

Finite-sized rigid spheres in turbulent Taylor–Couette flow: effect on the overall drag

Dennis Bakhuis¹, Ruben A. Verschoof¹, Varghese Mathai¹,
Sander G. Huisman¹, Detlef Lohse^{1,2} and Chao Sun^{3,1,†}

¹Physics of Fluids Group, Max Planck UT Center for Complex Fluid Dynamics, MESA+ Institute and J.M. Burgers Centre for Fluid Dynamics, University of Twente, P.O. Box 217, 7500 AE Enschede, The Netherlands

²Max Planck Institute for Dynamics and Self-Organization, 37077 Göttingen, Germany

³Center for Combustion Energy, Key Laboratory for Thermal Science and Power Engineering of Ministry of Education, Department of Energy and Power Engineering, Tsinghua University, Beijing, China

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We report on the modification of drag by neutrally buoyant spherical finite-sized particles in highly turbulent Taylor–Couette (TC) flow. These particles are used to disentangle the effects of size, deformability and volume fraction on the drag, and are contrasted to the drag in bubbly TC flow. From global torque measurements, we find that rigid spheres hardly decrease or increase the torque needed to drive the system. The size of the particles under investigation has a marginal effect on the drag, with smaller diameter particles showing only slightly lower drag. Increase of the particle volume fraction shows a net drag increase. However, this increase is much smaller than can be explained by the increase in apparent viscosity due to the particles. The increase in drag for increasing particle volume fraction is corroborated by performing laser Doppler anemometry, where we find that the turbulent velocity fluctuations also increase with increasing volume fraction. In contrast to rigid spheres, for bubbles, the effective drag reduction also increases with increasing Reynolds number. Bubbles are also much more effective in reducing the overall drag.

Key words: multiphase flow, drag reduction, shear layer turbulence

1. Introduction

Flows in nature and industry are generally turbulent, and often these flows carry bubbles, drops or particles of various shapes, sizes and densities. Examples include sediment-laden rivers, gas–liquid reactors, volcanic eruptions, plankton in the oceans, pollutants in the atmosphere and air bubbles in the ocean mixing layer (Toschi & Bodenschatz 2009). Particle-laden flows may be characterized in terms of the particle density ρ_p , particle diameter d_p , volume fraction α and Reynolds number Re of

† Email address for correspondence: chaosun@tsinghua.edu.cn

the flow. When d_p is small (compared with the dissipative length scale η_K) and α is low ($<10^{-3}$), the system may be modelled using a point particle approximation with two-way coupling (Elghobashi 1994; Mazzitelli, Lohse & Toschi 2003; Mathai *et al.* 2016). With recent advances in computing, fully resolved simulations of particle-laden flows have also become feasible. Uhlmann (2008) conducted one of the first numerical simulations of finite-sized rigid spheres in a vertical particle-laden channel flow. They observed a modification of the mean velocity profile and turbulence modulation due to the presence of particles. A number of studies followed, which employed immersed boundary (Peskin 2002; Cisse, Homann & Bec 2013), Physalis (Naso & Prosperetti 2010; Wang, Sierakowski & Prosperetti 2017) and front-tracking methods (Unverdi & Tryggvason 1992; Roghair *et al.* 2011; Tagawa *et al.* 2013) to treat rigid particles and deformable bubbles respectively in channel and pipe flow geometries (Pan & Banerjee 1996; Lu, Fernández & Tryggvason 2005; Uhlmann 2008; Dabiri, Lu & Tryggvason 2013; Kidanemariam *et al.* 2013; Lashgari *et al.* 2014; Picano, Breugem & Brandt 2015; Costa *et al.* 2016). Flows with dispersed particles, drops and bubbles can, under the right conditions, reduce the skin friction and result in significant energetic (and therefore financial) savings. In industrial settings, this is already achieved using polymeric additives which disrupt the self-sustaining cycle of wall turbulence and dampen the quasi-streamwise vortices (Procaccia, L'vov & Benzi 2008; White & Mungal 2008). Polymeric additives are impractical for maritime applications, and therefore gas bubbles are used, with varying success rates (Ceccio 2010; Murai 2014). Local measurements in bubbly flows are non-trivial, and the key parameters and their optimum values are still unknown. For example, it is impossible to fix the bubble size in experiments and therefore to isolate the effect of bubble size. Various studies have hinted that drag reduction can also be achieved using spherical particles (Zhao, Andersson & Gillissen 2010) and also by using very large particles in a turbulent von Kármán flow (Cisse *et al.* 2015). In the latter study, a tremendous decrease in turbulent kinetic energy (TKE) was observed. A similar, but less intense, decrease in TKE was also seen by Bellani *et al.* (2012) using a very low particle volume fraction. By using solid particles, it is possible to isolate the size effect on drag reduction, and, even though rigid particles are fundamentally different from bubbles, this can give additional insight into the mechanism of bubbly drag reduction. Machicoane & Volk (2016) have already shown that the particle dynamics is highly influenced by the diameter of the particle. This might or might not have a direct influence on the global drag of the system and has never been studied. Whether and when solid particles increase or decrease the drag in a flow is yet not fully understood, and two lines of thought exist. On one side, it is hypothesized that solid particles decrease the overall drag as they damp turbulent fluctuations (Poelma, Westerweel & Ooms 2007; Zhao *et al.* 2010). On the other side, one could expect that solid particles increase the drag as they shed vortices, which must be dissipated. In addition, they also increase the apparent viscosity. A common way to quantify this is the so called ‘Einstein relation’ (Einstein 1906),

