

RESEARCH ARTICLE

A new model for radiocarbon dating of marine shells from the Netherlands

J van der Plicht  and H J Streurman

Center for Isotope Research, Faculty of Science and Engineering, University of Groningen, the Netherlands

Corresponding author: J van der Plicht; Email: j.van.der.plicht@rug.nl

Received: 28 November 2023; **Revised:** 12 August 2024; **Accepted:** 16 August 2024

Keywords: age model; the Netherlands; radiocarbon; reservoir effect; shell dating; stable isotopes

Abstract

A new model for the interpretation of radiocarbon (^{14}C) dates of Holocene marine shells is presented. For the Netherlands, the size of reservoir effect is difficult to assess, as these shells often lived in an environment of mixed marine- and river waters. Both stable isotopes ^{13}C and ^{18}O of the shell carbonate give insight in the environmental conditions the shells lived in. River water occurs in two main categories, distinguished by ^{18}O : the Rhine which is dominant, and other rivers. This leads to two estuary mixing lines between the North Sea and rivers. The stable isotopes of the shell carbonate are also indicative for additional processes, such as uptake of secondary carbonate from the soil by shells, and exchange of C isotopes between atmosphere and water. Extensions of the main model deal with special cases such as pools of stagnant water and lakes. The model leads to an assessment of the recent ^{14}C activities of the system the shells lived in, called $^{14}\text{a}^{\text{SYS}}$. The measured ^{14}C activities relative to these $^{14}\text{a}^{\text{SYS}}$ values determine the ^{14}C age of the shells and include the reservoir effect. This way we circumvent normalizing to $\delta^{13}\text{C} = -25\text{‰}$, i.e. the terrestrial timescale and the subsequent correction for reservoir effects. The model is applied to a large legacy dataset of marine shells from the Netherlands, obtained during the last 7 decades. It contains 1116 ^{14}C dated shells; for the majority of these, the 3 isotopes ^{13}C , ^{14}C and ^{18}O are measured.

Introduction

Radiocarbon (^{14}C) dates are by convention normalized for fractionation using the stable carbon isotope to $\delta^{13}\text{C} = -25\text{‰}$. Together with other normalizations (concerning half-life and standard activity), this defines the timescale in BP (Mook and van der Plicht 1999; Stuiver and Polach 1977). This timescale is valid for terrestrial samples. Aquatic shells are subject to reservoir effects. Generally, aquatic reservoirs contain less ^{14}C than terrestrial reservoirs and the atmosphere, causing an offset in ^{14}C dates. Therefore, when aquatic dates are normalized for fractionation and expressed in BP, subtraction of reservoir effects is needed for a correct age estimation (e.g. Cook et al. 2001; Lanting and van der Plicht 1998; Olsson 1983; Philippsen 2013).

For marine surface samples, a general value of 400 years applies for the size of the reservoir effect for the Southern North Sea during the Holocene. Our dataset concerns this locality and time range. For other regions and time periods, the magnitude of the reservoir effect can be different (Alves et al. 2018). We note that for the present calibration curve Marine20 (which is model based) it is more like 550 years (Heaton et al. 2020, 2023).

For absolute shell dates (BC, AD or calBP) this 400 years needs to be subtracted (from the measured date in BP) before calibrating using the terrestrial calibration curve IntCal20 (Reimer et al. 2020). Alternatively, one can calibrate the BP date using the marine calibration curve Marine20 (Heaton et al. 2020), which incorporates the reservoir effect. Marine20 takes into account temporal and local offsets from the global average value. The marine reservoir effect is caused by upwelling of deep ocean waters

which are old and thus depleted in ^{14}C . The surface ocean exchanges CO_2 (including $^{14}\text{CO}_2$) with the atmosphere but is not recent (in terms of ^{14}C) because of mixture with this upwelling deep and old ocean water.

The general “400 years rule” only works for pure marine shells. For other aquatic reservoirs like rivers different values apply. This reservoir effect is mainly caused by dissolved fossil (^{14}C -free) carbonate. For the Netherlands, the dominant river is the Rhine which shows reservoir effects of around 1300 years (Lanting and van der Plicht 1998; Mook 2006). Other water bodies may show different values. This is the case for estuaries and lagoons, which consist of a mixture of sea- and river waters.

There is no general numerical reservoir effect value that can be used for shells from aquatic waters other than 100% marine, such as rivers, lakes, lagoons, estuaries and other mixed water bodies. Only in exceptional cases one can compare ^{14}C dates of shells directly with those from terrestrial samples. Examples are shells from a well defined archaeological context or geological stratum. There are even cases where there is no (or small) reservoir effect, such as stagnant waters which can reach CO_2 equilibrium with the atmosphere (e.g. van der Plicht et al. 2020). Hence, transformation of ^{14}C dates of shells from not-100% marine environments into absolute dates is problematic. This is the case for several hundreds of shell dates measured over the years (since 1952) in Groningen. The dataset consists of marine shells, as well as many shells from rivers, lakes, stagnant waters, estuaries and a variety of mixed water bodies.

We developed a model for obtaining absolute dates for such shells. It uses both stable isotopes ^{13}C and ^{18}O of the shell carbonate as tracers to reconstruct the isotopic environment where the shell species lived in, taking into account mixing of waters, fractionation and isotopic exchange processes. This way we can circumvent the need for reservoir effect correction, in fact by not normalizing to the terrestrial timescale. This more or less follows the practice used in isotope hydrology (Clark and Fritz 1997; Mook 2006). The modeled ^{14}C activities result in dates that can be made absolute by using the calibration curve IntCal20 (Reimer et al. 2020). These modeled dates are equivalent to but should not be expressed in the unit BP because they are not normalized for fractionation; they are formally not conventional. We will use here “ ^{14}C years” or “modeled years.”

The present work is enabled by our large dataset of shells. It is unique by virtue of its size, and a large amount of ^{18}O measurements. The latter isotope was not commonly measured in the first decades of radiocarbon dating. Of importance is also that the shells originate from a well studied delta including much archaeological and geophysical knowledge for a relatively small region. The dataset provides proper testing of our model.

The large density of measurements even allows to estimate the $\delta^{18}\text{O}$ value for the shells for which only the $\delta^{13}\text{C}$ value has been measured. This enables the application of our model to derive ^{14}C ages (albeit with increased uncertainty). The full dataset is available as supporting online material. It includes all shells analyzed in Groningen during the years 1952–2023. Detailed applications concerning past landscape developments in the Netherlands will be published in the more specialized or local geophysical/archaeological literature.

Dataset and methods

The shell carbonate dataset measured in Groningen contains 1116 shells of the Netherlands which are dated by ^{14}C . For about 70% of these, the 3 isotopes ^{13}C , ^{14}C and ^{18}O are measured.

There is a significant amount of shells for which only the two carbon isotopes are measured.

In addition, 20 shell dates measured in the 1950s do not have stable isotope data at all, also not ^{13}C . These data are valuable nevertheless, the lacking stable isotopes can often be estimated (justified by the mere size of the total dataset) and subsequently be analyzed by our model.

In this article we focus on shells with the 3 isotopes available from a Holocene geophysical context, which amounts to about 700 shells. The remaining data concern shells from an archaeological context, recent shells and a few shells which appeared to be of Pleistocene age.



Figure 1. Modern map of the Netherlands, showing the main water bodies: the North Sea, Waddensea and Lake IJssel, and the rivers Scheldt, Meuse, Rhine and IJssel. The coastal provinces are indicated, as well as the closure dike (Afsluitdijk) between North Sea/Waddensea and Lake IJssel, the former Zuiderzee. “A” is the location of Amsterdam.

Over the years, a selection of measurements found their way in publications and theses. These were usually interpreted in the users community using a reservoir effect of 400 years. For completeness, also included is a dataset of 264 shells for which only the stable isotopes ^{13}C and ^{18}O are measured; these were mostly analyzed before the introduction of AMS.

A modern map of the Netherlands is shown in Figure 1. The datatables are organized according to regions. These regions correspond to provinces, except for the Wadden Islands, which belong to three provinces and are taken together here. Figure 1 also shows the main water bodies: the North Sea and the rivers Rhine, Meuse and Scheldt. The Rhine is the dominant river; the flow rate is about $2000\text{ m}^3/\text{s}$. For the Meuse, that is $230\text{ m}^3/\text{s}$; for the Scheldt, $120\text{ m}^3/\text{s}$. These numbers indicate the annual averages. The IJssel river is a separate branch of the Rhine. The Lake IJssel is a freshwater inner lake; it used to be part of the North Sea called Zuiderzee. Since 1932 it is disconnected from the sea by a 32 km long closure dike (called Afsluitdijk). The former lake area is partly used for land reclamation and is today the province of Flevoland.

For illustrative purposes, a map showing a reconstruction of the country dating 3850 BC is included (Figure 2). The map is taken from Vos (2015). Maps from other times during the Holocene are also available, these can be obtained from the Rijksdienst voor het Cultureel Erfgoed (2024). Together they provide an excellent illustration of the temporal changes in the prehistoric landscape during the Holocene, in particular the development of coastline, lakes, estuaries and course of rivers.

The ^{14}C shell dates were obtained by 4 different instrumental methodologies: the conventional method (laboratory code GrN, used until 2011; Mook and Stuiver 1983), AMS using the Tandem (laboratory code GrA, used 1994-2017; Aerts et al. 2001; van der Plicht et al. 2000) and the Micadas (laboratory code GrM, used since 2017; Dee et al. 2020). Before Groningen had an operational AMS facility, shells were pretreated and graphitized in Groningen and subsequently AMS-dated in Uppsala (laboratory code Ua; van Klinken 1991). The stable isotope ratios were all measured by Isotope Ratio Mass Spectrometry (IRMS) in Groningen.

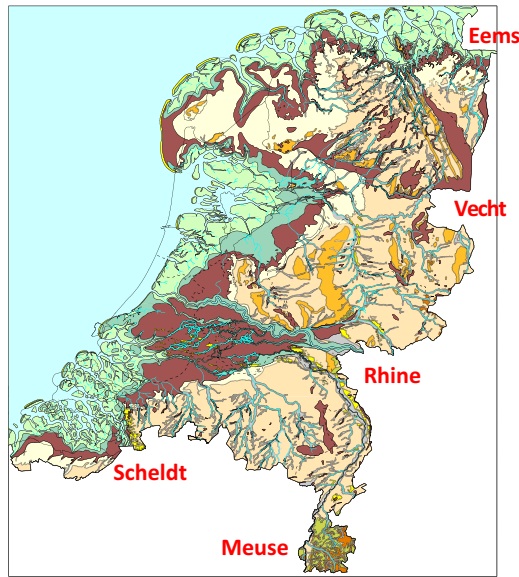


Figure 2. Map of the Netherlands dating ca. 3850 BC. The modern provinces are shown by the black lines. The map is taken from Vos (2015), which reference also contain maps from other times during the Holocene. The rivers Rhine, Meuse, Scheldt, Vecht and Eems are indicated.

The stable isotope ratios are expressed in a delta value, which for ^{13}C is a measure of the difference of the $^{13}\text{C}/^{12}\text{C}$ isotope ratio of a sample and that of a reference material:

$$^{13}\delta = \delta^{13}\text{C} = \left(\frac{^{13}\text{C}/^{12}\text{C}}{\text{sample}} / \left(\frac{^{13}\text{C}/^{12}\text{C}}{\text{reference}} \right) - 1 \right) (\times 1000\text{‰}) \quad [1]$$

Similar, for ^{18}O this is:

$$^{18}\delta = \delta^{18}\text{O} = \left(\frac{^{18}\text{O}/^{16}\text{O}}{\text{sample}} / \left(\frac{^{18}\text{O}/^{16}\text{O}}{\text{reference}} \right) - 1 \right) (\times 1000\text{‰}) \quad [2]$$

For both ^{13}C and ^{18}O in carbonates, the reference is an international standard limestone known as Pee Dee Belemnite, or PDB which has an accurately measured absolute ^{13}C concentration. For ^{18}O in water, the reference is SMOW (standard mean ocean water). The reference materials have accurately measured absolute isotope concentrations. For more details, see Mook (2006) and references therein. The short notations $^{13}\delta$ and $^{18}\delta$ will be used in the more complex formulas in order to make them better readable. The measurement precision of the stable isotope ratios is about 0.1‰.

The ^{14}C measurements are reported in activity ratios ^{14}a , as defined by Mook and van der Plicht (1999). It follows the convention by using the half-life value of 5568 years (the Libby value) and standard activity (95% of the activity of the specific batch of Oxalic Acid nr.1 in 1950).

The convention also requires a correction for isotopic fractionation to $\delta^{13}\text{C} = -25\text{‰}$, here called normalization using

$$^{14}\text{a}_\text{N} = ^{14}\text{a}[1 - 2(\delta^{13}\text{C} + 0.025)] \quad [3]$$

which is valid as a good approximation (Mook 2006). The $\delta^{13}\text{C}$ reference value of -25‰ is chosen as typical for charcoal, wood and peat of C3 plants (Mook and Streurman 1983). The normalized activity ratio $^{14}\text{a}_\text{N}$ is equivalent to $F^{14}\text{C}$; see e.g. van der Plicht and Hogg (2006) for the nomenclature. Both lead to ^{14}C dates in BP, the terrestrial timescale.

Table 1. General contents of the stable isotopes ^{13}C and ^{18}O for water and shell carbonate in the Netherlands. For water, the values of Chlorinity [Cl] and modern ^{14}C activity (named $^{14}\text{a}^{\text{SYS}}$, see text) are also shown

Reservoir	Water					Shell carbonate		
	$\delta^{13}\text{C}$ ‰ PDB HCO_3^-	conc. HCO_3^- mmol/L	$\delta^{18}\text{O}$ ‰ SMOW H_2O	[Cl] ‰	$^{14}\text{a}^{\text{SYS}}$ %	$\delta^{13}\text{C}$ ‰ PDB CaCO_3	$\delta^{18}\text{O}$ ‰ PDB CaCO_3	Model
North Sea	1.5	2.5	0	19.3	100	1.5	1.0	
Rhine river	-10.5	2.5	-10.0	0	85	-10.5	-9.0	R
Other rivers	-10.5	2.5	-7.3	0	85	-10.5	-6.3	P

This normalization leads to an offset with dates of aquatic origin, known as the reservoir effect. For the model introduced in this manuscript, we use not-normalized ^{14}C activity ratios, ^{14}a (and not $^{14}\text{a}_\text{N}$) in order to avoid the need for reservoir corrections.

For conventional samples, the ^{14}C activities are directly measured in CO_2 by proportional gas counters, leading to ^{14}a values (using the conventional half-life and oxalic acid standard). For the same gas, also the $\delta^{13}\text{C}$ value is measured by IRMS (Mook and Streurman 1983).

For AMS samples however, ambiguities do exist. The CO_2 gas is transferred into graphite; the AMS measures the ^{13}C and ^{14}C concentration in the graphite (Dee et al. 2020). The AMS dates are subsequently normalized using the $\delta^{13}\text{C}$ value as measured by the AMS. This takes into account the fractionation caused by the graphite production and in the accelerator system, which can be significant.

The $\delta^{13}\text{C}$ value for all samples is also measured by IRMS. Hence there are two measurements available for the $\delta^{13}\text{C}$ values. The AMS $\delta^{13}\text{C}$ value is less precise than the one measured by IRMS, typically by about one order of magnitude. The IRMS value is reported, the one measured by AMS is not reported. The IRMS $\delta^{13}\text{C}$ value represents the proper ^{13}C value of the shell; the AMS $^{14}\text{a}_\text{N}$ value or BP date is calculated using the AMS $\delta^{13}\text{C}$ value. For normalized dates this is not an issue. However, our model is based on ^{14}a (i.e. not $^{14}\text{a}_\text{N}$). The problem is solved by de-normalizing the AMS $^{14}\text{a}_\text{N}$ value using the IRMS-measured proper $\delta^{13}\text{C}$ value:

$$^{14}\text{a} = ^{14}\text{a}_{\text{N,AMS}} / [1 - 2(\delta^{13}\text{C}_{\text{IRMS}} + 0.025)] \quad [4]$$

The effect is not large, usually well within the measurement uncertainty.

