2007, *ApJ*, 669, L89
- Meléndez, J., Asplund, M., Gustafsson, B., & Yong, D. 2009, *ApJ*, 704, L66
- Meléndez, J., Schuster, W. J., Silva, J. S., Ramírez, I., Casagrande, L., & Coelho, P. 2010, *A&A*, 522, A98
- Meléndez, J., Ramírez, I., Karakas, A. I., *et al.* 2014a, *ApJ*, 791, 14
- Meléndez, J., Schirbel, L., Monroe, T. R., *et al.* 2014b, *A&A*, 567, L3
- Meléndez, J., Bean, J. L., Bedell, M., *et al.* 2015, *The Messenger*, 161, 28
- Meléndez, J., Bedell, M., Bean, J. L., *et al.* 2017, *A&A*, 597, A34
- Metcalfe, T. S., Chaplin, W. J., Appourchaux, T., *et al.* 2012, *ApJ*, 748, L10
- Monroe, T. R., Meléndez, J., Ramírez, I., *et al.* 2013, *ApJ*, 774, L32
- Nissen, P. E. 2015, *A&A*, 579, A52
- Nissen, P. E. 2016, *A&A*, 593, A65
- Pace, G. & Pasquini, L. 2004, *A&A*, 426, 1021
- Pasquini, L., Biazzo, K., Bonifacio, P., Randich, S., & Bedin, L. R. 2008, *A&A*, 489, 677
- Porto de Mello, G. F. & da Silva, L. 1997, *ApJ*, 482, L89
- Porto de Mello, G. F., da Silva, R., da Silva, L., & de Nader, R. V. 2014, *A&A*, 563, A52
- Ramírez, I., Meléndez, J., & Asplund, M. 2009, *A&A*, 508, L17
- Ramírez, I., Asplund, M., Baumann, P., Meléndez, J., & Bensby, T. 2010, *A&A*, 521, A33
- Ramírez, I., Michel, R., Sefako, R., *et al.* 2012, *ApJ*, 752, 5
- Ramírez, I., Meléndez, J., Bean, J., *et al.* 2014, *A&A*, 572, A48
- Ramírez, I., Khanal, S., Aleo, P., *et al.* 2015, *ApJ*, 808, 13
- Robles, J. A., Lineweaver, C. H., Grether, D., *et al.* 2008, *ApJ*, 684, 691-706
- Saffe, C., Flores, M., Jaque Arancibia, M., Buccino, A., & Jofré, E. 2016, *A&A*, 588, A81
- Schirbel, L., Meléndez, J., Karakas, A. I., *et al.* 2015, *A&A*, 584, A116
- Shapiro, A. I., Schmutz, W., Cessateur, G., & Rozanov, E. 2013, *A&A*, 552, A114
- Skumanich, A. 1972, *ApJ*, 171, 565
- Soderblom, D. R. 1983, *ApJS*, 53, 1
- Soubiran, C. & Triaud, A. 2004, *A&A*, 418, 1089
- Spina, L., Meléndez, J., Karakas, A. I., *et al.* 2016, *A&A*, 593, A125



- Takeda, Y. & Tajitsu, A. 2009, *PASJ*, 61, 471
- Takeda, Y., Kawanomoto, S., Honda, S., Ando, H., & Sakurai, T. 2007, *A&A*, 468, 663
- Teske, J. K., Khanal, S., & Ramírez, I. 2016a, *ApJ*, 819, 19
- Teske, J. K., Shectman, S. A., Vogt, S. S., *et al.* 2016b, *AJ*, 152, 167
- Tucci Maia, M., Meléndez, J., & Ramírez, I. 2014, *ApJ*, 790, LL25
- Tucci Maia, M., Meléndez, J., Castro, M., *et al.* 2015, *A&A*, 576, L10
- Tucci Maia, M., Ramírez, I., Meléndez, J., *et al.* 2016, *A&A*, 590, A32
- Unterborn, C. T., Johnson, J. A., & Panero, W. R. 2015, *ApJ*, 806, 139
- van Saders, J. L., Ceillier, T., Metcalfe, T. S., *et al.* 2016, *Nature*, 529, 181
- Wright, J. T., Marcy, G. W., Butler, R. P., & Vogt, S. S. 2004, *ApJS*, 152, 261
- Yana Galarza, J., Meléndez, J., Ramírez, I., *et al.* 2016a, *A&A*, 589, A17
- Yana Galarza, J., Meléndez, J., & Cohen, J. G. 2016b, *A&A*, 589, A65