$$\nu_\alpha = \nu \left(1 + \frac{5}{2}\alpha \right), \quad (1.1)$$

where ν is the viscosity of the continuous phase. This compensation is valid for the small α values used in this paper (Stickel & Powell 2005). Direct measurements of drag in flows with solid particles are scarce, and the debate on under what conditions they either enhance or decrease the friction has not yet been settled. Particles and bubbles may show collective effects (clustering), and experiments have revealed that

this has a significant influence on the flow properties (Liu & Bankoff 1993; Kulick, Fessler & Eaton 1994; Muste & Patel 1997; So *et al.* 2002; Fujiwara, Minato & Hishida 2004; van den Berg *et al.* 2005, 2007; Calzavarini *et al.* 2008; Shawkat, Ching & Shoukri 2008; Colin, Fabre & Kamp 2012; van Gils *et al.* 2013; Maryami *et al.* 2014; Mathai *et al.* 2015; Alm eras *et al.* 2017; Mathai *et al.* 2018). In general, the Stokes number is used to predict this clustering behaviour, but for neutrally buoyant particles, this is found to be insufficient (Fiabane *et al.* 2012; Bragg, Ireland & Collins 2015). In addition, the position of the particles (or the particle clusters) is likely to have a large influence on the skin friction. In direct numerical simulation at low Reynolds numbers, Kazerooni *et al.* (2017) found that the particle distribution is mainly governed by the bulk Reynolds number.

In order to study the effects of particles on turbulence it is convenient to use a closed set-up where one can relate global and local quantities directly through rigorous mathematical relations. In this paper, the Taylor–Couette (TC) geometry (Grossmann, Lohse & Sun 2016) – the flow between two concentric rotating cylinders – is employed, as this is a closed set-up with global balances. The driving of the TC geometry can be described using the Reynolds number based on the inner cylinder (IC), $Re_i = u_i d / \nu$, where $u_i = \omega_i r_i$ is the azimuthal velocity at the surface of the IC, ω_i is the angular velocity of the IC, $d = r_o - r_i$ is the gap between the cylinders, ν is the kinematic viscosity and r_i (r_o) is the radius of the inner (outer) cylinder. The geometry of TC flow is characterized by two parameters: the radius ratio $\eta = r_i / r_o$ and the aspect ratio $\Gamma = L / d$, where L is the height of the cylinders. The response parameter of the system is the torque, τ , required to maintain constant rotation speed of the inner cylinder. It has been mathematically shown that in TC flow, the angular velocity flux, defined as $J^\omega = r^3 (\langle u_r \omega \rangle_{A,t} - \nu (\partial / \partial r) \langle \omega \rangle_{A,t})$, where the subscript A, t denotes averaging over a cylindrical surface and time, is a radially conserved quantity (Eckhardt, Grossmann & Lohse 2007). One can, in analogy to Rayleigh–B enard convection, normalize this flux and define a Nusselt number based on the flux of the angular velocity,

$$Nu_\omega = \frac{J^\omega}{J_{lam}^\omega} = \frac{\tau}{2\pi L \rho J_{lam}^\omega}, \quad (1.2)$$

where $J_{lam}^\omega = 2\nu r_i^2 r_o^2 (\omega_i - \omega_o) / (r_o^2 - r_i^2)$ is the angular velocity flux for laminar purely azimuthal flow and ω_o is the angular velocity of the outer cylinder. In this spirit, the driving is expressed in terms of the Taylor number,

$$Ta = \frac{1}{4} \sigma d^2 (r_i + r_o)^2 (\omega_i - \omega_o)^2 \nu^{-2}. \quad (1.3)$$

Here, $\sigma = ((1 + \eta) / (2\sqrt{\eta}))^4 \approx 1.057$ is a geometric parameter (‘geometric Prandtl number’), in analogy to the Prandtl number in Rayleigh–B enard convection. In the presented work, where only the inner cylinder is rotated and the outer cylinder is kept stationary, we can relate Ta to the Reynolds number of the inner cylinder by

$$Re_i = \frac{r_i \omega_i d}{\nu} = \frac{8\eta^2}{(1 + \eta)^3} \sqrt{Ta}. \quad (1.4)$$

The scaling of the dimensionless angular velocity flux (torque) with the Taylor (Reynolds) number has been analysed extensively, see, e.g., Lathrop, Fineberg & Swinney (1992), Lewis & Swinney (1999), van Gils *et al.* (2011), Paoletti & Lathrop

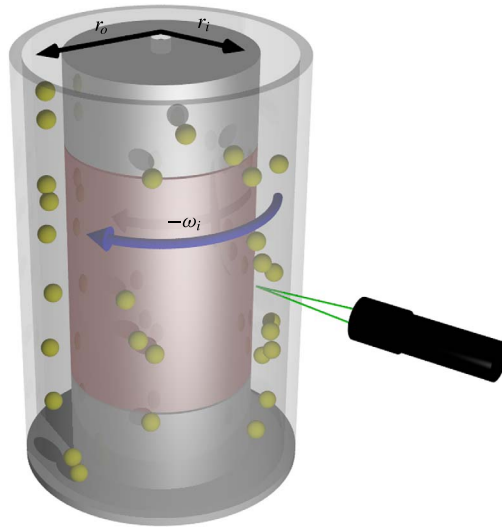


FIGURE 1. (Colour online) Schematic of the TC set-up: two concentric cylinders of radii $r_{i,o}$ with a working fluid in between. Particles are not to scale. The inner cylinder rotates with angular velocity ω_i , while the outer cylinder is kept at rest. We measure the torque on the middle section (highlighted). The laser Doppler anemometry (LDA) probe is positioned at midheight to measure the azimuthal velocity at midgap.