The modeled ^{14}C dates, based on not-normalized ^{14}C activities are calibrated using IntCal20 (Reimer et al. 2020) and the OxCal code (version 4.4, <https://c14.arch.ox.ac.uk/oxcal/OxCal.html>). In our tables the calibrated dates are reported in calBP, i.e. calendar years relative to 1950 AD. Reported are the 95.4% probability date ranges, rounded to 5 years and taking separated date ranges together.

Isotopes in water and carbonate

Our model is based on the isotopes ^{13}C , ^{14}C and ^{18}O in natural waters and carbonate. The general isotope values for the main reservoirs relevant for the Netherlands are shown in Table 1. The table distinguishes the three main water bodies marine (the North Sea) and rivers (Rhine and others).

The chlorinity of the water is shown as [Cl]. This [Cl] value is defined as the concentration of chloride (plus bromide and iodide) given in g/kg or ‰ (Mook 1971, 2006). For the sea, the Cl concentration is 560 mmol/L, which corresponds to 19.36 ppt (g/kg) or 19.36‰. Freshwater does not contain Cl, hence its concentration is 0 mmol/L or 0‰.

For North Sea water, measurements show that for dissolved inorganic carbon (DIC) the typical value for $\delta^{13}\text{C}$ is 1.5‰ which is based on measurements by Mook (1968, 104). The $\delta^{18}\text{O}$ value is 0 (the SMOW reference value). Also, for shell carbonate, the $\delta^{13}\text{C}$ values for a large body of North Sea shells

have been measured, resulting in a typical value of 1.5‰. For $\delta^{18}\text{O}$, the fractionation between water and shell carbonate is known to be 1‰ (Mook 1968, 2006).

In terms of stable isotopes, the rivers in the Netherlands can be distinguished in two main categories: the Rhine, and others. The $\delta^{13}\text{C}$ values for bicarbonate and shell carbonate for all freshwater bodies is -10.5‰ . For ^{18}O however, there is a difference between various rivers. The Rhine is dominant and is mainly fed by snow from the Alp mountains in Switzerland. The ^{18}O contents is therefore depleted by the so-called altitude effect, which is basically a temperature effect. About 800 km downstream and including contributions from tributary rivers along the way, in the Netherlands the typical $\delta^{18}\text{O}$ value for Rhinewater is -10.0‰ (SMOW).

The other rivers (Meuse, Scheldt and other smaller streams) are rain-fed by precipitation at low altitudes. Their average $\delta^{18}\text{O}$ value for water is -7.3‰ (SMOW) (Mook 1970). The 1‰ fractionation between water and shell carbonate leads for shells to $\delta^{18}\text{O} = -9.0\text{‰}$ (PDB) for the Rhine, and -6.3‰ (PDB) for the other (precipitation fed) rivers. This forms the basis of what we call “model R” and “model P”, respectively. The values $\delta^{18}\text{O} = -10.0\text{‰}$ and -7.3‰ for water are measured annual averages. They show small seasonal variations with an amplitude of about 0.5‰ (Mook 1970, 2006).

The numbers shown in Table 1 are widely used in hydrological applications. For a more detailed treatise we refer to the literature (Clark and Fritz 1997; Mook 2006; see also IAEA 2024 and references therein). For radiocarbon, the typical value for the recent ^{14}C activity $^{14}\text{a}^{\text{SYS}}$ for river water observed throughout the Netherlands is 85%. A selection of measurements leading to this number is given in Appendix A. This recent activity corresponds to a riverine reservoir effect of about 1300 years.

The shell dating model

This chapter describes in detail a new ^{14}C dating model for shells. It is based on the three isotopes ^{13}C , ^{14}C and ^{18}O of the shell carbonate.

The concentrations of the stable isotopes ^{13}C and ^{18}O are different for shells living in different environments. There are marine shells, riverine shells and shells living in estuaries, consisting of mixed river and sea water. Riverwater can be distinguished in two categories: Rhine water, and water from other rivers. The stable isotope contents in shells also depends on addition effects, such as isotopic exchange between water and the atmosphere, and uptake of carbonate from the soil.

There are other aquatic environments which are habitats for shells: stagnant waters and lakes, and various mixed water bodies. The latter can also show variations through time which obviously complicates the dating procedure.

The isotopic behavior of water and shells is investigated for all the above mentioned environments, including equations for the three natural isotopes involved. This then leads to our dating model for shells, which includes handling reservoir effects.

Following a general introduction, the various environments and isotopic effects therein are discussed below in sections a) through g).

The basic ^{14}C age equations, using the conventional half-life $T_{1/2} = 5568$ years are the following:

$$^{14}\text{a}(t) = ^{14}\text{a}(t = 0) \exp(-\lambda t) \text{ with } \lambda = \ln 2 / T_{1/2} = 0.693 / 5568 \quad [5]$$

$$\text{age}(t) = -8033 \ln [^{14}\text{a}(t) / ^{14}\text{a}(t = 0)] \quad [6]$$

The time $t = 0$ represents the time of death of the organism, the “start of the ^{14}C clock” in dating terms. This corresponds to the “modern” or “recent” activity, i.e. the ^{14}C content of the environment the organism was living in. This in turn also represents (in principle) the activity of the standard, $^{14}\text{a}(t = 0) = ^{14}\text{a}^0$ (Mook and van der Plicht 1999), referring to “year 0,” i.e. 1950, the reference year.

When normalized for isotopic fractionation, the terrestrial recent value ($t = 0$) will remain the same: $^{14}\text{a}_\text{N} = 100\%$. However, the marine value becomes $^{14}\text{a}_\text{N} = 105\%$. The difference of 25‰ in $\delta^{13}\text{C}$ corresponds to 50‰ = 5% in ^{14}a or (approximately) 400 ^{14}C years (for not-too-old samples).

We developed a new method for ^{14}C dating for interpretation of dates from aquatic samples, instigated by our large series of shells from the Netherlands, which is in fact a large delta region (see Figure 1). These shells live in environments consisting of water bodies with various compositions. The marine water is North Sea water, for which the reservoir effect is 400 years during the Holocene. The freshwaters can be rivers, lakes or lagunes leading to complex isotopic mixing situations of water bodies, and thus unknown reservoir effects.

We introduce here the symbol $^{14}\text{a}^{\text{SYS}}$ (SYS for system or reservoir) which is more consistent for our purpose, directly indicating the original natural ^{14}C activity ratio of the system (environment) the organism to be dated lived in. This is not necessarily the same as $^{14}\text{a}^0$ as defined in radiometry, or the number defined in the ^{14}C convention. This way, for a recent terrestrial sample the reference values are then $^{14}\text{a}^{\text{SYS}} = 100\%$ and $\delta^{13}\text{C} = -25\%$. For a recent fully marine sample, these values are $^{14}\text{a}^{\text{SYS}} = 100\%$ and $\delta^{13}\text{C} = 0\%$.

Thus, our model is used for interpretation of ^{14}C dates for aquatic samples without normalization to $\delta^{13}\text{C} = -25\%$, i.e. the terrestrial regime which makes subtracting reservoir effects unnecessary. Instead, we will use tracers to follow isotopic processes: in particular $\delta^{18}\text{O}$ values of the dated shells, basic water properties such as Chlorinity, and specific shell species behavior.

The starting point will be the $^{14}\text{a}^{\text{SYS}}$ value, which would have been the ^{14}a value measured at the time the organism to be dated lived in.

For a sample with measured ^{14}C activity ^{14}a , the ^{14}C age is then calculated as

$$\text{age} = -8033\ln(^{14}\text{a}/^{14}\text{a}^{\text{SYS}}) \quad [7]$$

using the conventional half-life $T_{1/2} = 5568$ years and the oxalic acid reference. The normalization to $\delta^{13}\text{C} = -25\%$ (fractionation correction) is not applied here. Again, this age is therefore formally not expressed in BP.

The formula [7] can also be written as:

$$\text{age} = -8033\ln(^{14}\text{a}/^{14}\text{a}^{\text{SYS}}) = [-8033\ln(^{14}\text{a})] - [-8033\ln(^{14}\text{a}^{\text{SYS}})] = -8033\ln(^{14}\text{a}) - R \quad [8]$$

where $R = -8033\ln(^{14}\text{a}^{\text{SYS}})$, which can be interpreted as a measure of the reservoir effect.

As an illustrative numerical example, the recent activity for freshwater rivers is $^{14}\text{a}^{\text{SYS}} = 85\%$ giving $R = 1305$ years. For the North Sea, $^{14}\text{a}^{\text{SYS}} = 100\%$ giving $R = 0$; this obviously follows from using the not normalized activity. The value for normalized sea water is $^{14}\text{a}_\text{N} = 105\%$, which results in $-8033\ln(^{14}\text{a}_\text{N}) = -392$ years.

These numbers correspond (well within uncertainties) with the general rounded values of 1300 and 400 years used for the freshwater and marine reservoir effects, respectively.

a) Estuary mixing

For estuaries, the stable isotope values of the shell carbonate (numbers shown in Table 1) lead to the following mixing lines. These mixing equations are possible because the concentration of bicarbonate [HCO_3^-] for North Sea and rivers are the same, 2.5 mmol/L.

There are some exceptional cases, but the effect can be neglected within uncertainties.

The mixing relations for the stable isotopes are

$$\delta^{13}\text{C} = 1.64 \delta^{18}\text{O} - 0.14 \text{ for precipitation fed rivers (model P)} \quad [9]$$

based on the endpoints (1.0, 1.5) and (-6.3, -10.5) for ($\delta^{18}\text{O}$, $\delta^{13}\text{C}$); and

$$\delta^{13}\text{C} = 1.20 \delta^{18}\text{O} + 0.30 \text{ for the Rhine river (model R)} \quad [10]$$

based on the endpoints (1.0, 1.5) and (-9.0, -10.5) for ($\delta^{18}\text{O}$, $\delta^{13}\text{C}$).

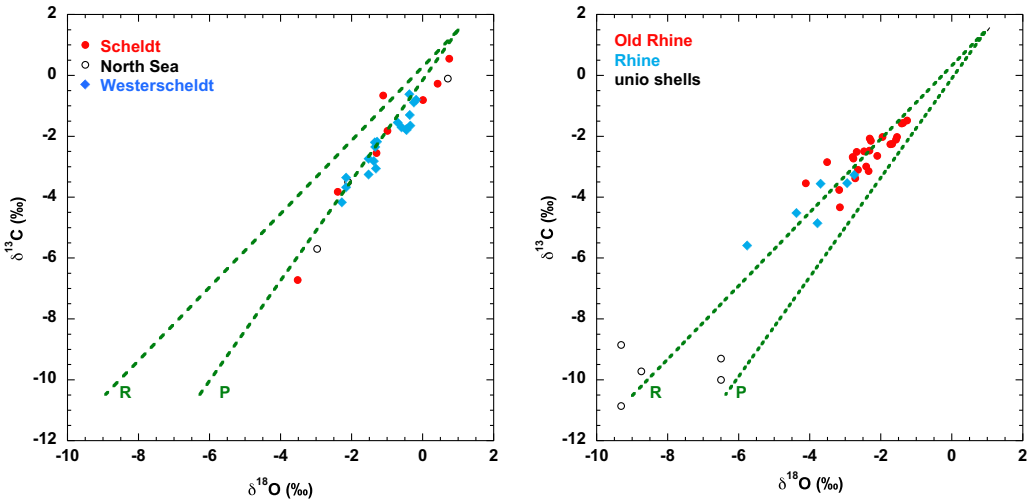


Figure 3. Selected stable isotope data for shells, showing the estuary lines for the models P and R. Figure 3a shows shells from the Westerscheldt estuary, province of Zeeland; Figure 3b shows shells from Zuid Holland. See text for detailed explanation.

The relation between the ^{14}C and ^{13}C is another linear mixing relation, which can be expressed as follows:

$$\frac{(^{14}\text{a}^{\text{SYS}} - ^{14}\text{a}_m)}{(^{14}\text{a}_f - ^{14}\text{a}_m)} = \frac{(^{13}\delta - ^{13}\delta_m)}{(^{13}\delta_f - ^{13}\delta_m)} = \frac{(^{18}\delta - ^{18}\delta_m)}{(^{18}\delta_f - ^{18}\delta_m)} \quad [11]$$

where “m” stands for marine-, and “f” for freshwater. Using the numbers of Table 1, the C isotope mixing formula for shell carbonate is (with ^{14}a in % and $^{13}\delta$ in ‰) as follows:

$$^{14}\text{a}^{\text{SYS}} = 1.25^{13}\delta + 98.125 \quad [12]$$

An analogue formula can be derived for the stable oxygen isotope $^{18}\delta$.

Eq. [12] combined with the stable isotope mixing lines [9] and [10] gives

$$^{14}\text{a}^{\text{SYS}} = 2.05 \delta^{18}\text{O} + 97.95 \quad \text{for model P} \quad [13]$$

$$^{14}\text{a}^{\text{SYS}} = 1.50 \delta^{18}\text{O} + 98.50 \quad \text{for model R} \quad [14]$$

where $^{14}\text{a}^{\text{SYS}}$ represents the recent activity of the estuary, $^{14}\text{a}(\text{est})$.

The final activity $^{14}\text{a}(\text{fin})$ for the shell is

$$^{14}\text{a}(\text{fin}) = ^{14}\text{a}(\text{measured}) / ^{14}\text{a}^{\text{SYS}}(\text{est}) \quad [15]$$

The estuary ^{14}C age can now be calculated as

$$^{14}\text{C} \text{ age} = -8033 \ln \left[^{14}\text{a}(\text{measured}) / ^{14}\text{a}^{\text{SYS}}(\text{est}) \right] \quad [16]$$

with $^{14}\text{a}^{\text{SYS}}(\text{est})$ given by [13] or [14] for model P or R, respectively.

b) Observed data

Much information can be derived from a plot of measured $\delta^{13}\text{C}$ vs. $\delta^{18}\text{O}$ values for a series of shell carbonates. Figure 3 shows the theoretical mixing lines, i.e. the estuary lines for the stable isotopes. The position of the stable isotope values for the measured shell carbonate determines the mixing ratio

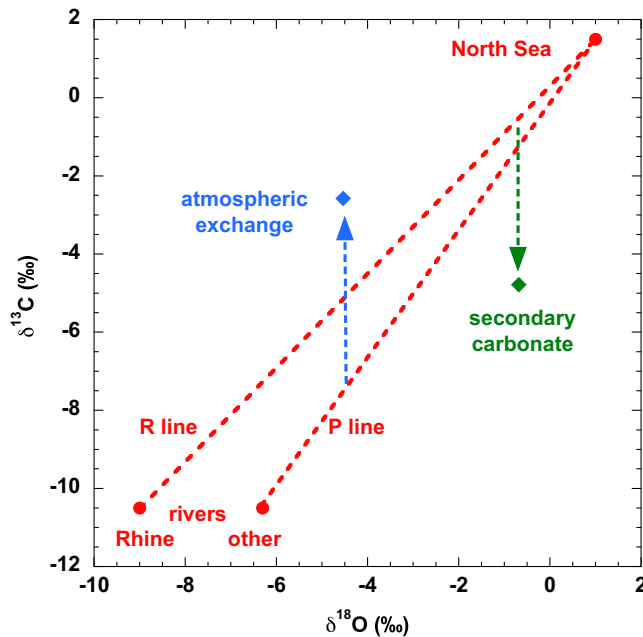


Figure 4. Schematic estuary lines ($\delta^{13}\text{C}$ vs. $\delta^{18}\text{O}$) for shells from marine, river and estuary environments and the effect of atmospheric exchange and secondary carbonate.

between marine- and freshwater reservoirs they were living in, for the two freshwater systems considered: Rhine (R) and other (P).

The division between P- and R-water is clearly visible in Figure 3. Shown is $^{13}\delta$ vs. $^{18}\delta$ values of a selection of shells subject to estuary mixing of sea- and river water. The selection is that only shells which are not subject to special effects such as atmospheric exchange or uptake of secondary carbonate are shown. These effects will be discussed below (see Figure 4).

Figure 3a shows shells from the Westerscheldt estuary, province of Zeeland. It shows measurements of the stable isotopes $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ for historic and recent shells. They are selected from the various databales. The shells shown are all following the P-line. A few data from the North Sea, just outside the Zeeland coastline are included. Figure 3b shows a selection of shells from Zuid Holland. In this province the rivers Rhine (R) and Meuse (P) show complex coarse changes during the Holocene (Berendsen and Stouthamer 2002; de Haas et al. 2018).

At present the main flow of the Rhine into the North Sea is near Rotterdam. However, during pre-and protohistoric times the main river flow into the sea was at present Katwijk (near Leiden). This part of the Rhine system still exists as a relatively small river, today called the “Old Rhine.” This water was part of the so-called Limes, the boundary of the Roman empire along the Rhine (van Dinter 2013). The shells shown are older than ca. 6000 years, and younger than ca. 1500 years. These shells all clearly follow the R-line (Rhine), not the P-line (Meuse).

A few datapoints represent *unionid* shells. This shell is a freshwater taxon, hence they show stable isotope values for riverine water and not estuary water. Indeed, this also shows in Figure 3b; three of the $\delta^{18}\text{O}$ values are those of the Rhine (R), indicating that during the periods shown by the dates there was no influence of the sea, or Meuse river (P). These shells include the dated shells GrA-3640 and GrA-3641 (both Maassluis, Zuid Holland, ca. 7200 years old). The third datapoint shown is for a shell from Wijk bij Duurstede near Utrecht (GrN-6326) with a Roman context.

Two other *unionid* shells are connected with the P-line. One is a recent shell from from the Meuse near Bergen in the province of Limburg (Verdegaal et al. 2005); the other one from Spijkenisse in the Rotterdam region. The shells are not ^{14}C dated but the Spijkenisse shell originates from an

archaeological context dating ca. 4200 years (Versteegh 2009). The stable isotope values represent the river Meuse: $\delta^{18}\text{O} = -6.5\text{‰}$ for both. That means that 4200 years ago, the dominant river near Rotterdam must have been the Meuse (P-water).

Figure 3 demonstrates the existence of two clearly distinguished sea/river mixing lines in the Netherlands we call P and R, determining the estuary isotopic values. These estuary lines form the basis of our dating model, together with additional effects determining the final ^{14}C age of the shell: atmospheric exchange and secondary carbonate.

Figure 4 shows a schematic drawing of the P and R estuary lines, including deviations from the estuary line caused by two different effects: uptake of secondary carbonate from the soil by the shells, and isotopic exchange of CO_2 with the atmosphere. They are indicated by the green and blue lines in Figure 4, respectively. Both effects change the $\delta^{13}\text{C}$ value of the shell, and not the $\delta^{18}\text{O}$ value. This makes the additional measurement of the ^{18}O isotope for shell carbonates crucial, because it determines the position in the $\delta^{13}\text{C}/\delta^{18}\text{O}$ plot and thereby also the proper ^{14}a value, and thus also $^{14}\text{a}^{\text{SYS}}$ and the ^{14}C age. This is discussed further below.

The “estuary age” of the shell is $-8033 \ln(^{14}\text{a}/^{14}\text{a}^{\text{SYS}})$. The recent ^{14}C activity of the estuary $^{14}\text{a}^{\text{SYS}}(\text{est})$ is calculated by formulas [13] or [14] for model P and R, respectively.

Next a correction term is introduced, representing the difference between the measured $\delta^{13}\text{C}$ value with the value of $\delta^{13}\text{C}$ on the estuary line based on its $\delta^{18}\text{O}$ value:

$$\Delta = \delta^{13}\text{C}_{\text{corrected}} - \delta^{13}\text{C}_{\text{measured}} \quad [17]$$

where $\delta^{13}\text{C}_{\text{corrected}}$ is given by the equations [9] and [10] for model P and R, respectively.

The Δ value is used in the correction formulas for atmospheric exchange or secondary carbonate uptake (see Figure 4).

When there is a secondary carbonate effect, the $\delta^{13}\text{C}$ will show below the mixing line because the CO_2 from the soil is depleted in ^{13}C . The $\delta^{13}\text{C}$ values originating from the soil organic matter are typically around -25‰ . The soil sediment is not recent, hence the ^{14}C activity of this organic matter is lower than 100%. Therefore, a correction term needs to be subtracted from the measured age.

When there is exchange with the atmosphere, the $\delta^{13}\text{C}$ shows above the mixing line. The ^{14}C age appears too young, a correction term needs to be added to the measured age. The ^{18}O in the exchange process does not play a role, because in water the amount of oxygen is much larger than the amount of carbon.

Both effects will be quantified in our model. They are distinguished by their Δ value. The atmospheric exchange correction procedure is used in case $\Delta < 0$; the secondary carbonate correction for $\Delta > 0$. This will be discussed below in sections c) and d).

We use the $\delta^{18}\text{O}$ formula for our dating model, because the secondary carbonate effect and the atmospheric exchange effect both change the $\delta^{13}\text{C}$, and not the $\delta^{18}\text{O}$. Only in a few exceptional cases also the $\delta^{18}\text{O}$ is affected; an example is discussed below in section g).

c) $\Delta < 0$: atmospheric exchange correction

The size of the age correction is estimated as 109Δ . This is determined as follows.

For seawater, the shell carbonate in equilibrium has a recent activity $^{14}\text{a}^{\text{SYS}} = 100\%$ and $\delta^{13}\text{C} = 1.5\text{‰}$. For rivers, the values are $^{14}\text{a}^{\text{SYS}} = 85\%$ and $\delta^{13}\text{C} = -10.5\text{‰}$. The age difference between recent seawater and riverwater is measured as 1300 years, corresponding to a difference of 12‰ in $\delta^{13}\text{C}$. Thus, 1‰ in $\delta^{13}\text{C}$ corresponds with 109^{14}C years. Thus, the age can be corrected by adding a term 109Δ years, Δ given by [17].

For the shell age, the atmospheric exchange effect needs to be added to the estuary age given by [16], yielding the final modeled ^{14}C age:

$$^{14}\text{C age} = -8033 \ln [^{14}\text{a}(\text{measured})/^{14}\text{a}^{\text{SYS}}(\text{est})] + 109\Delta \quad [18]$$

d) $\Delta > 0$: secondary carbonate correction

In order to quantify the secondary carbonate uptake effect, we introduce a bicarbonate balance equation for the recent activities for the estuary (est) and secondary carbonate (sec):

$$(2.5 + F\Delta)^{14}\text{a}^{\text{SYS}}(\text{tot}) = 2.5^{14}\text{a}^{\text{SYS}}(\text{est}) + F\Delta^{14}\text{a}^{\text{SYS}}(\text{sec}) \quad [19]$$

which is based on the following.

The bicarbonate concentration in the ocean is 2.5 mmol/L (Mook 1968, 2006). Extra bicarbonate (the secondary carbonate) is added to the estuary water. This is caused by reactions in the soil which produce HCO_3^- . This scales with $\delta^{13}\text{C}$ (in the form of Δ) and an empirical factor F, to be quantified. When $\Delta = 0$, the stable isotopes of the shell are located on the estuary line, then we have simply:

$$^{14}\text{a}^{\text{SYS}} = ^{14}\text{a}^{\text{SYS}}(\text{est}) \quad [20]$$

The factor F has been determined by measurements of carbon properties (chemical and isotopic). For water samples from the Wadden Sea it appears that $F = 0.37$. For brackish waters from the hinterland, the measurements result in $F = 0.88$. The latter will be used for stagnant waters, for which we developed a separate “submodel” S which is discussed below. The measurements and interpretations resulting in the above values for F are shown in Appendix B.

All surface reactions (leading to secondary carbonate) are taking place between 0 and 30 cm in the sediment. The sedimentation rate is known to be ca. 2 mm per year, so that the average age will be about 80 years. This corresponds to 1% in the ^{14}C activity ^{14}a , so that the recent activity of the sediment can be taken as 99%. For the surface sediment (tidal flat and gullies) this results in

$$^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.99^{14}\text{a}^{\text{SYS}}(\text{est}) \quad [21]$$

A special treatment is needed for shell species which do not acquire food by filtering the water, but by grazing organisms (for example *Buccinum*, *Hydrobia/Peringia*, and *Littorinia* species); and also for species applying both filtering and grazing (for example *Macoma* and *Scrobicularia* species). See Appendix C for relevant properties of the shell species.

In gullies during low tide algae and seaweed are living in a “recent ^{14}C ” environment (determined by photosynthesis), for which $^{14}\text{a}^{\text{SYS}} = 100\%$. But the secondary HCO_3^- lowers this value to (about) 99%. The biologically active zone is between 0 and approximately 30 cm. Hence here we have mixing of food obtained by filtering with $^{14}\text{a}^{\text{SYS}} = 0.99^{14}\text{a}(\text{est})$ (R or P) and the surface component $^{14}\text{a}^{\text{SYS}} = 99\%$, both affected by secondary HCO_3^- .

Further, in order to derive the contribution of the secondary carbonate, we introduce a “feeding parameter” γ for the shells. This factor γ ranges between $\gamma = 0$ for tidal flat organic matter (shells feeding from the surface only), and $\gamma = 1$ for suspended organic matter (shells feeding by filtering, estuary only). This results for the shells in the following properties:

$\gamma = 0$ for surface feeding species, $\gamma = 1$ for suspension feeding species and $\gamma = 0.5$ for species using both (assuming equal proportions).

The recent activity of the secondary carbonate contribution can now be written as a combination of the estuary and tidal flat surface:

$$^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.99\gamma^{14}\text{a}^{\text{SYS}}(\text{est}) + (1 - \gamma)^{14}\text{a}^{\text{SYS}}(\text{tidal flat}) \quad [22]$$

which leads to the following, for model P and R respectively:

model P

$$^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.99\gamma(1.50\delta^{18}\text{O} + 98.50) + 99(1 - \gamma) \approx 99 - 2\gamma + 2\gamma\delta^{18}\text{O} \quad [23]$$

$$= \delta^{18}\text{O} + 98(\gamma = 0.5) \text{ or } 2\delta^{18}\text{O} + 97(\gamma = 1) \quad [24]$$

model R

$$^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.99\gamma(2.05\delta^{18}\text{O} + 97.94) + 99(1 - \gamma) \approx 99 - 1.5\gamma + 1.5\gamma\delta^{18}\text{O} \quad [25]$$

$$= 0.75\delta^{18}\text{O} + 98.25(\gamma = 0.5) \text{ or } 1.5\delta^{18}\text{O} + 97.5(\gamma = 1) \quad [26]$$

Some shells are carnivorous, for these $\gamma = 0$. This leads for both models P and R to

$$^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.99 \quad [27]$$

All parts of equation [17] are now determined, which enables calculation of the total secondary carbonate contribution:

$$^{14}\text{a}^{\text{SYS}}(\text{tot}) = [2.5^{14}\text{a}^{\text{SYS}}(\text{est}) + \text{F}\Delta^{14}\text{a}^{\text{SYS}}(\text{sec})]/(2.5 + \text{F}\Delta) \quad [28]$$

Next we can calculate the final activity for the dated sample:

$$^{14}\text{a}^{\text{SYS}}(\text{fin}) = 100[^{14}\text{a}/^{14}\text{a}^{\text{SYS}}(\text{tot})] \quad [29]$$

where ^{14}a is the measured activity. Finally this leads to the modeled age:

$$^{14}\text{C age} = -8033 \ln[^{14}\text{a}(\text{fin})/100] \quad [30]$$

where $^{14}\text{a}^{\text{SYS}}(\text{fin})$ is given in %.

e) Stagnant waters: model S

Shells living in stagnant seawater (only *Cardium glaucum* species can survive in this water) form a special category for the treatise of secondary carbonates.

The $^{18}\delta$ value can not be used as a tracer for stagnant waters. It is influenced by evaporation and precipitation as a function of time. This also means we can not use the same Δ as before, since $^{13}\delta_{\text{corrected}}$ depends on the $^{18}\delta$ value.

For the stagnant water case, we use an alternative Δ here called Δ^* (* to avoid confusion):

$$\Delta^* = ^{13}\delta_{\text{sea}} - ^{13}\delta_{\text{measured}} = 1.5 - ^{13}\delta_{\text{measured}} \quad [31]$$

since the $^{13}\delta$ value for the sea is 1.5‰ (see Table 1).

The situation discussed here is the mixing between seawater and the secondary carbonate. The case discussed above in section c) dealt with mixing of estuary water and the secondary carbonate. Taken together, the formula now translates into

$$\begin{aligned} ^{14}\text{a}^{\text{SYS}}(\text{tot}) &= [2.5 ^{14}\text{a}^{\text{SYS}}(\text{sea}) + 0.88 \Delta^* ^{14}\text{a}^{\text{SYS}}(\text{sec})]/(2.5 + 0.88\Delta^*) \\ &= [250 + 0.88\Delta^* ^{14}\text{a}^{\text{SYS}}(\text{sec})]/(2.5 + 0.88\Delta^*) \end{aligned} \quad [32]$$

with $^{14}\text{a}^{\text{SYS}} = 100\%$ for the North Sea.

The secondary carbonate contribution is quantified as $^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.97 = 97\%$. This value is based on well dated stratigraphies of peat dates, so-called vegetation horizons and marine clay deposits from the province of Groningen. The marine clay contains shells deposited during storm surges which lived in the remaining stagnant pools. The data and a full analysis leading to the number $0.97 = 97\%$ is shown in Appendix D.