(2011), Ostilla-Mónico *et al.* (2013) and the review articles by Fardin, Perge & Taberlet (2014) and Grossmann *et al.* (2016), and the different regimes are well understood. In the current Taylor number regime, it is known that $Nu_\omega \propto Ta^{0.4}$. Because this response is well known, it can be exploited to study the influence of immersed bubbles and particles (van den Berg *et al.* 2005, 2007; van Gils *et al.* 2013; Maryami *et al.* 2014; Verschoof *et al.* 2016) on the drag needed to sustain constant rotational velocity of the inner cylinder.

In this paper, we will use the TC geometry to study the effect of neutrally buoyant rigid spherical particles on the drag. We study the effects of varying the particle size d_p , the volume fraction α , the density ratio ϕ and the flow Reynolds number Re on the global torque (drag) of the TC flow. The drag reduction is expressed as $DR = (1 - Nu_\omega(\alpha)/Nu_\omega(\alpha = 0))$ and, as we are interested in the net drag reduction, it is not compensated for increased viscosity effects using correction models, such as the Einstein relation.

The paper is organized as follows. Section 2 presents the experimental set-up. In § 3, we discuss the results. The findings are summarized and an outlook for future work is given in the last section.

2. Experimental set-up

The experiments were conducted in the Twente Turbulent Taylor–Couette (T^3C) facility (van Gils *et al.* 2011). A schematic of the set-up is shown in figure 1. In this set-up, the flow is confined between two concentric cylinders, which rotate independently. The top and bottom plates are attached to the outer cylinder. The radius of the inner cylinder (IC) is $r_i = 0.200$ m and the radius of the outer cylinder (OC) is $r_o = 0.2794$ m, resulting in a gap width of $d = r_o - r_i = 0.0794$ m and a

radius ratio of $\eta = r_i/r_o = 0.716$. The IC has a total height of $L = 0.927$ m, resulting in an aspect ratio of $L/d = 11.7$. The IC is segmented axially into three parts. To minimize the effect of the stationary end plates, the torque is measured only over the middle section of the IC with height $L_{mid}/L = 0.58$, away from the end plates. A hollow reaction torque sensor made by Honeywell is used to measure the torque, which has an error of roughly 1% for the largest torques we measured. Between the middle section and the top and bottom sections of the inner cylinder is a gap of 2 mm.

The IC can be rotated up to $f_i = \omega_i/(2\pi) = 20$ Hz. In these experiments, only the IC is rotated and the OC is kept at rest. The system holds a volume of $V = 111$ l of working fluid, which is a solution of glycerol ($\rho = 1260$ kg m⁻³) and water. To tune the density of the working fluid, the amount of glycerol is varied between 0% and 40%, resulting in particles being marginally heavy, neutrally buoyant or marginally light. The system is thermally controlled by cooling the top and bottom plates of the set-up. The temperature is kept at $T = (20 \pm 1)$ °C for all the experiments, with a maximum spatial temperature difference of 0.2 K within the set-up, and we account for the density and viscosity changes of water and glycerol (Glycerine Producers' Association 1963).

Rigid polystyrene spherical particles (RGPballs S.r.l.) are used in the experiments; these particles have a density close to that of water (940–1040 kg m⁻³). We chose particles with diameters $d_p = 1.5, 4.0$ and 8.0 mm. At our disposal are 2.22 l of 1.5 mm diameter particles, 2.22 l of 4 mm diameter particles and 6.66 l of 8 mm diameter particles, resulting in maximum volume fractions of 2%, 2% and 6% respectively. The particles are found to be nearly mono-disperse (99.9% of the particles are within ± 0.1 mm of their target diameter). Due to the fabrication process, small air bubbles are sometimes entrapped within the particles. This results in a slightly heterogeneous density distribution of the particles. After measuring the density distribution for each diameter, we calculated the average for all batches, which was $\rho_p = 1036 \pm 5$ kg m⁻³. By adding glycerol to water, we match this value in order to have neutrally buoyant particles.

Using a laser Doppler anemometry (LDA) system (BSA F80, Dantec Dynamics) we capture the azimuthal velocity at midheight and midgap of the system (see figure 1) and we perform a radial scan at midheight. The flow is seeded with 5 μ m diameter polyamide particles (PSP-5, Dantec Dynamics). Because of the curved surface of the outer cylinder (OC), the beams of the LDA get refracted in a non-trivial manner, which is corrected for using a ray-tracing technique described by Huisman, van Gils & Sun (2012).

Obviously, LDA measurements in a multiphase flow are more difficult to set up than for single-phase flows, as the method relies on the reflection of light from tiny tracer particles passing through a measurement volume (0.07 mm \times 0.07 mm \times 0.3 mm). Once we add a second type of relatively large particles to the flow, this will affect the LDA measurements, mostly by blocking the optical path, resulting in lower acquisition rates. These large particles will also move through the measurement volume, but as these particles are at least 300 times larger than the tracers and thus much larger than the fringe pattern (fringe spacing $d_f = 3.4$ μ m), the reflected light is substantially different from a regular Doppler burst and does not result in a measured value. The minimal signal-to-noise ratio for accepting a Doppler burst is set to 4. As a postprocessing step, the velocities are corrected for the velocity bias by using the transit time of the tracer particle.