For model S, the formulas [29] and [30] derived above can be applied to calculate the final modeled ^{14}C age.

f) Summary of formulas

The essential formulas for the various (sub)models are summarized in the textboxes below. The activities ^{14}a are in %, and the δ values in ‰. Examples of worked calculations are given in the Appendix G.

model P

$$\begin{aligned}
 {}^{13}\delta(\text{corrected}) &= 1.64 {}^{18}\delta(\text{measured}) - 0.14 \\
 {}^{14}\text{a}^{\text{SYS}}(\text{est}) &= 2.05 {}^{18}\delta(\text{measured}) + 97.95 \\
 \Delta &= {}^{13}\delta(\text{corrected}) - {}^{13}\delta(\text{measured}) \\
 \Delta < 0, & \text{ atmospheric exchange correction} \\
 {}^{14}\text{a}(\text{fin}) &= {}^{14}\text{a}(\text{measured}) / {}^{14}\text{a}^{\text{SYS}}(\text{est}) \\
 \text{estuary age} &= -8033 \ln[{}^{14}\text{a}(\text{fin})] \\
 {}^{14}\text{C age} &= \text{estuary age} + 109\Delta \\
 \Delta > 0, & \text{ secondary carbonate correction} \\
 \gamma = 0: & {}^{14}\text{a}^{\text{SYS}}(\text{sec}) = 99 \\
 \gamma = 0.5: & {}^{14}\text{a}^{\text{SYS}}(\text{sec}) = {}^{18}\delta(\text{measured}) + 98 \\
 \gamma = 1: & {}^{14}\text{a}^{\text{SYS}}(\text{sec}) = 2 {}^{18}\delta(\text{measured}) + 97 \\
 {}^{14}\text{a}^{\text{SYS}}(\text{tot}) &= [2.5 {}^{14}\text{a}(\text{est}) + 0.37\Delta {}^{14}\text{a}^{\text{SYS}}(\text{sec})] / (2.5 + 0.37\Delta) \\
 {}^{14}\text{a}(\text{fin}) &= 100 [{}^{14}\text{a}(\text{measured}) / {}^{14}\text{a}^{\text{SYS}}(\text{tot})] \\
 {}^{14}\text{C age} &= -8033 \ln[{}^{14}\text{a}(\text{fin}) / 100]
 \end{aligned}$$

model R

$$\begin{aligned}
 {}^{13}\delta(\text{corrected}) &= 1.20 {}^{18}\delta(\text{measured}) + 0.30 \\
 {}^{14}\text{a}^{\text{SYS}}(\text{est}) &= 1.50 {}^{18}\delta(\text{measured}) + 98.50 \\
 \Delta &= {}^{13}\delta(\text{corrected}) - {}^{13}\delta(\text{measured}) \\
 \Delta < 0, & \text{ atmospheric exchange correction} \\
 {}^{14}\text{a}(\text{fin}) &= {}^{14}\text{a}(\text{measured}) / {}^{14}\text{a}^{\text{SYS}}(\text{est}) \\
 \text{estuary age} &= -8033 \ln[{}^{14}\text{a}(\text{fin})] \\
 {}^{14}\text{C age} &= \text{estuary age} + 109\Delta \\
 \Delta > 0, & \text{ secondary carbonate correction} \\
 \gamma = 0: & {}^{14}\text{a}^{\text{SYS}}(\text{sec}) = 99 \\
 \gamma = 0.5: & {}^{14}\text{a}^{\text{SYS}}(\text{sec}) = 0.75 {}^{18}\delta(\text{measured}) + 98.25 \\
 \gamma = 1: & {}^{14}\text{a}^{\text{SYS}}(\text{sec}) = 1.5 {}^{18}\delta(\text{measured}) + 97.5 \\
 {}^{14}\text{a}^{\text{SYS}}(\text{tot}) &= [2.5 {}^{14}\text{a}(\text{est}) + 0.37\Delta {}^{14}\text{a}^{\text{SYS}}(\text{sec})] / (2.5 + 0.37\Delta) \\
 {}^{14}\text{a}(\text{fin}) &= 100 [{}^{14}\text{a}(\text{measured}) / {}^{14}\text{a}^{\text{SYS}}(\text{tot})] \\
 {}^{14}\text{C age} &= -8033 \ln[{}^{14}\text{a}(\text{fin}) / 100]
 \end{aligned}$$

model S

$$\begin{aligned}
 \Delta^* &= 1.5 \cdot {}^{13}\delta(\text{measured}) \\
 {}^{14}\text{a}(\text{sec}) &= 97 \\
 {}^{14}\text{a}^{\text{SYS}}(\text{tot}) &= [250 + 0.88\Delta^* {}^{14}\text{a}^{\text{SYS}}(\text{sec})] / (2.5 + 0.88\Delta^*) \\
 {}^{14}\text{a}(\text{fin}) &= 100 {}^{14}\text{a}(\text{measured}) / {}^{14}\text{a}(\text{tot}) \\
 {}^{14}\text{C age} &= -8033 \ln[{}^{14}\text{a}(\text{fin})]
 \end{aligned}$$

g) Special mixing situations

The model is expanded in order to deal with complex mixing situations, often changing during (pre/ proto)historical times. Most prominent examples are the northern Rhine branch known as Oer-IJ in North Holland (Vos 2015) and the Rhine/Meuse delta in Zuid Holland (Berendsen & Stouthamer, 2002; Pierik et al. 2018). Detailed geophysical analysis using our model will be published in a more applied local journal.

This leads to (sub)models called “L” (lake) and “Z” (Zuiderzee). The model calculations are shown for “P” and “R” in the main tables together with the administrative information; the final dates (modeled and calibrated) are given for “L” and “Z.” Detailed calculations for “L” and “Z” are given in separate tables. These special submodels only apply to a limited amount of shell dates.

Applying the model: illustrative examples

The applications of our model for the physical geography and archaeology of the Netherlands are many. In this paragraph selected examples of model applications will be discussed. These are illustrative and show the validity of the model. The examples concern estuary shells (a), shells subject to atmospheric CO₂ exchange (b) or secondary carbonate uptake (c), and others (d–f). All dates in this section are rounded to 5.

a) Estuary shells

The oldest Holocene shells within the recent coastline are dated about 7000 ¹⁴C years old. These are *Cardium* shells from the locations Beverwijk (N. Holland), Maasdijk (Z. Holland) and Kerkwerve (Zeeland); see Table 2, which also contains dated associated and contemporaneous terrestrial samples.

The locations represent Early Holocene estuaries from three different locations. Beverwijk is located west of Amsterdam at the present coastline; at the time of the shell, it was part of a large estuary of the Vecht river (see Figure 2). The Beverwijk shell is from a depth of 16.98 m NAP (New Amsterdams Peil, the Dutch Ordnance Datum). It is deposited on top of a peat layer known as base peat, which is dated as 7260 ± 60 BP (GrN-15928). The uncorrected age (i.e. not normalized, not modeled) and conventional age (after subtracting 400 years) appear way too old. Applying our model P yields a date of 7155 years, which is consistent with the peat date: it is younger. The Maasdijk shell originates from a depth of 26.2 m NAP, in a deep marine gully. The location is between Rotterdam and the coast. It should date younger than the base peat deposits in the region; see the cross section in Vos (2015, 242). Peat stratigraphy from nearby Rotterdam has been dated, the relevant date is 7160 ± 45 BP (GrA-32101). See Cohen and Hijma (2008) for a treatise of the Rotterdam (Blijdorp) excavation, and Hijma and Cohen (2011) for a palaeogeographic description of the region.

The uncorrected shell age, 7585 years is too old, as is the normalized age with additional subtraction of 400 years. Applying our model R yields a date of 6880 years, which is consistent with the geography. Kerkwerve is located on the island of Schouwen-Duiveland in the province of Zeeland. The shell represents the old Scheldt river course. Organic samples from the region date 7280 ± 45 BP (Anna Jacoba polder on Tholen, peat, GrN-16936) and 7185 ± 40 BP (Korendijk, charred seeds, GrA-49578). Stratigraphically, the shell should date younger. Also here, the not corrected date is significantly older; the same is true for the normalized age in BP, including subtraction of 400 years. The P-modeled age is 6835 years which does fit the stratigraphy.

The value of 400 years for the reservoir effect in the examples above is obviously not correct, that applies only to a 100% marine shell habitat. We emphasize this here because this value has probably been used in the users community. These examples (as well as the ones following below) illustrate the first successful method to quantify the reservoir effect that fits the stratigraphy, based on geophysical observations and ¹⁴C dates of terrestrial samples.

Table 2. Examples of modeled estuary shell dates compared with contemporaneous samples

Location	Sample	Lab nr.	Uncorrected age	Modeled age	Model	Conventional age (BP)
Beverwijk	Shell	GrN-15433	7695 ± 100	7155	P	
Beverwijk	Peat	GrN-15928			—	7260 ± 60
Maasdijk	Shell	GrA-3186	7585 ± 40	6880	R	
Rotterdam	Peat	GrA-32101			—	7160 ± 45
Kerkwerpe	Shell	GrA-3461	7390 ± 50	6835	P	
Tholen	Peat	GrN-16936			—	7280 ± 45
Korendijk	Seeds	GrA-49578			—	7185 ± 40

b) Leijduin: shells subject to the atmospheric exchange effect

Leijduin is located in the province of North Holland. Measurements for *Cardium* coastal shells from this location yield the isotopic ratio values $\delta^{18}\text{O} = -4.53\text{‰}$ and $\delta^{13}\text{C} = -2.58\text{‰}$, and $^{14}\text{a} = 58.80\%$ (GrN-14203). The uncorrected ^{14}C age is $-8033\ln(^{14}\text{a}) = 4265$ years.

The estuary age is calculated using $^{14}\text{a}^{\text{SYS}}(\text{est}) = 2.05 \delta^{18}\text{O} + 97.94 = 88.65\%$ which results in an estuary age of 3298 years. The shell lived in an environment with no uptake of secondary carbonate from the soil. The stable isotope datapoint is located far above the estuary mixing line. The estuary line $^{13}\delta = 1.64 \delta^{18}\text{O} - 0.14$ for the P model predicts $\delta^{13}\text{C} = -7.57\text{‰}$, revealing a large difference of $\Delta = 4.99\text{‰}$ caused by isotopic exchange with the atmosphere. This results in a shift in age of $109\Delta = 543$ years, yielding a modeled age of $3298 + 543 = 3841$ years.

The $\delta^{13}\text{C}$ value is strongly enriched. Other large enrichments are observed for GrN-7774 and 7775 (Alkmaar), GrN-9042 (Heiloo), GrN-10169 (Nijenburg) and GrN-10170 (Kooibrug).

The Leijduin shell represents the most extreme case in our dataset. The estuary effect is close to 1000 years in one direction, and the exchange effect more than 500 years in the other direction. Observe that for a shell not subject to uptake of secondary carbonate, the equation $^{14}\text{a}^{\text{SYS}} = ^{14}\text{a}(\text{est}) = 1.25^{13}\delta + 98.25 = 94.90\%$, resulting in a ^{14}C age of $-8033\ln(58.80/94.90) = 3845$ years, which is practically the same as the number 3841 above. It also shows a reservoir effect of $4265 - 3845 = 420$ years. All together, this analysis shows the validity of our correction model for ^{14}C dates.

c) Shells subject to secondary carbonate and the sea level

Figure 5 shows ^{14}C dates of shells from the province of Zeeland, plotted as a function of depth. They can be compared with the sea level curve of Meijles et al. (2018), known as the MSL curve. The latter is obtained by ^{14}C dating of peat deposits and is valid for the part of the North Sea discussed here. The peat record does not extend beyond a depth of 12m.

Figure 5 shows uncorrected (measured) and corrected (modeled) ^{14}C dates, using model P for the ^{14}C dates and IntCal20 for calibrated dates. The model makes the shells younger. The black open circles show the uncorrected dates; the filled circles the modeled *Scrobicularia* (scp) shell dates, and diamond symbols for selected *Cardium* (car) shell dates.

For the deepest part (below 14 m) of the shell curve, only a few measurements for car shells (no scp shells) are available. Observe that the sea level curve based on peat (the MSL curve) represents dated plant remains, whereas dates of shells can provide a more direct measurement of the sea level at low tide. The MSL peat curve is shown as a green dashed line (see Figure 10 in Meijles et al. 2018). The sea level curve for shells (based on model P) is shown as a purple dashed line drawn through the datapoints

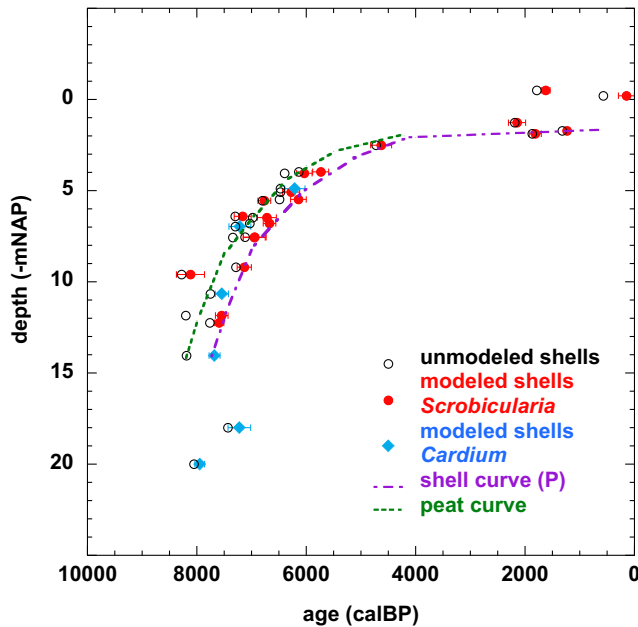


Figure 5. Age/depth plot of shells from Zeeland, shown together with the sea level curve of Meijles *et al.* (2018) which is based on peat dates. The *Scrobicularia* shells follow the sea level curve (see text for details).

and is located below the peat curve. This analysis shows that from our shell database, sea levels can be reconstructed. Our model is shown here to provide a valid explanation for the measured ^{14}C dates.

The shell record contains some shells from much larger depth. Also, the shell dates as a function of depth represent the sea level, albeit of a different nature than the MSL curve. It concerns only shells that live at or near the dry surface, about 0–30 cm depth during low tides. This concerns *Scrobicularia* (*scp*) shells, and often *Cardium edule* (*ced*) shells. The latter can also be found in deep waters, as is also the case for *Macoma* (*mac*) shells. The near surface shells should show below the MSL curve; they can not be located above this curve. The dates of the *scp* shells do fit this criterium, after correction as estuary shells including the secondary carbonate effect.

An interesting observation is the *scp* shell that shows well above MSL curve (GrA-3528). As it happens its ^{14}C date (modeled age 7285 ± 130 ^{14}C years; the calibrated age 8375–7860 calBP) corresponds to the well known Storegga tsunami event in the North Atlantic, including the North Sea (Walker *et al.* 2020 and references therein). The shell is not in situ and must have been redeposited later.

d) Monster: an example of stagnant water

Monster is a small town, located south of Den Haag (The Hague) at the coastline. The natural landscape is a clay deposit on top of peat; the peat layer (called “Hollandveen”) throughout the region has known ^{14}C dates of about 2600–4200 BP from top to bottom. Below this peat an older layer of clay was deposited.

The Monster site is an archaeological excavation, showing Iron Age activity; peat was reclaimed in the past by digging holes. One of these holes contained a wooden artifact. Later, this hole was filled with marine deposits and became brackish, including *Cardium glaucum* (*cgl*) shells that favour such environments. Again later, the pit was covered by phragmites-sedge peat (“rietzeggeveen;” de Jong, ^{14}C sample submission form RGD; van der Valk [1988]).

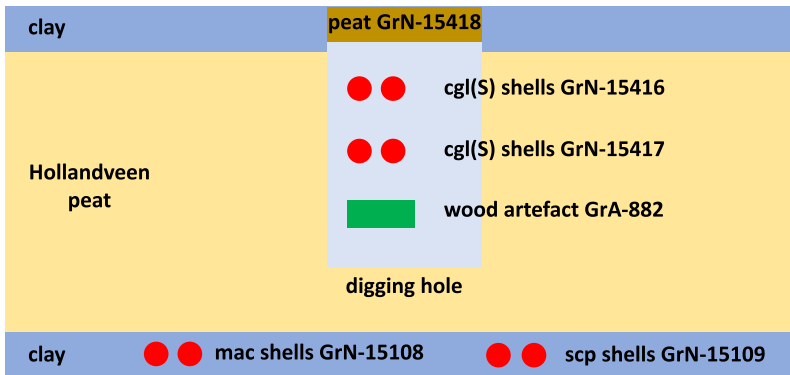


Figure 6. Schematic drawing of an archaeological site at Monster (Zuid Holland), illustrating the validity of our shell dating model for stagnant waters. The peat date GrN-15418 is 2300 ± 20 BP, the wood date GrA-882 is 2360 ± 60 BP. The modeled shell ages are 2310 ± 60 (GrN-15416), 2540 ± 65 (GrN-15417), 4360 ± 50 (GrN-15108) and 4365 ± 60 (GrN-15109).