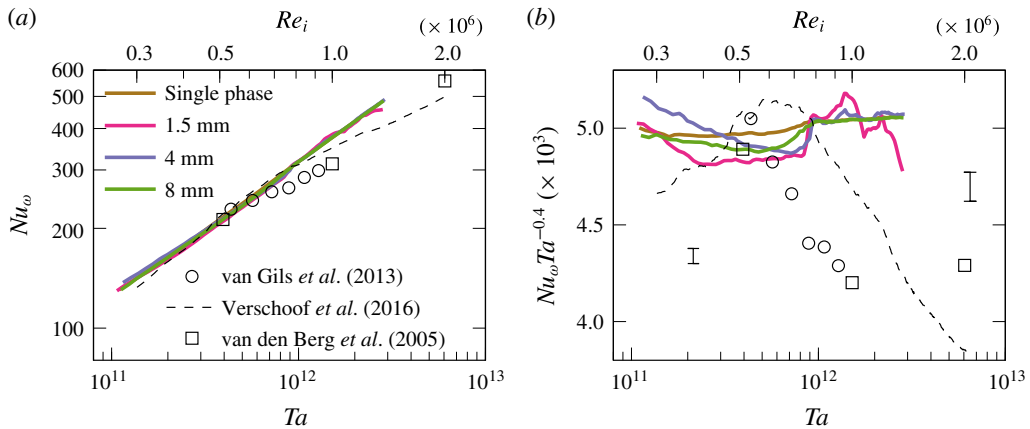


FIGURE 2. (Colour online) (a) A plot of $Nu_\omega(Ta)$ for 2% particle volume fraction with particle diameters of 1.5 mm, 4.0 mm and 8.0 mm, and for comparison the single-phase case. Data from comparable bubbly drag reduction studies are plotted using black markers. (b) The same data, but now as a compensated plot $Nu_\omega/Ta^{0.40}$ as a function of Ta . The error bar indicates the maximum deviation for repeated measurements from all measurements combined (coloured curves), which is less than 1%. At $Ta \geq 2 \times 10^{12}$, the 1.5 mm particles show an increased uncertainty of 1.7%, which is indicated by the right error bar.

3. Results

3.1. Effect of particle size

First, we study the effect of changing the particle diameter on the torque of the system. In these experiments, we kept the particle volume fraction fixed at 2% and the density of the working fluid, ρ_f , at 1036 kg m^{-3} , for which the particles are neutrally buoyant. The results of these measurements are presented as $Nu_\omega(Ta)$ in figure 2(a). Our curves are practically overlapping, suggesting that the difference in drag between the different particle sizes is only marginal. We compare these with the bubbly drag reduction data at similar conditions (hollow symbols) from van den Berg *et al.* (2005), van Gils *et al.* (2013) and Verschoof *et al.* (2016). At low Ta , the symbols overlap with our data. However, at larger Ta , the bubbly flow data show much lower torque (drag) than the particle-laden cases. As we are in the ultimate regime of turbulence where Nu_ω effectively scales as $Nu_\omega \propto Ta^{0.4}$ (Huisman *et al.* 2012; Ostilla-Mónico *et al.* 2013), we compensate the data with $Ta^{0.40}$ in figure 2(b) to emphasize the differences between the datasets. For the single-phase case, this yields a clear plateau. For the particle-laden cases, the lowest drag corresponds to the smallest particle size. The reduction is, however, quite small (<3%). The compensated plots also reveal a sudden increase in drag at a critical Taylor number of $Ta^* = 0.8 \times 10^{12}$. The jump is more distinct for the smaller particles, and might suggest a reorganization of the flow (Huisman *et al.* 2014). Beyond Ta^* , the drag reduction is negligible for the larger particles (4 mm and 8 mm spheres). However, for the 1.5 mm particles, the drag reduction seems to increase, and was found to be very repeatable in experiments. Interestingly, the size of these particles is comparable to that of the air bubbles in van Gils *et al.* (2013). This might suggest that for smaller size particles at larger Ta , one could expect drag reduction. At the increased viscosity of the suspension, a maximum $Ta \approx 3 \times 10^{12}$ could be reached in our experiments.

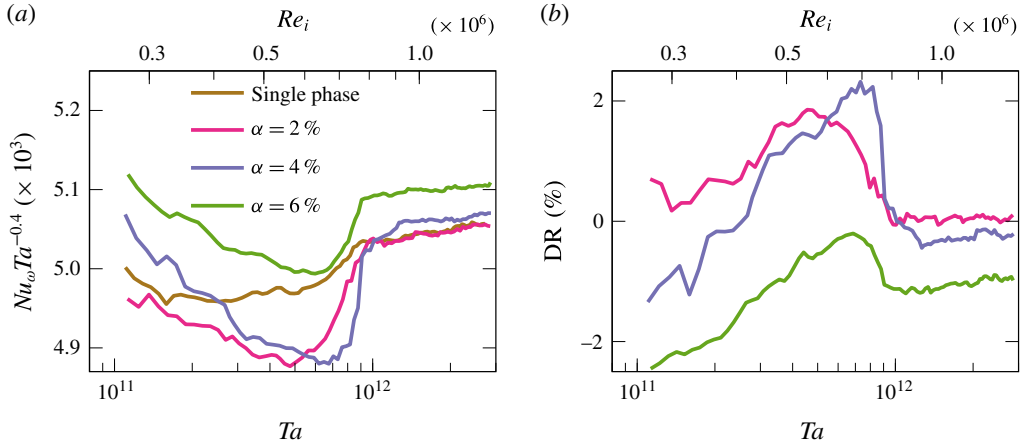


FIGURE 3. (Colour online) (a) A plot of $Nu_\omega(Ta)$, compensated by $Ta^{0.4}$, for 8 mm particles with various particle volume fractions, and for comparison the single-phase case. (b) The drag reduction, defined as $DR = (1 - Nu_\omega(\alpha)/Nu_\omega(\alpha = 0))$, plotted against Ta .

We have performed an uncertainty analysis by repeating the measurements for the single phase and for the cases with 8 mm and 1.5 mm particles multiple times and calculating the maximum deviation from the ensemble average. The left error bar indicates the maximum deviation for all measurements combined and is $\approx 1\%$. For $Ta \geq 2 \times 10^{12}$, we see an increase in uncertainty of 1.7% (shown by the right error bar in figure 2b), which is only caused by the 1.5 mm particles. These tiny particles can accumulate in the 2 mm gap between the cylinder segments and thereby increase the uncertainty. Above $Ta \geq 2 \times 10^{12}$, both the 8 mm and 4 mm particles show a maximum deviation below 0.25%.

Below Ta^* , the drag reduction due to spherical particles appears to be similar to bubbly drag reduction (van Gils *et al.* 2013). However, in the lower- Ta regime, the bubble distribution is highly non-uniform due to the buoyancy of the bubbles (van den Berg *et al.* 2005; van Gils *et al.* 2013; Verschoof *et al.* 2016). Therefore, the volume fractions reported are only the global values, and the torque measurements are for the midsections of their set-ups. What is evident from the above comparisons is that in the high- Ta regime, air bubbles drastically reduce the drag, reaching far beyond the drag modification by rigid spheres.

3.2. Effect of particle volume fraction

The next step is to investigate the effect of the particle volume fraction on the torque. For the 8 mm particles, we have the ability to increase the particle volume fraction up to 6%. This is done in steps of 2%, and the results are plotted in compensated form in figure 3(a). The normalized torque increases with the volume fraction of particles. The 6% case shows the largest drag. Figure 3(b) shows the same data in terms of drag reduction as function of Ta . A 2% volume fraction of particles gives the highest drag reduction. With increasing α , the drag reduction decreases. These measurements are in contrast to the findings for bubbly drag reduction (van Gils *et al.* 2013), for which the net drag decrease with increasing gas volume fraction of drag in a particle-laden flow is the larger apparent viscosity. If we were to calculate the drag modification using an apparent viscosity (e.g. the Einstein relation (1.1)) for the case using $\alpha = 6\%$

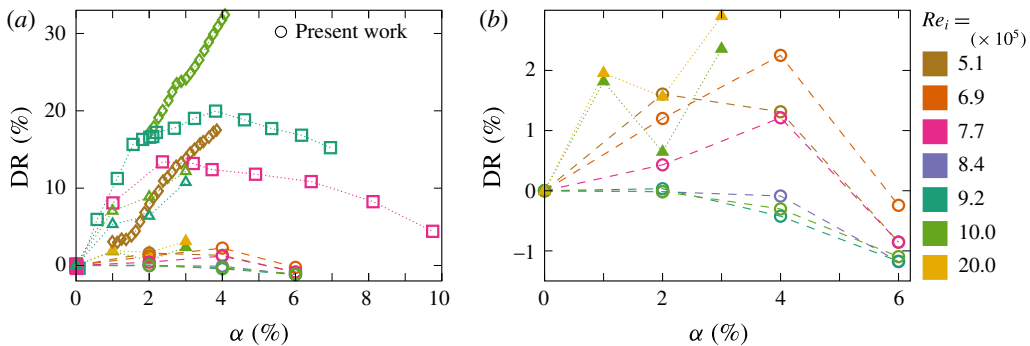


FIGURE 4. (Colour online) (a) Drag reduction as function of particle volume fraction from \circ $d_p = 8$ mm particles from the present work compared with similar gas volume fractions from \square van den Berg *et al.* (2005), \diamond van Gils *et al.* (2013) and \triangle Verschoof *et al.* (2016). Symbols indicate the different studies while colours differentiate between the Reynolds numbers. The current work has DR defined as $(1 - Nu_\omega(\alpha)/Nu_\omega(\alpha = 0))$; the other studies use dimensionless torque G (van Gils *et al.* 2013), friction coefficient c_f (van den Berg *et al.* 2005) or plain torque τ (Verschoof *et al.* 2016) to define DR. (b) Zoom of the bottom part of (a) where the data from the present work are compared with bubbly drag reduction data using 6 ppm of surfactant from Verschoof *et al.* (2016).

of particles, the measured drag would be 15% larger compared to the pure working fluid case. Inclusion of this effect in our drag reduction calculation would result in reductions of the same order. However, when comparing the drag with or without particles, the net drag reduction is practically zero. This result is different from the work of Picano *et al.* (2015) in turbulent channel flow, where they found that the drag increased more than the increase of the viscosity.

For a better comparison with bubbly drag reduction, we plot the drag reduction as a function of (gas or particle) volume fraction α ; see figure 4(a). Different studies are shown using different symbols, and Re is indicated by colours. None of the datasets were compensated for the changes in effective viscosity. The DR is defined in a slightly different way in each study: van den Berg *et al.* (2005) makes use of the friction coefficient $(1 - c_f(\alpha)/c_f(0))$; van Gils *et al.* (2013) uses the dimensionless torque $G = \tau/(2\pi L_{mid}\rho v^2)$, $(1 - G(\alpha)/G(0))$; Verschoof *et al.* (2016) uses the plain torque value $(1 - \tau(\alpha)/\tau(0))$. While the rigid particles only show marginal drag reduction, some studies using bubbles achieve dramatic reduction of up to 30% and beyond. Figure 4(b) shows a zoomed in view of the bottom part of the plot with the rigid-sphere data. The triangles denote the data from Verschoof *et al.* (2016), corresponding to small bubbles in the TC system. The rigid particles and the small bubbles show a similar drag response. What is remarkable is that this occurs despite the huge difference in size. The estimated diameter of the bubbles in Verschoof *et al.* (2016) is 0.1 mm, while the rigid spheres are approximately two orders in magnitude larger. This provides key evidence that the particle size alone is not enough to cause drag reduction, the density ratio of the particles and the carrier fluid is also of importance.