Hence, the stratigraphy (from top to bottom) is peat (rietzeggeveen), shells, artifact, peat (Hollandveen) and clay. The bottom clay layer also contained marine shells. The artifact, shells and top peat deposit have been ^{14}C dated. For a schematic drawing of site and sample locations see Figure 6.

The phragmites-sedge peat dates to 2300 ± 20 BP (GrN-15418), and the wooden artifact to 2360 ± 60 BP (GrA-882). Both dates correspond to ca. 350 BC. Two *Cardium glaucum* (cgl) shells from the marine sediment were dated; they must be younger than the wood artifact. But both GrN-15416 (uncorrected age 2495 ± 60) and 15417 (uncorrected age 2720 ± 65) date too old when normalized, and a reservoir effect of 400 years subtracted. After correction using model S the ^{14}C age of the shell GrN-15416 is 2310 ± 60 , confirming the expected age; GrN-15417 dates 2540 ± 65 and is still too old. The latter observation can possibly be explained as follows. Clay sediment is partly mixed with peat particles affecting $^{14}\text{a}(\text{sec})$ with $^{14}\text{a}(\text{sec}) = 97\%$, causing an “old peat effect”. Based on the average age of the Hollandpeat and assuming a contaminating amount of 10%, we obtain $^{14}\text{a}(\text{sec}) = 94\%$ and the date becomes 2355 modeled ^{14}C years.

This example shows the validity of our model S for stagnant waters. It is important to note that *Cardium glaucum* shells were often not submitted for dating by the RGD (Geological Survey of the Netherlands), because “they always appear too old” (W.H. Zagwijn, unofficial statement on submission form), either in BP and subsequent marine reservoir correction, or not normalized for fractionation. Our model now provides an explanation for this interesting observation made decades ago.

e) The province of Groningen

A particular observation is that throughout the northern part of the Netherlands, the then existing peat deposit was covered with marine clay during the 9th century BC. The marine deposit is interpreted as the result of several storm surge events during 840–760 BC. The peat deposits are extensively dated by ^{14}C ; throughout the northern Netherlands, the typical ^{14}C date for the toplayer of this base peat is 2600 BP (see also Appendix A). The marine deposit contains shells, many of which are dated by ^{14}C . We applied our model to derive calendar dates, focussing on the province of Groningen from which we have collected and analyzed dozens of samples.

An overview of shells from the province of Groningen is shown in Figure 7a. The stable isotope ratios $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ are shown, with the estuary lines for model P and R (see also Figure 4). Figure 7a shows the stable isotopes of all shells ($\delta^{13}\text{C}$ vs. $\delta^{18}\text{O}$), categorized by species *Cardium edule* (ced), *Cardium glaucum* (cgl), *Macoma* (mac), *Scrobicularia* (scp) and others. The same data are shown in

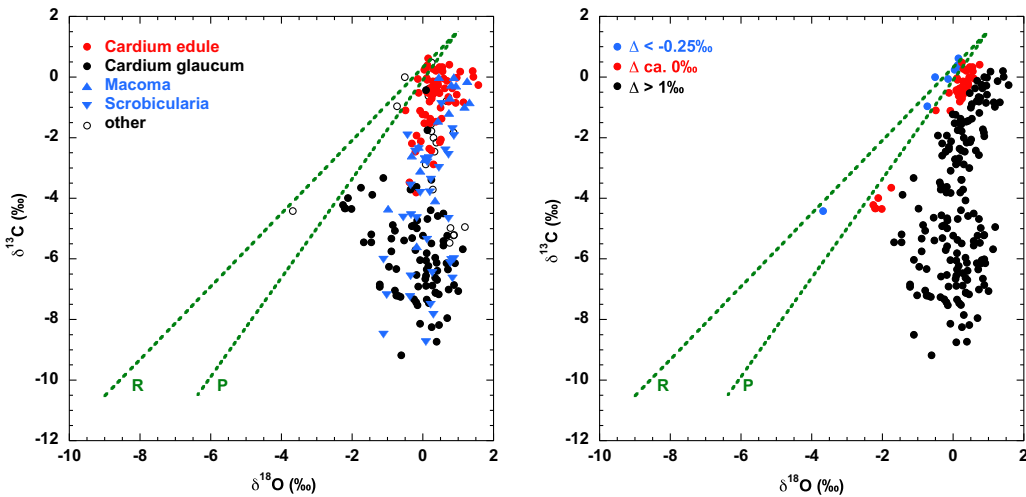


Figure 7. Shell stable isotope data for the province of Groningen. The dashed lines show the estuary mixing lines for precipitation fed rivers (P) and the Rhine (R). a) shells categorized to shell species: *Cardium edule*, *Cardium glaucum*, *Macoma* and *Scrobicularia*; b) shells categorized to their Δ values (see text).

Figure 7b, but now categorized by their Δ value which is the difference between measured and estuary $\delta^{13}\text{C}$ value used in our model. The plots represent shells from all (Holocene, but not recent) ^{14}C ages of the province.

Considering uncertainties involved, we have chosen $\Delta < -0.25\text{‰}$ for shells subjected to the atmospheric exchange effect, $\Delta > 1.0\text{‰}$ for shells subjected to the secondary carbonate effect, and Δ values $\Delta \approx 0\text{‰}$ (between -0.25‰ and $+1.0\text{‰}$) for shells only subjected to estuary mixing.

The dataset for the province of Groningen contains one “outlier,” a freshwater species with $\delta^{13}\text{C} = -4.42\text{‰}$ and $\delta^{18}\text{O} = -3.68\text{‰}$ which is not part of our modeling. It is shown for completeness. All others are marine shells.

As can be seen in Figure 7b, the data with $\Delta > 1$ concern only *Scrobicularia*, *Macoma* and *Cardium glaucum* shell species. The data with $\Delta \approx 0$ are *Cardium* shells, positioned on or close to the precipitation model line. There are only a few datapoints with $\Delta < 1$. It is obvious that the datapoints with $\Delta > 1$ are dominating; the region was characterized by tidal flats and stagnant waters, resulting in (often large) secondary carbonate effects.

The Groningen coastline was, and still is characterized by an extended tidal flat. Today the land is protected by a high seadike. In historical times, land was continuously reclaimed and protected by dikes still visible in the landscape. During prehistory, people lived on “terpen” (mounds). The land was regularly flooded by storm surges, often catastrophic. The flooding events left their traces, as visible in shell middens with especially *Cardium* (car, ced, cgl), *Scrobicularia* (scp) and other species, but not *Cardium glaucum* in stagnant water, cgl(S). *Macoma* (mac) and *Scrobicularia* (scp) are shells living in gullies in the tidal flat, which are rich in organic matter. Hence, they show large secondary carbonate effects, as is clear from Figure 7.

Also, cgl(S) shells are subject to even larger secondary carbonate effects, because seawater is flooding organic rich vegetations. Isotopically, the three species are very similar. However, the mac and scp species require running water conditions; they can not live in stagnant water, whereas for the cgl(S) shells this is the favorite habitat. During storm surges seawater flooded the hinterland and became stagnant. When shell brood of *Cardium* shells (car, ced) is involved, they will develop into cgl(S) in these circumstances. They die when water becomes too fresh or disappears by evaporation, in fact the living period of the shell is an indication for an “event.” Their isotopic behavior is described by our

Table 3. Examples of shell dates (using model S) compared with associated peat dates

Location	Sample	Lab nr.	Uncorrected age	Modeled age	Model	Conventional age (BP)
Winsum	Shell	GrN-17904	2740 ± 40	2565	S	
Winsum	Peat	GrN-14372			—	2690 ± 50
Warffum	Shell	GrN-32864	2755 ± 35	2575	S	
Warffum	Peat	GrN-32960			—	2600 ± 40
Wirdum	Shell	GrN-32818	2820 ± 45	2650	S	
Schildmeer	Peat	GrN-8960			—	2655 ± 30

model S for stagnant waters. See also Appendix C for information on the various shell species discussed in this article.

A storm surge with resulting stagnant water as described above occurs during a relatively short time. Therefore, the cgl(S) shells usually are an indication for an “event.” Note that there are also other types of storm surges, dumping shell middens on the tidal level, even above sea level. These contain various species, but not cgl(S); these are redeposited from the sea bottom.

Following the retreat of the brackish seawater, pastures developed recognized by so-called vegetation horizons. These are characteristic thin dark layers of organic material in Late Holocene clay sediments. Such horizons represent moist meadows (Taayke et al. 2022). These horizons provide an important time marker in the region, for instance the Early Iron Age (ca. 2500 BP). Younger horizons are also observed.

The storm surge period during 840–760 BC coincides with a time characterized by significant climate change, rising groundwater tables and drowning of land, and migration of inhabitants known in the paleobotanical and archaeological record (van Geel et al. 1996, 1998; van Zijverden 2017). It also coincides with a large increase in the $\Delta^{14}\text{C}$ record, part of the millennial scale oscillation in solar cosmic ray production and apparently also in the North Atlantic climate (Bond et al. 2001). The 840 BC event also shows in some shells from the coast of Noord Holland and Zuid Holland; in Zeeland it is not observed—here, no shells for this age are found or measured.

As a summarizing example of model S, Table 3 shows a direct comparison of shell dates and those of associated peat. The peat samples are representative for a large series of peat dated throughout the region.

The shells are deposited on the peat and should therefore be younger. The modeled dates are younger; the not-modeled (uncorrected) dates are all too old. Hence, the model is in accordance with the stratigraphy, and the not-modeled dates are not.

See also Appendix D, which contains more information on the peat deposits leading to the value 97% for the recent value of the secondary carbonate $^{14}\text{a}^{\text{SYS}}(\text{sec})$, which is used for model S.

f) Complex mixing situations in the Zuiderzee region

The shells from Zuiderzee (Lake IJssel, Flevoland; see Figure 1) represent complex mixing situations, depending on time period and location. The same is true for the so-called Oer-IJ region (Vos et al. 2015; Weerts et al. 2002).

Our pre-modern shell dataset for the province of Flevoland (the Lake IJssel region) is limited in size—only 9 shells have been dated. Nevertheless, their isotope values illustrate the model in terms of past geophysical developments. Figure 8 shows the measured isotope ratios $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ for two distinguished groups, according to their age.

For a palaeogeographical description of the IJsselmeer region, we refer to Vos and de Vries (2016), Grondboor & Hamer (2016), van den Biggelaar (2017) and van den Biggelaar et al. (2015). The Rhine river became connected to the Lake IJssel during the first millennium AD. When exactly is not known, Cohen et al. (2009) conclude around 550 AD, and Vos (2015) states ca. 800 AD.

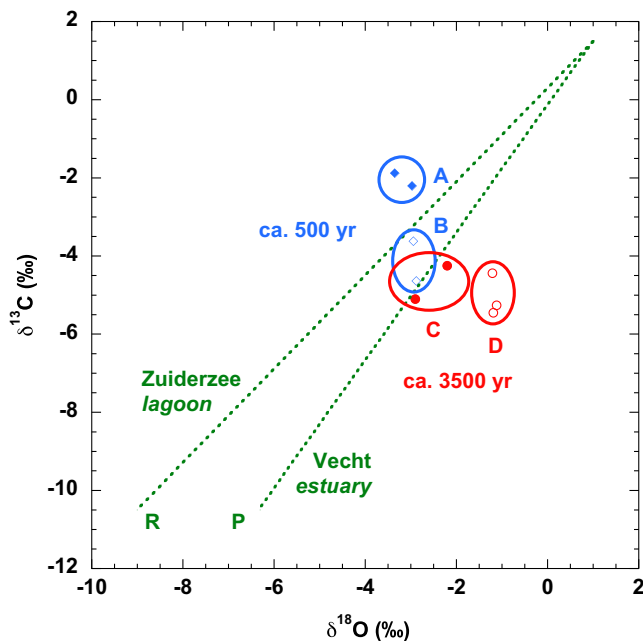


Figure 8. Shell stable isotope data for the IJsselmeer (Lake IJssel) region. The dashed lines are the estuary mixing lines for precipitation fed rivers (P) and the Rhine (R). Two groups can be distinguished: “old” dates (red) and young dates (blue). This can be explained by the breakthrough of Rhine river water (via the IJssel) to the sea during the first millennium AD.

The 5 older dates (ca. 3500 years, thus much older than the Rhine breakthrough) are shown in red. They do not show influence of Rhine water, as it should be for shells of this age. The 5 shells appear to belong to 2 groups; 2 (GrN-11498, 19513; C in Figure 8) are on the precipitation line, and 3 (GrN-7082, 10623, 18358; D in Figure 8) are shifted to more positive $\delta^{18}\text{O}$ values. The location of shells “C” is close to the mouth of the Eem river into the lake, which is probably the reason they are not subject to secondary carbonate. The shells “D” are below the estuary line, caused by the uptake of secondary carbonate.

The Rhine component should be only visible in the younger set of dates. They are shown in blue in Figure 8. They are from two locations (Hindeloopen and Medemblik), with two different shells analysed for each location. The two with the most positive $\delta^{13}\text{C}$ values (A in Figure 8) are *Cardium glaucum* (cgl) shells. They show above the Rhine line, subject to exchange with the atmosphere, and their isotope values are consistent with those of modern shells. The two with the more negative $\delta^{13}\text{C}$ values (B in Figure 8) are *Scrobicularia* (scp) shells. The values are below the Rhine line, so these are clearly subject to the secondary carbonate effect.

For the younger group we developed model Z, with specific calculations for individual shells. The modeled dates are shown in the datatables. Here we show as an example a detailed calculation for two shells from Hindeloopen, a small town located at the Zuiderzee coast of Friesland.

For the Zuiderzee, Eisma, Mook and Das (1976) analyzed the stable isotopes (^{13}C and ^{18}O) for historic shells obtained from museum collections. They were collected before 1932, the year that the Afsluitdijk was completed, which transformed part of the sea into a lake. For these shells no context is known, except for its general location along the coastline. A limited amount was ^{14}C dated later by the conventional method.

Below, we use the subscript “m” for marine water, “f” for freshwater and “s” for shell carbonate. Eisma et al. (1976) determined the Chlorinity for *Cardium* shells; the [Cl] value determines the number

Table 4. The measured data for the isotopes ^{13}C , ^{18}O and ^{14}C and Chlorinity data for two shell species from the Zuiderzee

Lab nr	Location	$^{14}\text{a}_s$ (%)	$^{13}\delta_s$ (‰)	$^{18}\delta_s$ (‰)	$[\text{Cl}]_s$ (‰)	Species	Marine %
GrN-12024	Hindeloopen	90.67	-1.88	-3.35	7.3	cgl	38
GrN-12025	Hindeloopen	88.97	-3.62	-2.94	8.5	scp	

of growth bands R (known as “shell ribs”). The relation between both quantities is given by the equation $[\text{Cl}]_s = 2\text{R}-31‰$ (curve “E” in Figure 1 in Eisma et al. [1976]).

The mixing line ($^{18}\delta_m$ - $^{18}\delta_s$)/ $([\text{Cl}]_m$ - $[\text{Cl}]_s)$ between Zuiderzee and North Sea leads for the measured properties to the relation between the $^{18}\delta$ value and chlorinity of the shells:

$$[\text{Cl}]_s = 2.75^{18}\delta_s + 16.52 \quad [33]$$

The measured isotope values and Chlorinity calculated using [33] for the Hindeloopen shells are shown in Table 4. The marine percentages are calculated by using $[\text{Cl}]_s/19.3$.

The *Cardium* (cgl) shell is subject to the atmospheric exchange effect; the *Scrobicularia* (scp) shell, is subject to secondary uptake of older carbon from the soil.