3.3. Effect of marginal changes in particle density ratio

With the effects of particle size and volume fraction revealed, we next address the sensitivity of the drag to marginal variations in particle density. A change in the

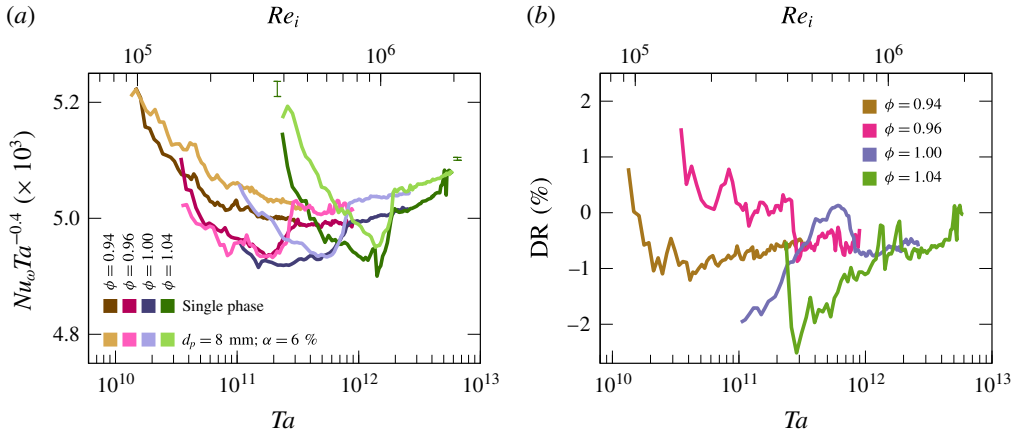


FIGURE 5. (Colour online) (a) A plot of Ta as a function of Nu_ω compensated by $Ta^{0.4}$ for various density ratios $\phi = \rho_p/\rho_f$ indicated by the corresponding colour. The darker shades indicate the single-phase cases while the lighter shades show the cases using 6% particle volume fraction of 8 mm diameter particles. Due to the increase in viscosity, the maximum attainable Ta is lower for larger density ratios. The uncertainty is again estimated using the maximum deviation from the average for multiple runs and here is only shown for the green curves. This value is slightly below 1% at lower Ta and decreases with increasing Ta to values below 0.25%. This trend is seen for all values of ϕ . (b) The drag reduction, calculated from the data of (a), plotted against Ta . The drag reduction is defined as $DR = (1 - Nu_\omega(\alpha = 6\%)/Nu_\omega(\alpha = 0\%))$.

particle density ratio brings about a change in the buoyancy and centrifugal forces on the particle, both of which can affect the particle distribution within the flow. We tune the particle to fluid density ratio $\phi \equiv \rho_p/\rho_f$ by changing the volume fraction of glycerol in the fluid, such that the particles are marginally buoyant ($\phi = 0.94, 0.97$), neutrally buoyant ($\phi = 1.00$) and marginally heavy ($\phi = 1.04$) particles. In figure 5(a), we show the compensated Nu_ω as a function of Ta for various values of ϕ . Here, α is fixed to 6% and only 8 mm particles are used. The darker shades of colour correspond to the single-phase cases, while lighter shades correspond to particle-laden cases. In general, the single-phase drag is larger as compared with the particle-laden cases. However, there is no striking difference between the different values of ϕ . In figure 5(b), we present the drag reduction for particle-laden cases at different density ratios. On average, we see for all cases drag modification of approximately $\pm 2\%$. We can also identify a small trend in the lower- Ta region: the two larger ϕ cases (heavy and neutrally buoyant particles) tend to have a drag increase, while the smaller ϕ cases (both light particles) have a tendency for drag reduction. Nevertheless, the absolute difference in DR between the cases is within 4%. The above results provide clear evidence that minor density mismatches do not have a serious influence on the global drag of the system. To investigate for strong buoyancy effects, additional measurements were made using 2 mm expanded polystyrene particles ($\phi = 0.02$). However, due to the particles accumulating between the inner cylinder segments leading to additional mechanical friction, these measurements were inconclusive.

3.4. Flow statistics using particles

In the above sections, we presented the effects of changing particle size, volume fraction and density on the global drag of the system. Next, we look into local

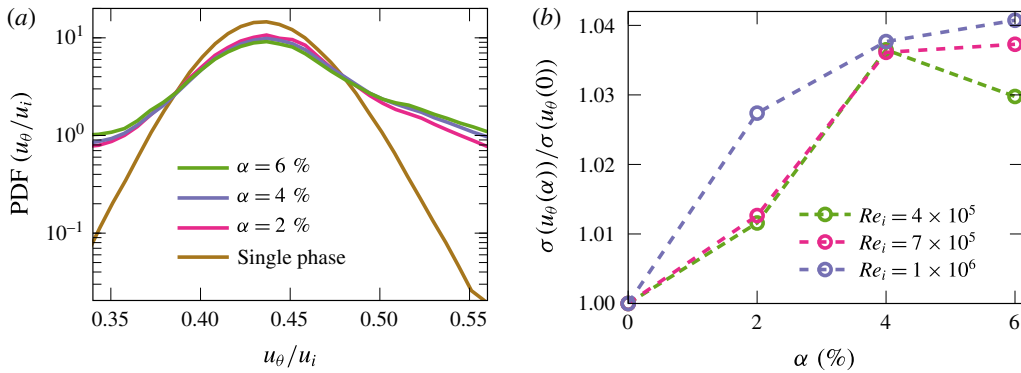


FIGURE 6. (Colour online) (a) Probability density functions of u_θ/u_i for various values of α and the single-phase case. The particle size is fixed to 8 mm and $Re_i = 1 \times 10^6$ for all cases. (b) Standard deviation of the azimuthal velocity normalized by the standard deviation of the single-phase case for three different values of Re for a fixed particle size of 8 mm.