The mixing equation for marine- (relative amount x) and freshwater (amount $1-x$) is

$$(x)(^{13}\delta_m) + (1-x)(^{13}\delta_f) = ^{13}\delta_s \quad [34]$$

The marine component is $38\% = 0.38$, hence for ^{13}C , $\delta_f = (\delta_s - 1.5x)/(1-x)$ which gives $^{13}\delta_f = -3.95‰$; for ^{18}O , $\delta_f = (\delta_s - x)/(1-x)$ resulting in $^{18}\delta_f = -6.02‰$ for GrN-12024.

We can now derive the initial ^{14}C concentration $^{14}\text{a}^{\text{SYS}}$ for the freshwater component for the shell, using the equation [12]: $^{14}\text{a}_f = 1.25^{13}\delta_f + 98.125 = 93.19\%$. The isotope parameters for the estuary water can be determined from the mixing equations for seawater/freshwater [11] resulting in $^{14}\text{a}(\text{est}) = 0.97^{18}\delta_s + 99.03$ and $^{13}\delta(\text{est}) = 0.78^{18}\delta_s + 0.72$.

For the scp shell, we can determine now also the secondary carbonate contribution $^{14}\text{a}(\text{sec})$, using mixing relations between estuary and tidal flat (wad), for which $^{14}\text{a}^{\text{SYS}} = 100\%$. Further we assume equal contributions from wad and estuary (1:1 mixing).

Next, we need to establish the relationship between $^{14}\text{a}(\text{sec})$ and $^{18}\delta_s$, as follows.

For $^{18}\delta_s = -3‰$, $^{14}\text{a}(\text{est}) = 96.12\%$ yielding $^{14}\text{a}(\text{sec}) = [(96.12+100)/2](0.99) = 97.08\%$;

for $^{18}\delta_s = 1‰$, $^{14}\text{a}(\text{est}) = 100\%$ resulting in $^{14}\text{a}(\text{sec}) = [(100+100)/2](0.99) = 99\%$.

The mixing line between these 2 points ($^{18}\delta_s$, $^{14}\text{a}(\text{sec})$) = (-3, 97.08) and (1, 99) then finally gives for the secondary effect $^{14}\text{a}(\text{sec})$ for this specific shell: $^{14}\text{a}(\text{sec}) = 0.48^{18}\delta_s + 96.60$

Finally, the modeled ^{14}C dates are calculated, using equations [12] and [28] for GrN-12024 and GrN-12025, respectively:

$^{14}\text{a}^{\text{SYS}} = 1.25^{13}\delta_s + 98.125 = 95.775\%$ and ^{14}C age = $-8033 \ln[^{14}\text{a}_s/^{14}\text{a}(\text{sys})] = 440$ years;

$^{14}\text{a}^{\text{SYS}} = [2.5^{14}\text{a}(\text{est}) + 0.37\Delta^{14}\text{a}(\text{sec})]/[2.5 + 0.37\Delta] = 95.90\%$ and ^{14}C age = $-8033 \ln(^{14}\text{a}_s/^{14}\text{a}^{\text{SYS}}) = 603$ years.

Estimation of model uncertainties

a) General remarks

The ^{14}C dates are the result of a physical measurement, for which uncertainties (error bars) are determined. For a Gaussian probability distribution, these are given as sigma σ values in BP $\pm \sigma$, representing 68.3% probability. The calibration curve, the relation between ^{14}C dates and the calendar, is not a linear function. Therefore, the calibrated dates are not Gaussian, and here the probability distribution is given as a 68.3% dating range (corresponding to 1σ in BP) or a 95.4% dating range (corresponding to 2σ).

The uncertainties introduced by handling and interpreting the measured ^{14}C dates for aquatic samples are not straightforward to quantify. This concerns variations in the size of the reservoir effect, and uncertainties in the applied model parameters.

For this reason, the calibrated dates are reported as 95.4% ranges, taking the complete range and ignoring the effect of multiple peaks in the distribution, when present. This is a conservative and pragmatic approach. It is clear that in general the model works—it provides an explanation of ^{14}C dates that appear wrong, when the model is *not* applied. Prime examples are given in the chapter showing applications of the model. This holds for practically all our dates, which represents an unprecedented number of dated shells.

Here we argue that the uncertainties in the values of the main model parameters used do not significantly change the outcome of the calibrated dates. The resulting increase of larger uncertainties for the 95.4% probability range in calendar years is limited in almost all cases. Below follow estimates for the size of the uncertainties, calculated by varying the values of the most significant parameters used in the model.

b) The recent activity of the freshwater reservoir

The main parameter is the recent activity of the riverwater, which is determined to have the value $^{14}\text{a}_{\text{SYS}} = 85\%$. This is based on measurements and other observations, discussed in Appendix A. There we argue that a reasonable assessment for the uncertainty in the $^{14}\text{a}_{\text{SYS}}$ value for river water is about 1%.

The influence of this uncertainty on the modeled age can be best shown by performing calculations using 84% instead of the model value 85% in equation [11]. For a shell with $\delta^{18}\text{O} = -2\%$, the calculated result for the ^{14}C activity using model P is then $^{14}\text{a} = 93.4\%$. For the chosen model parameter value $^{14}\text{a}_{\text{f}} = 85\%$, the calculated activity will be $^{14}\text{a} = 93.8\%$. Thus, the difference between the two calculations is 0.4% in ^{14}a . Hence, a deviation of 1% in the number 85% is equivalent to about 30 ^{14}C years.

This effect of the $^{14}\text{a}_{\text{f}}$ value deviating from 85% depends mainly on the $\delta^{18}\text{O}$ value (or alternatively Chlorinity) of the shell. Calculations show that the effect becomes larger for more negative $\delta^{18}\text{O}$ values. The result of 30 years as calculated above can be considered as a typical value for our dataset.

In a similar way the effect of variations in the input numbers for $^{18}\delta_{\text{f}}$ can be estimated. These are assessed as $-9.0 \pm 0.2\%$ and $-6.3 \pm 0.2\%$ for model R and P, respectively. In this case, the effect for the modeled ages is not larger than 20 ^{14}C years.

Summarizing, the value $85 \pm 1\%$ for the recent activity (and its uncertainty) of the freshwater is shown to be valid for the Rhine/Meuse delta for the part of the Holocene investigated. It is not necessarily a valid number for other regions. See Appendix A for more details.

c) The secondary carbonate

The factor F is used in the formula to calculate the secondary carbonate contribution. It shows two different values for two different environments. These values are determined by a combination of experiments and analysis of data, in particular ^{14}C dates of peat (see Appendix B for details). Including uncertainties these values are assessed as $F = 0.37 \pm 0.10$ for outside the dikes, and $F = 0.88 \pm 0.10$ for inside the dike. The effect on the calculated ^{14}C ages is negligible (<10 years).

d) Illustrative example

The assessment of the uncertainty in the modeled age is best illustrated using an example. The shell GrM-15351 is considered a high precision date, with a standard deviation of the measurement of 15 BP. The modeled age is calculated as 2165 ± 15 ^{14}C years. For this shell, the calibrated probability

distribution of the age is bimodal; the calibration graph shows 2 peaks, around 2280 and 2140 calBP. There is no probability in the middle (the median), around 2200 calBP. Both peaks taken together results in a calibrated age range 2295–2120 calBP (68.3%), or 2300–2100 calBP (95.4%). We use the 95.4% probability, and final dates are rounded to 5.

This high precision date results in a modeled calibrated age range of about 2 centuries. When we increase the measurement uncertainty from 15 to 20, the resulting modeled and calibrated date range will not be significantly different. This example can be considered an extreme case, but it does illustrate the relative insignificance of the uncertainties in the model parameters.

e) Final notes

We note that uncertainties also apply to the “standard model” using a 400 year reservoir effect. The 400 year value is not a holy number either, also here uncertainties can be larger than the standard deviation of a high precision ^{14}C date.

The calibrated numbers are taken together as one range, also when it includes wiggles and/or multiple solutions. In most cases, these are not very relevant for aquatic samples anyway, since these are “damped” compared with terrestrial samples. The latter reflect changes in the atmospheric ^{14}C content (moreless) instantaneously.

Adding all uncertainty contributions σ_i quadratically following the standard statistical formula $\sigma_{\text{tot}} = \sqrt{[1/\sum(1/\sigma_i^2)]}$ yields a final total uncertainty in the modeled age not larger than 2σ , this σ being the reported measurement error. The 95.4% calibrated age probability distribution we therefore consider as a reasonable pragmatic approach for the error in the modeled age. This is supported by the modeled dates which fit the stratigraphy taking into account the uncertainties, whereas not modeled dates mostly do not. Uncertainties remain, but based on our large dataset we can derive parameters that explain the observed modeled dates and their uncertainties with confidence.

Conclusion

A model is presented to assess reservoir effects for shells from the North Sea, rivers and complex mixing waters such as estuaries and lakes during the Holocene in the Netherlands. The model and background information leading to it are described and discussed, and all data (measurements and calculations) are included.

The shells are all dated in Groningen during the last 7 decades. A grand total of 1116 shells are dated and presented in datelists. The whole covers unique aspects: the size of the dataset (many hundreds of shells), representing a large density for a relatively small region which is well studied in terms of palaeogeography and archaeology. For most shell carbonates, the three isotopes ^{14}C , ^{13}C and ^{18}O are measured, thus including ^{18}O which is/was not standard practice, depending on period of measurement and/or laboratory. The two stable isotopes combined are tracers for the past environment the shells lived in, which is crucial information to derive the size of the reservoir effect.

For the Netherlands, the size of the reservoir effect is difficult to assess, as the shells often lived in an environment of mixed marine- and river waters. River water occurs in two main categories, distinguished by ^{18}O : the Rhine which is dominant, and other rivers. This leads to two estuary mixing lines between the North Sea and rivers. The stable isotopes of the shell carbonate are also indicative for additional processes, such as uptake of secondary carbonate from the soil by shells, and exchange of C isotopes between atmosphere and water. Extensions of the main model deal with special cases such as pools of stagnant water and lakes.

The model leads to an assessment of the recent ^{14}C activities of the system the shells lived in, which we call $^{14}\text{a}^{\text{SYS}}$. The measured ^{14}C activities relative to these $^{14}\text{a}^{\text{SYS}}$ values determine the ^{14}C age of the shells and include the reservoir effect. This way we circumvent normalizing to $\delta^{13}\text{C} = -25\text{‰}$, i.e. the terrestrial timescale and the subsequent correction for reservoir effects.

We emphasize that the modeled dates are not in BP, because that would include normalization to $\delta^{13}\text{C} = -25\text{‰}$, the conventional correction for isotope fractionation. Perhaps superfluous, it is noted that the other elements of the convention (the oxalic standard and Libby half-life) are used. Our modeled dates can be calibrated using the present calibration curve IntCal20.

The model is based on the three isotopes ^{13}C , ^{14}C and ^{18}O for shell carbonate. The model uses $^{14}\text{a}^{\text{SYS}} = 0.85$ as the recent value for rivers. The ^{13}C isotope ratio for riverine shell carbonate is $\delta^{13}\text{C} = -10.5\text{‰}$. For ^{18}O , the Rhine shows $\delta^{18}\text{O} = -9.0\text{‰}$, for the other rivers $\delta^{18}\text{O} = -6.3\text{‰}$ applies. For the North Sea, the values are $\delta^{13}\text{C} = 1.5\text{‰}$ and $\delta^{18}\text{O} = 1.0\text{‰}$.

We recommend that the ^{18}O isotope should receive more attention by the user community. The position of the ^{18}O isotope in the $\delta^{13}\text{C}/\delta^{18}\text{O}$ plot determines primarily the ^{14}C value of a mixed reservoir, and thus the proper shell age. The present article concerns the Rhine/Meuse delta in the Netherlands. We recommend other delta regions to be investigated using the same or similar methods, using the proper regional values for the three isotopes.

We also recommend that in dating reports it is completely clear which ^{14}C property is reported: ^{14}a (i.e. not normalized for fractionation) or $^{14}\text{a}_\text{N}$ (i.e. normalized, equivalent to F^{14}C). For ^{14}C dates, it should be clear whether it is calculated from ^{14}a or $^{14}\text{a}_\text{N}$. Formally, only the latter leads to dates in BP. The first includes reservoir effects, the latter requires correction for reservoir effects.

For the Netherlands, the validity of the model is shown by many examples. Only a limited selection of these is discussed here; others will follow in more local publications. The modeled dates are consistent with stratigraphy; not modeled dates are inconsistent with stratigraphy.

Supplementary material. To view supplementary material for this article, please visit <https://doi.org/10.1017/RDC.2024.127>

Supporting online material. The Supporting Online Material contains the data tables (Tables A1–A21) and a description of its contents.

References

- Aerts AT, van der Plicht J and Meijer HAJ (2001) Automatic AMS sample combustion and CO_2 collection. *Radiocarbon* **43**, 293–298.
- Alves EQ, Macario K, Ascough P and Bronk Ramsey C (2018) The worldwide marine Radiocarbon reservoir effect: definitions, mechanisms, and prospects. *Reviews of Geophysics* **56**, 278–305.
- Berendsen H and Stouthamer E (2002) Palaeogeographic evolution and avulsion history development of the Holocene Rhine–Meuse delta, the Netherlands. *Netherlands Journal of Geosciences* **81**, 97–112.
- Bond G, Kromer B, Beer J, Muscheler R, Evans MN, Showers W, Hoffmann S, Lotti-Bond R, Hajdas I and Bonani G (2001) Persistent solar influence on North Atlantic climate during the Holocene. *Science* **294**, 2130–2136.
- Clark P and Fritz P (1997) *Environmental Isotopes in Hydrogeology*. Boca Raton (FL): Lewis Publishers, ISBN 1-56670-249-6.
- Cohen KM and Hijma MP (2008) Het Rijnmondgebied in het vroeg-Holoceen: inzichten uit een diepe put bij Blijdorp (Rotterdam). *Grondboor en Hamer* **3-4**:64–71. In Dutch.
- Cohen KM, Stouthamer E, Hoek WZ, Berendsen HJA and Kempen HFJ (2009) *Zand in Banen*. Arnhem, Provincie Gelderland. In Dutch.
- Cook GT, Bonsall C, Hedges REM, McSweeney K, Boronean V and Pettitt PB (2001) A freshwater diet-derived ^{14}C reservoir effect at the stone age sites in the Iron Gates gorge. *Radiocarbon* **43**, 453–460.
- Craig H (1965) The measurement of oxygen isotope paleotemperatures. In Tongiorgi E (ed), *Stable Isotopes in Oceanographic Studies and Paleotemperatures. Proceedings of the Third Spoleto Conference, Spoleto, Italy*. Pisa: V. Lischi & Figli, 161–182.
- de Bruyne R, van Leeuwen S, Meylin AG and Daan R (2013) *Schelpdieren van het Nederlandse Noordzeegebied*. Utrecht: Tirion. ISBN 9052108218. In Dutch.
- de Haas T, Pierik HJ, vsn der Spek AFJ, Cohen KM, van Maanen B and Kleinhaas MG (2018) Holocene evolution of tidal systems in the Netherlands: Effects of rivers, coastal boundary conditions, eco engineering species, inherited relief and human interference. *Earth Science Reviews* **177**, 139–163.
- Dee MW, Palstra SWL, Aerts-Bijma AT, Bleeker MO, de Bruijn S, Ghebru F, Jansen HG, Kuitens M., Paul D, Richie RR, Spiensma JJ, Scifo A, van Zonneveld D, Verstappen-Dumoulin BMAA, Wietzes-Land P and Meijer HAJ (2020) Radiocarbon dating at Groningen: new and updated chemical pretreatment procedures. *Radiocarbon* **62**, 63–74.
- Eisma D, Mook WG and Das HA (1976) Shell characteristics, isotopic composition and trace element contents of some euryhaline molluscs as indicators of salinity. *Palaeogeography, Palaeoclimatology, Palaeoecology* **19**, 39–62.
- Erlenkeuser H, Metzner H and Willkomm H (1975) University of Kiel Radiocarbon measurements VIII. *Radiocarbon* **17**, 276–300.