flow properties using LDA while the particles are present. First, we collect a total of 1×10^6 data points of azimuthal velocity at midheight and midgap. These are captured over a period of approximately 3×10^4 cylinder rotations. From these data, we calculate the probability density function (PDF) of u_θ normalized by u_i for various values of α , shown in figure 6(a). The particle size is fixed to 8 mm and the Reynolds number is set to 1×10^6 . From this figure, we see a large increase in turbulent fluctuations, resulting in very wide tails. While the difference between 2%, 4% and 6% is not large, we can identify an increase in fluctuations with increasing α . These increased fluctuations can be explained by the additional wakes produced by the particles (Poelma *et al.* 2007; Alm eras *et al.* 2017). The increase in fluctuations can also be visualized using the standard deviation of $\sigma(u_\theta) = \langle u_\theta^2 \rangle^{1/2}$ normalized by the standard deviation of the single-phase case – see figure 6(b). In this figure, $\sigma(u_\theta)$ is shown for three different values of Re , again for 8 mm particles. In general, we see a monotonically increasing trend with α , and it seems to approach an asymptotic value. One can speculate that there has to be an upper limit for fluctuations that originate from wakes of the particles. For large α , the wakes from particles will interact with one another and with the carried flow.

Measurements using 4 mm particles yielded qualitatively similar results. It is known that in particle-laden gaseous pipe flows, large particles can increase the turbulent fluctuations, while small particles result in turbulence attenuation (Tsuji, Morikawa & Shiomi 1984; Gore & Crowe 1989; Vreman 2015). The LDA measurements were not possible with the smallest particles (1.5 mm), as the large amount of particles in the flow blocked the optical paths of the laser beams.

We are confident that for these bidisperse particle-laden LDA measurements, the large particles do not have an influence on the measurements as these millimetric-sized particles are much larger than the fringe spacing ($d_f = 3.4 \mu\text{m}$) and do not show a Doppler burst. However, during the measurements, the particles get damaged and small bits of material are fragmented off the particles. We estimate the size of these particles to be slightly larger than the tracer particles, and these can have an influence on the LDA measurements as they do not act as tracers.

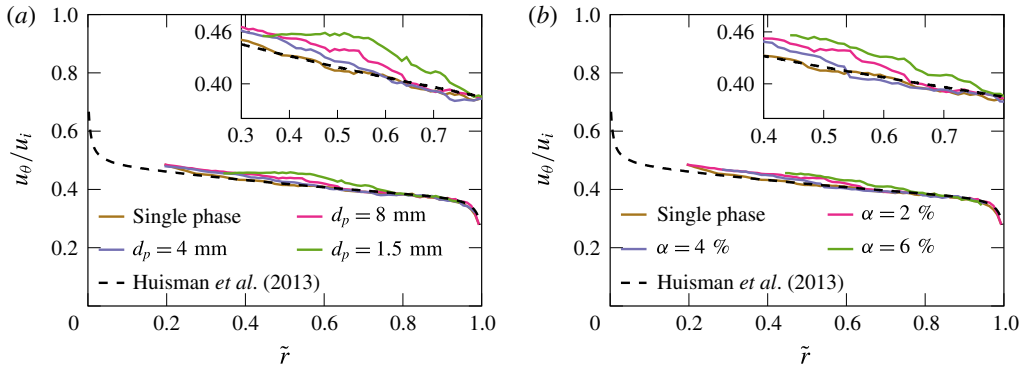


FIGURE 7. (Colour online) A plot of u_θ normalized by the velocity of the inner cylinder wall u_i as a function of the normalized radius for various values d_p while $\alpha = 2\%$ (a) and various values of α while $d_p = 8$ mm (b). In all cases, Re_i is fixed to 1×10^6 . For comparison, the single-phase case using water at $Re_i = 1 \times 10^6$ from Huisman *et al.* (2013) is also plotted in dashed black in both plots. Both plots have an inset showing an enlargement of the centre area from the same plot.

The way in which the average azimuthal velocity changes with particle radius is shown in figure 7. We measured a total of 3×10^4 data points during approximately 900 cylinder rotations. Again, the data are corrected for velocity bias by using the transit time as a weighing factor. Figure 7(a) shows the effect of particle size for $\alpha = 2\%$ and figure 7(b) shows the effect of particle volume fraction for 8 mm particles. Both figures additionally show the high-precision single-phase data from Huisman *et al.* (2013), for which our single-phase measurements are practically overlapping. Since LDA measurements close to the inner cylinder are difficult, due to the reflecting inner cylinder surface, we limited our radial extent to $\tilde{r} = (r - r_i)/(r_o - r_i) = [0.2, 1]$. We found that the penetration depth of our LDA measurements is the smallest for experiments with the smallest particles and the largest α . All differences from the single-phase case are only marginal and we can conclude that the average mean velocity is not much affected by the particles in the flow, at least for $\tilde{r} \geq 0.2$.

To get an idea of the fluctuations we can use the previous data to construct two-dimensional PDFs of the azimuthal velocity as a function of radius. These are shown for $Re = 1 \times 10^6$ using 8 mm particles at various values of α and the single-phase case in figure 8. The first thing to notice is again that the penetration depth decreases with increasing α . The single-phase case shows a narrow-banded PDF. When α is increased, for the lower values of \tilde{r} , the PDF is much wider. While it makes sense that an increase in α increases the fluctuations due to the increased number of wakes of particles, this is expected everywhere in the flow, not only closer to the inner cylinder. It is possible that the particles have a preferred concentration closer to the inner cylinder. We tried to measure the local concentration of particles as a function of radius but failed due to limited optical accessibility. Therefore, we can only speculate under what circumstances there would be an inhomogeneous particle distribution that would lead to the visible increase in fluctuations. The first possibility is a mismatch in density between the particles and the fluid, which would result in light particles ($\phi < 1$) accumulating closer to the inner cylinder. Another possibility is that due to the rotation of the particles, an effective lift force arises, leading to a different particle