- Fernandes R, Rinne C, Nadeau MJ and Grootes P (2016) Towards the use of radiocarbon as a dietary proxy: establishing a first wide-ranging radiocarbon reservoir effects baseline for Germany. *Environmental Archaeology* **21**, 285–294.
- Grondboor & Hamer (2016) *De Marker Wadden*. Nederlandse Geologische Vereniging, jaargang 70, nr. 5/6. In Dutch.
- Heaton TJ, Köhler P, Butzin M, Bard E, Reimer RW, Austin WEN, Grootes PM, Hughen KA, Reimer PJ, Adkins J, Burke A, Cook MS, Olsen J, Skinner LC. 2020. Marine20—the marine radiocarbon age calibration curve (0–55,000 cal BP). *Radiocarbon* **62**, 779–820.
- Heaton TJ, Bard E, Bronk Ramsey C, Butzin M, Hatté C, Hughen KA, Köhler P and Reimer PJ (2023) A response to community questions on the Marine20 radiocarbon age calibration curve: Marine reservoir ages and the calibration of ¹⁴C samples from the oceans. *Radiocarbon* **65**, 247–273.
- Hijma MP and Cohen KM (2011) Holocene transgression of the Rhine river mouth area, the Netherlands/Southern North Sea: Palaeogeography and sequence stratigraphy. *Sedimentology* **58**:1453–1485.
- IAEA (2024) Proceedings of the IAEA International Symposium on Isotope Hydrology series. Available at www.iaea.org.
- Lanting JN and van der Plicht J (1998) Reservoir effects and apparent ¹⁴C ages. *Journal of Irish Archaeology* **9**, 151–165.
- Lee-Thorp JA, Sealy JC and van der Merwe NJ (1989) Stable carbon isotope ratio differences between bone collagen and bone apatite, and their relationship to diet. *Journal of Archaeological Science* **16**, 585–599.
- Meijles EW, Kiden P, Streurman HJ, van der Plicht J, Vos PC and Gehrels WR (2018) Holocene relative sea-level changes in the Wadden Sea area, northern Netherlands. *Journal of Quaternary Science* **33**, 905–923.
- Mook WG (1968) of the Stable Carbon and Oxygen Isotopes of Natural Waters in the Netherlands. PhD thesis, University of Groningen.
- Mook WG (1970) Stable carbon and oxygen isotopes of natural waters in the Netherlands. Symposium on the use of isotopes in hydrology, Vienna. IAEA-SM-129/12.
- Mook WG (1971) Paleotemperatures and chlorinities from stable carbon and oxygen isotopes in shell carbonate. *Palaeogeography, Palaeoclimatology, Palaeoecology* **9**, 245–263.
- Mook WG (2006) *Introduction to Isotope Hydrology*. London: Taylor and Francis. ISBN 0415381975.
- Mook WG and Streurman HJ (1983) Physical and chemical aspects of radiocarbon dating. *PACT Publications* **8**, 31–55.
- Mook WG and van der Plicht J (1999) Reporting ¹⁴C activities and concentrations. *Radiocarbon* **41**, 227–239.
- Olsson IU (1983) Dating non-terrestrial materials. *PACT Publications* **8**, 277–294.
- Pierik HJ, Stouthamer E, Schuring T and Cohen KM (2018) Human caused avulsion in the Rhine-Meuse delta before historic embankment (the Netherlands). *Geology* **46**, 935–938.
- Philippens B (2013) The freshwater reservoir effect in radiocarbon. *Heritage Science* **1**, 24.
- Reimer PJ, Austin WEN, Bard E, Bayliss A, Blackwell P, Bronk Ramsey C, Butzin M, Edwards L, Friedrich M, Grootes PM, Guilderson T, Hajdas I, Heaton T, Hogg AG, Hughen KA, Kromer B, Manning SW, Muscheler R, Palmer J, Pearson C, van der Plicht J, Reimer RW, Richards D, Scott EM, Southon JR, Turney CSM, Wacker L, Adophi F, Büntgen U, Capano M, Fahrni S, Fogtmann-Schulz A, Friedrich R, Köhler P, Kudsk S, Miyake F, Olsen J, Reinig F, Sakamoto M, Sookdeo A and Talamo S (2020) The IntCal20 Northern Hemisphere radiocarbon calibration curve (0–55 kcal BP). *Radiocarbon* **62**, 725–757.
- Rijksdienst voor het Cultureel Erfgoed (2024) Available at: <https://www.cultureelerfgoed.nl/onderwerpen/bronnen-en-kaarten/documenten/publicaties/2019/01/01/paleogeografische-kaarten-pdf>.
- Roeleveld W (1974) The Groningen Coastal Area – A Study in Holocene Geology and Lowland Physical Geography. PhD thesis, VU Amsterdam.
- Stuiver M, Polach HA. 1977. Discussion reporting of ¹⁴C data. *Radiocarbon* **19**:355–363.
- Taayke E, Streurman HJ and van der Plicht J (2022) Vegetation horizons: Human or natural? In Nicolay J and Schepers M (eds), Embracing the salt marsh: foraging, farming and food preparation in the Dutch-German coastal area up to AD 1600. *Jaarverslagen van de Vereniging voor Terpenonderzoek* **102**, 77–90.
- van den Biggelaar DFAM, Kluiving SJ, Bohncke SJP, van Balen RT, Kasse C, Prins MA and Kolen J (2015) Landscape potential for the adaptation of crop cultivation: role of local soil properties and ground table water rise during 6000–5400 BP in Flevoland (central Netherlands). *Quaternary International* **367**, 77–95.
- van den Biggelaar DFAM (2017) New Land, Old History: Past Landscapes and Hominin Activity Covering the Last 220.000 Years in Flevoland, the Netherlands. PhD thesis, VU Amsterdam, ISSN 1571-0750.
- van der Plicht J and Hogg A (2006) A note on radiocarbon. *Quaternary Geochronology* **1**, 237–240.
- van der Plicht J, Kaupová Drtikolová S, Velemínský P, Smolík J, Kučera J, Kameník J, Havránek V, Brůžek J, Vellev J and Rasmussen KL (2020) From the depths of a stagnant pool – on the diet of Tycho Brahe and his wife Kirsten Barbara Jørgensdatter. *Heritage Science* **8**, 73.
- van der Plicht J and Streurman HJ. Forthcoming. Dating, diets and reservoir effects revisited.
- van der Plicht J, Wijma S, Aerts AT, Pertuisot MH and Meijer HAJ (2000) The Groningen AMS facility: status report. *Nuclear Instruments and Methods B* **172**, 58–65.
- van der Valk L (1988) Modderen in Monster: vervening in het Maasmond gebied in de Midden- tot Late IJzertijd. *Westerheem* **37**, 87–92. In Dutch.
- van Dinter M (2013) The Roman Limes in the Netherlands: how a delta landscape determined the location of the military structures. *Netherlands Journal of Geosciences* **92**, 11–32.
- van Geel B, Buurman J and Waterbolk HT (1996) Archaeological and palaeoecological indications of an abrupt climate change in the Netherlands, and evidence for climatological teleconnections around 2650 BP. *Journal of Quaternary Science* **11**, 451–460.

- van Geel B, van der Plicht J, Kilian MR, Klaver ER, Kouwenberg JHM, Reynoud-Farrera I, Waterbolk HT (1998) The sharp rise of $\Delta^{14}\text{C}$ ca. 800 calBC: possible causes, related climatic teleconnections and the impact on human environments. *Radiocarbon* **40**, 535–550.
- van Klinken GJ (1991) Dating and Dietary Reconstruction by Isotopic Analysis of Amino Acids in Fossil Bone Collagen, with Special Reference to the Caribbean. PhD thesis, University of Groningen.
- van Zijverden WK (2017) After the Deluge: A Palaeogeographical Reconstruction of Bronze Age West-Frisia (2000–800 BC). PhD thesis, Leiden University
- Veenstra HJ (1971) De herkomst van de wadafzettingen. *Waddenbulletin* **6**, 1–7. In Dutch.
- Verdegaal S, Troelstra SR, Beets CJ and Vonhof HB (2005) Stable isotope records in unionid shells as a paleoenvironmental tool. *Netherlands Journal of Geosciences* **84**, 403–408.
- Versteegh E (2009) Silent Witnesses: Freshwater Bivalves as Archives for Environmental Variability in the Rhine-Meuse Delta. PhD thesis, VU Amsterdam.
- Vos PC (2015) *Origin of the Dutch coastal landscape*. Barkhuis publishers, Groningen. ISBN 9789491431821.
- Vos PC and Knol E (2015) Holocene landscape reconstruction of the Wadden Sea area between Marsdiep and Weser. *Netherlands Journal of Geosciences* **94**:157–183.
- Vos P, de Koning J and van Eerden R (2015) Landscape history of the Oer-IJ tidal system, Noord Holland (the Netherlands). *Netherlands Journal of Geosciences* **94**:295–332.
- Vos P and de Vries S (2016) Van wad tot Marker Wadden, geologie, archeologie en ontstaansgeschiedenis. *Grondboor en Hamer* **5/6**, 116–123. In Dutch.
- Walker J, Gaffney V, Fitch S, Muru M, Fraser A, Bates M and Bates R (2020) A great wave: The Storegga tsunami and the end of Doggerland? *Antiquity* **94**, 1409–1425.
- Weerts H, Cleveringa P and Gouw M (2002) De Vecht/Angstel, een riviersysteem in het veen. *Grondboor en Hamer* **3/4**, 66–71. In Dutch.
- Westerink B (2022) *Wierdenlandschap*. Noordbroek Publishing, ISBN 978-90-5615-861-3. In Dutch.

Appendices

The appendices show data, text and other background information underlying the model. There are 7 appendices, organized as follows:

- Appendix A. recent activities ($^{14}\text{a}^{\text{SYS}}$) for rivers
- Appendix B. the factor F for secondary carbonate correction
- Appendix C. shell species characteristics
- Appendix D. recent activity ($^{14}\text{a}^{\text{SYS}}$) for secondary carbonate
- Appendix E. marine shells with $\delta^{18}\text{O} > 1\text{‰}$
- Appendix F. note for the users community concerning reservoir confusions
- Appendix G. example calculations

Appendix A) recent activities $^{14}\text{a}^{\text{SYS}}$ for rivers

The value 85% for the ^{14}C activity ratio $^{14}\text{a}^{\text{SYS}}$ for rivers is used as the general value in this article. This value is the result of a variety of observations. This section discusses a few cases of supporting data.

1. Two *Unio* shells (a freshwater species) from a deep gully near Maassluis (GrA-3640, 3641) yield an averaged (not-normalized) ^{14}C age of 8405 years. The shells correspond stratigraphically with the top of peat sediment from nearby Rotterdam, dating 7160 ± 45 BP (GrA-32101). The difference between these two age measurement values is 1245 years which corresponds to about 85% in ^{14}C activity.
2. A series of 7 recent shells from the Westerscheldt estuary was collected in 1967 for measurement of the stable isotopes ^{13}C and ^{18}O . Later they were dated by ^{14}C (GrN 33301-33307). The locations range between the coast (Westkapelle) and inland (Kruiningen). The latter location is towards the border of Belgium (mouth of the Scheldt river). The resulting mixing line along the sample localities gives a recent value for the Scheldt river $^{14}\text{a} = 107.5\%$. The North Sea datapoint from this series shows a value of 127%. Hence the ratio Scheldt/North Sea is $107.5/127 = 0.85 = 85\%$.

3. In a separate manuscript (van der Plicht and Streurman, [forthcoming](#)) we will revisit reservoir effects by a thorough analysis of isotopic fractionation in environmental systems and caused by diet. A model is developed based on both ^{13}C and ^{15}N isotopes of bone collagen of consumers of aquatic food (in particular fish and meat from shells). Most data applied in this model are obtained from known age samples, including modern samples (influenced by the bomb peak).

This diet model can be “reversed”: from the isotopic measurements and other data the “recent value” $^{14}\text{a}^{\text{SYS}}$ for the bicarbonate system in freshwater systems can be determined.

For freshwater conditions, meat for fish (and mussels) shows for the fractionation factor between meat and HCO_3^- in water values of $^{13}\varepsilon = -22\text{‰}$. The bone collagen of consumers is enriched by 5‰ , thus has $^{13}\varepsilon$ values of -17‰ (Lanting and van der Plicht 1998; Lee-Thorp et al. 1989). Vice versa, when bone collagen of consumers is depleted by 17‰ , their values can be used to determine the $^{14}\text{a}^{\text{SYS}}$ for the water system which must be enriched by 17‰ .

The ε is the general symbol for the fractionation factor; the fractionation factor δ is expressed with respect to a reference (Mook 2006).

The $^{13}\delta$ value for the bicarbonate of the water can be determined by adding the fractionation factor value $^{13}\varepsilon$ to the value of the $^{13}\delta$ of the collagen of the consumer:

$$^{13}\delta(\text{water}) = ^{13}\delta(\text{consumer}) + ^{13}\varepsilon$$

The ^{14}a value of the bicarbonate in water can now be calculated using the fractionation correction factor:

$$^{14}\text{a}_{\text{water}} = ^{14}\text{a}_{\text{consumer collagen}} [1 + 2^{13}\varepsilon]$$

The average value for recent water, calculated from a series of more than 20 measurements, derived from the carbonate data:

$$^{14}\text{a}^{\text{SYS}} = 84.5\%$$

Within uncertainties, this confirms the typical value $^{14}\text{a}^{\text{SYS}} = 85\%$ for DIC (dissolved inorganic carbon) in freshwater in the Netherlands.

4. Three samples of *Unio* shells (a freshwater species) from the Rhine near Utrecht show an average not-normalized ^{14}a value of 66.3% (GrN-6326, 17543, 17544). The shells have a Roman association. Assuming a recent activity of $^{14}\text{a}^{\text{SYS}} = 85\%$, the average shell activity would correspond to an age of $-8033 \ln(66.3/85) = 1995$ years which indeed is Roman.

Deviations of the value 85% do exist; these can be temporary or regional. Temporary events are for example heavy rains, leading to values larger than 85% because precipitation is recent. In contrast, severe drought events may cause values lower than 85% when groundwater influence increases. The events mentioned are short term, and do not significantly influence the dates of shells which signal a few years average.

In regions other than the Rhine/Meuse delta in the Netherlands, $^{14}\text{a}^{\text{SYS}}$ values can be significantly different from 85%. To mention one example, in Southeastern Germany mussels show large reservoir effects, corresponding to $^{14}\text{a}^{\text{SYS}}$ values of around 80% (Fernandes et al. 2016).

All together, we conclude that the recent value for the activity of riverwater for the Netherlands is $^{14}\text{a}^{\text{SYS}} = 85 \pm 1\%$. Deviations larger than 1% would result in dates which no longer fit the stratigraphy, which is never observed.

Appendix B) the factor F for secondary carbonate correction

The factor F is used in our model to calculate the contribution of secondary carbonate in the measured ^{14}C dates of shell carbonates.

The secondary carbonate is caused by reactions in the sediment soil which produce HCO_3 . Examples are oxidation ($\text{O}_2 + \text{organic matter}$), denitrification ($\text{NO}_3 + \text{organic matter}$) and reduction ($\text{Fe}(\text{OH})_3 + \text{organic matter}$, and reduction of $\text{SO}_4 + \text{organic matter}$).