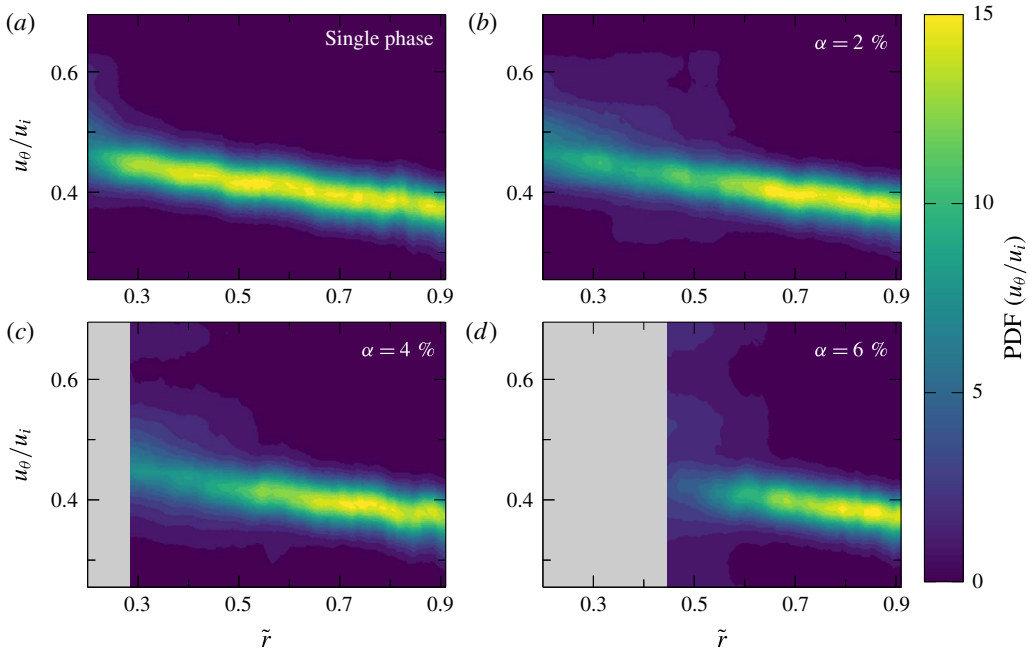


FIGURE 8. (Colour online) Probability density functions of the normalized azimuthal velocity as a function of the normalized radial position for various values of α for the case of 8 mm particles and the single-phase case while keeping Re at 1×10^6 . With increasing α , the maximum penetration depth decreases. The grey areas indicate radial positions for which no data are available.

distribution in the flow. While this is quite plausible, this is difficult to validate as we would need to capture the rotation. The fragments of plastic that are sheared off the particles can also give a bias to the LDA measurement. While we estimate them to be larger than the tracers, they might still be small enough to produce a signal, and they might not follow the flow faithfully.

4. Conclusions and outlook

We have conducted an experimental study on the drag response of a highly turbulent TC flow containing rigid neutrally buoyant spherical particles. We have found that, unlike the case of bubbles used in prior works (van Gils *et al.* 2013; Verschoof *et al.* 2016), rigid particles barely reduce (or increase) the drag on the system, even for cases where their size is comparable to that of the bubbles used in other studies. There is no significant size effect. Even for very large particles, which can attenuate turbulent fluctuations and generate wakes, there is no distinct difference from the single-phase flow. We also varied the volume fraction of the particles in the range 0%–6%. The particle volume fraction has no greater effect on the system drag than what is expected due to changes in the apparent viscosity of the suspension. Further, we tested the sensitivity of our drag measurements to marginal variations in the particle to fluid density ratio ϕ . A trend was noticeable, towards drag reduction when ϕ was reduced from 1.00 to 0.94. This suggests that a low density of the particles could be a necessary ingredient for drag reduction. Finally, we have also

probed the local flow at the midheight and midgap of the system using LDA. With the addition of particles, the liquid velocity fluctuations are enhanced, with wider tails of the distributions. A finite relative velocity between the particle and the flow around it can cause this increase in velocity fluctuations (Mathai *et al.* 2015), as seen for bubbly flows (pseudo-turbulence) and in situations of sedimenting particles in quiescent or turbulent environments (Gore & Crowe 1989). In the present situation, the relative velocity between the particle and the flow is expected, due to the inertia of the finite-sized particles we used. There is only a marginal deviation from the single-phase case in the average azimuthal velocity over the radial positions measured using any size or concentration of particles measured. From the two-dimensional PDFs, we see that closer to the inner cylinder, using smaller d_f or larger α , the PDF gets wider. This could be due to a preferential concentration of the particles or a slight density mismatch.

Our study is a step towards a better understanding of the mechanisms of bubbly drag reduction. Bubbles are deformable, and they have a tendency to migrate towards the walls, either due to lift force (Dabiri *et al.* 2013) or due to centripetal effects (van Gils *et al.* 2013). When compared with the drag reducing bubbles in van Gils *et al.* (2013) and Verschoof *et al.* (2016), our particles do not deform, and they do not experience centripetal effects as they are density matched. At least one of these differences must therefore be crucial for the observed bubbly drag reduction in those experiments. In a future investigation, we will conduct more experiments using very light spherical particles that experience similar centripetal forces to the bubbles in van Gils *et al.* (2013), but are non-deformable. These particles need to be larger than the size of the gap between the inner cylinder segments, and very rigid, or the set-up needs to be modified to close the gap between the IC segments. Such experiments can then disentangle the role of particle density on drag reduction from that of the particle shape.

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