The $^{13}\delta$ value for organic matter is typically -25% ; the fractionation leading to CO_2 and further to HCO_3 is $\epsilon \approx 8\%$ (Mook, 2006), leading to a typical value for $^{13}\delta_{\text{sec}} = -17\%$. For seawater/clean estuary water $^{13}\delta_{\text{est}} = 0\%$.

For estuaries, the following balance equation for carbon applies (Mook 2006):

$$(\Sigma\text{C}_{\text{est}})(^{13}\delta_{\text{est}}) + (\Sigma\text{C}_{\text{sec}})(^{13}\delta_{\text{sec}}) = (\Sigma\text{C}_{\text{tot}})(^{13}\delta_{\text{tot}})$$

where $\Sigma\text{C}_{\text{tot}} = \Sigma\text{C}_{\text{est}} + \Sigma\text{C}_{\text{sec}}$, the total amount of carbon, $\Sigma\text{C}_{\text{est}}$ is the clean water component, and $\Sigma\text{C}_{\text{sec}}$ the extra contribution (the secondary carbonate).

From series of measurements, the typical value for the extra contribution of bicarbonate ($^{13}\delta = -17\%$) appears about 3.9 mmol/L which means for the carbon balance equation:

$$(2.5)(0) + (3.9)(-17) = (6.4)(^{13}\delta_{\text{tot}})$$

which leads to $^{13}\delta_{\text{tot}} = -10.36\%$ and subsequently $F = 3.9/10.52 = 0.37$.

For stagnant water, we performed experiments mixing sea sediment with clean seawater. This resulted in an average value of 8.5 mmol/L HCO_3 with $^{13}\delta_{\text{sec}} = -6.8\%$, so that (using the seawater value 2.5%) $\Delta(\text{HCO}_3) = 8.5 - 2.5 = 6\%$ which leads to $F = 6/6.8 = 0.88$.

Appendix C) shell species characteristics

List of shell species

A list of shell species including some properties relevant for our model is summarized in this section. Three are freshwater species, the others are all marine shells. The shell species represented in the datelists are shown in Table 5. The table shows their scientific names, Dutch names and abbreviations used in the manuscript. This “code” is an abbreviated name used in the datelists and text.

Table 6 shows the shells discussed in this article with their habitat and other relevant conditions. The information shown is taken from de Bruyne (2013).

Except for “unio,” “dre” and “valv,” these are all marine shells. Unio is a general name used for freshwater shells (Versteegh, 2009). *Valvata* is a freshwater shell, but this species can also live in brackish water. See de Bruyne et al. (2013) for a detailed description of these and other shells.

Shell species which are commonly found in brackish environments are car(cgl), mac and scp. These are all possibly subject to the secondary carbonate effect. The shells car(ced), spi and others are not, they are normally found on top of the sand bottom (the so-called supratidal zone); their stable isotope values are around the mixing line, as they are determined by running water. These are all very general observations; naturally, there can also be mac shells not subject to the secondary carbonate effect, for example.

The arc (*Arca lactea*) shell has a southern origin, it does not belong to the Dutch fauna. There happens to be only one measurement for this shell species (from the North Sea). It lives in the Channel and is probably redeposited in the southern North Sea.

According to Veenstra (1971), the shells can be divided in two groups. “Suspension feeders” sieve material from the water; these are car, myt and mya. “Deposit feeders” obtain their food from the soil. The mac and scp shells belong to the same group. Based on their biology and environmental conditions (de Bruyne et al. 2013), our isotopic dataset enables to make some general distinctions between species as summarized below.

Table 5. Overview of shell species used in this manuscript

Code	Scientific name	Dutch name	Remarks
arc	<i>Arca lactea</i>	Arkschelp	
bar	<i>Barnea candida</i>	Boormossel	
buc	<i>Buccinum undatum</i>	Wulk	
car	<i>Cardium</i>		General type
ced	<i>Cardium edule</i>	Gewone kokkel	
cgl	<i>Cardium glaucum</i>	Brakwaterkokkel	
dre	<i>Dreissena polymorpha</i>	Driehoeksmossel	Freshwater shell
hyd	<i>Hydrobia ulvae</i>	Wadslakje, same as “per”	Synonym
lit	<i>Littorinia littorea</i>	Alikruik	
mac	<i>Macoma balthica</i>	Nonnetje	
mtc	<i>Mactra corallina</i>	Grote strandschelp	
mya	<i>Mya arenaria</i>	Strandgaper	
mys	<i>Mysella bidentata</i>	Tweetandschelpje	
myt	<i>Mytilus edulis</i>	Mossel	
ost	<i>Ostrea edulis</i>	Oester	
per	<i>Peringia ulvae</i>	Wadslakje, same as “hyd”	Synonym
pet	<i>Petricolavia pholadiformis</i>	Amerikaanse boormossel	
sep	<i>Scrobicularia plana</i>	Platte slijkgaper	
ses	<i>Sessilia</i>	Zeepokken	
spi	<i>Spisula subtruncata</i>	Halfgeknotte strandschelp	
unio	<i>Unio pictorum</i>	Schildersmossel	Freshwater shell
valv	<i>Valvata piscinaris</i>	Vijverpluimdrager	Freshwater shell

Table 6. Living conditions for various shell species discussed in this manuscript*

Type	Near surface	Deep water (max,m)	Food	Soil	Depth below surface (cm)	Cl (%)	Estuary	Shell age (year)	Δ (%)
myt	x	x	f		0	10–22	x	18–24	0/1
ced	x	x	f	s	5	14–20	x	3–4	0/1
mac	x	35	f,g	c,s	6	2–17	x	6–7	++
mct	x	50	f	s	10				0
sep	x		f,g	c	2–30	6–17	x	4–5	++
mya	x	70	f	c,s	50	3–19	x	5–40	+
spi	x	40	f	s	4	7–19	x		0
per	x	20	g	c,s	0	3–18		2–5	+
buc	x	very deep	g		0	8–15		<30	0
cgl	x	>10	f	c,s	5	3–14	x	4–5	-0/+
lit	x	<5	g	c,s					0
mys			f						0
pet	x	15	f	c					0

*Food: f, filtering; g, grazing. Soil: c, clayey; s, sand.

Cardium (car) is the general name for this shell species. They can be distinguished in *Cardium edule* (ced) and *Cardium glaucum* (cgl). The ced shells are living in coastal regions including the Wadden sea. They are intertidal, living about 5 cm in the bottom. They mainly feed on living diatoms and algae from

the water. They can live in full marine conditions (maximum chlorinity 19.3 ‰). The cgl are estuary shells. Stagnant waters can also be the habitat for cgl shells. Two types of behavior can be distinguished corresponding to (a) running brackish water, and (b) stagnant brackish water:

- (a) Living about 5 cm in the bottom, in brackish water with chlorinity between 3 and 14‰. They can be found in water in the tidal zone (thus not in dry conditions during ebb). They are feeding on algae and detritus. The $\delta^{18}\text{O}$ value of the shell is linear related with chlorinity.
- (b) In this case the $\delta^{18}\text{O}$ value of this shell is not related to the chlorinity but depends on temperature. These shells are associated with storm surges, deposited in the hinterland. Because of evaporation of the water, the $\delta^{18}\text{O}$ value changes; as a consequence, also the chlorinity changes.

Macoma baltica (mac) lives about 6 cm deep in the bottom, in water with chlorinity between 2 and 17‰. They are feeding on detritus. They can also live in poor oxygen conditions, in which case SO_4 reduction is possible causing negative $\delta^{13}\text{C}$ values.

Scrobicularia plana (scp) lives in soils enriched in organic matter (clay), often with some freshwater influence. It is an intertidal species, found at depths up to ca. 30 cm. It can sustain chlorinities between 6 and 17‰.

Mytilus edulis (myt) lives in undeep water, with chlorinity between 10 and 22‰. The shell commonly filters food from the water (living, no detritus). Only in stress conditions it will consume detritus. This influences the stable isotope values.

The Wadden Sea is intertidal, undergoing ebb and flow causing changing water and dry land conditions. The wad (tidal flat) is characteristic for the shell species ced, myt and spi. In addition, mac and scp in gullies are subject to secondary carbonate effects. Also, lagoons are subject to ebb and flow, but here the bottom does not become dry land. There is isotopic exchange with the atmosphere, especially for $\delta^{13}\text{C}$. The shell species ced, myt, spi can be found in lagoons.

Summarized here are the γ parameter values used in the model for the different shell species. For mac and scp, $\gamma = 0.5$; for buc, lit and per/hyd, $\gamma = 0$; for all other species, unknown species and mixed shell samples we take $\gamma = 1$. Occasionally, mac shells can live in deep waters; in that case, $\gamma = 1$.

Appendix D) recent activity for secondary carbonate

The recent activity of the secondary carbonate, $^{14}\text{a}^{\text{SYS}}(\text{sec})$ can be derived from (pre)historical information. This is enabled by a large amount of ^{14}C dates obtained during the last decades from the province of Groningen, for both shells and organic deposits. The region was flooded repeatedly in prehistorical times, as well in historical times when there were dike breaches. Storm surges dumped large amounts of shells inland. After the event, the water remaining in pools became stagnant, an environment particularly suitable for *Cardium glaucum* (cgl) shells.

The organic deposits concern peat and so-called vegetation horizons (Roeleveld 1974; Taayke et al. 2022; Vos and Knol 2015). For the paleolandscape development of the northern Netherlands we refer to Vos (2015), Vos and Knol (2015), Westerink (2022) and references therein.

The Holocene stratigraphy of the province of Groningen consists of sequences of peat layers and marine clay deposits, containing shells. These were deposited during storm surges. The top layers of two such peat layers deposited throughout the province are well dated to 2600 and 1750 BP. The marine clay is in turn covered by vegetation horizons, dating ca. 2500 and 1600 BP, respectively. Hence for both cases the modeled shell dates must bracket between the peat and vegetation horizons. We mention here that the “2600 event” corresponds to ca. 800 BC, the start of the so-called Hallstatt-plateau in the calibration curve caused by a large increase in the natural $\Delta^{14}\text{C}$ signal, and indicative for a period of wet conditions, and climatic and cultural changes (e.g. van Geel et al. 1998).

The shells concern *Cardium glaucum* species, which are typical for stagnant waters following storm surges. These shells, here coded cgl(S), thrive on organic food available from the sediment in these environments. This information can be used to derive the value for $^{14}\text{a}^{\text{SYS}}(\text{sec})$, as follows.

For the 2600 event, the database contains 20 peat dates associated with the “2600 event”. The averaged value for the ^{14}C dates is 2605 ± 65 BP. We also have a series of 7 shell dates (GrN-17904, 31518, 31934, 32540, 32818, 32858 and 32864, see Table A5). We illustrate the calculation of $^{14}\text{a}^{\text{SYS}}(\text{sec})$ using a worked example calculation: the cgl(S) shell GrN-31934 from the location Baflo, a few km north of the city of Groningen.

The not-normalized age is 2820 ± 50 years, the $\delta^{13}\text{C}$ value is -7.53‰ . The age difference with 2600 is 220 years, which corresponds to an activity difference of $\exp(-220/8033) = 0.9730 = 97.30\%$. The equation [28]: $(2.5 \ ^{14}\text{a}^{\text{SYS}}(\text{sea}) + F \ \Delta^* \ ^{14}\text{a}^{\text{SYS}}(\text{sec})) / (2.5 + F \ \Delta^*)$ then results in $= (250 + 0.88 \ 9.03 \ ^{14}\text{a}^{\text{SYS}}(\text{sec})) / (2.5 + 0.88 \ 9.03) = 97.30$, using $^{14}\text{a}^{\text{SYS}} = 100\%$ for the sea, $F=0.88$ for stagnant water and $\Delta^* = 1.5 - (-7.53) = 9.03\text{‰}$. From this it follows that $^{14}\text{a}^{\text{SYS}}(\text{sec}) = 96.45\%$.

For all 20 dates, the averaged value for the recent value of the secondary carbonate is $^{14}\text{a}^{\text{SYS}}(\text{sec}) = 96.9 \pm 1.4\%$.

For the 1750 event, the database contains also 20 ^{14}C dates for vegetation horizon layers. Their averaged ^{14}C age is 1750 ± 70 BP.

For this event, the database contains 28 shell dates (see Table A5): GrA-57592 and 65099, GrN-17998, 25158, 26392, 26653, 27944, 28867, 28868, 32145, 31519, 31596, 32014, 32072, 32131, 32155, 32156, 32191, 32501, 32539, 32603, 32838, 32850, 32867, 32868, 32916, 32918 and 33300. The averaged value for the recent value of the secondary carbonate is $^{14}\text{a}^{\text{SYS}}(\text{sec}) = 96.7 \pm 1.0\%$.

Summarizing, we have shown that for stagnant water applications our model can use for the recent value of the secondary carbonate $^{14}\text{a}^{\text{SYS}}(\text{sec}) = 97 \pm 1\%$.

Appendix E) marine shells with $\delta^{18}\text{O} > 1\text{‰}$

Some of coastal shells show values for $\delta^{18}\text{O}$ larger than 1‰ , often leading to $^{14}\text{a}^{\text{SYS}} > 100\%$ which is not realistic. These are identified in the datatables and analyzed by model “T.” This is caused by temperature dependence of the $\delta^{18}\text{O}$ value, thus also on the location in the sea. In this case the exchange effect is not possible; only secondary reactions may occur.

For example, the origin of the Walcheren (Zeeland) shells is a bulk shell deposit from the sea, outside the coastline. These are all *Spisula* (spi) species, showing values $^{14}\text{a}^{\text{SYS}} > 100\%$ and $\delta^{18}\text{O} > 1\text{‰}$, i.e. they all show 100% marine isotope (no freshwater) signals. In these cases, they must have been relocated, most likely by a storm surge. Their $\delta^{18}\text{O}$ values indicate that they must originate from a region with significantly lower temperatures. This temperature dependence is known, allowing correction for this effect. The temperature dependence is given as

$$T(^{\circ}\text{C}) = 16.5 - 4.3^{18}\delta + 0.14(^{18}\delta)^2 \quad [33]$$

which is the well known paleotemperature scale for marine shells as developed in the 1960s (e.g. Craig 1965). The temperature dependence also correlates with $\delta^{13}\text{C}$. Taken together, the relationship between $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ is given by

$$^{13}\delta(\text{expected}) = -0.37^{18}\delta(\text{measured}) + 1.87 \quad [34]$$

which is known as the “calcite line.” See Mook (1968) and Mook (2006; Figure 5.14) for a treatise of the carbon/water geochemistry.

Here we define the Δ value as the difference between measured and expected $\delta^{13}\text{C}$:

$$\Delta^{**} = \text{abs}[^{13}\delta(\text{measured}) - ^{13}\delta(\text{expected})] \quad [35]$$

This leads to the $^{14}\text{a}^{\text{SYS}}$ value calculation using the earlier derived procedure, as follows.

There is no influence from rivers (like for our models “P” and “R”). Therefore, the recent ^{14}C activity for the ocean system is $^{14}\text{a}^{\text{SYS}}(\text{‘est’}) = 100\%$. The Δ term only represents the secondary carbonate HCO_3^- . Hence equation [28] now leads to

$$^{14}\text{a}^{\text{SYS}} = [2.5^{14}\text{a}(\text{est}) + 0.37\Delta^{**14}\text{a}(\text{sec})]/[2.5 + 0.37\Delta^{**}] \quad [36]$$

This is illustrated by a worked example, for GrA-1577:

$$^{14}\text{a}(\text{measured}) = 76.81\%, \text{ uncorrected age} = 2119 \text{ years}, \delta^{13}\text{C} = 0.12\text{‰}, \delta^{18}\text{O} = 1.67\text{‰}$$

$$\delta^{13}\text{C}(\text{expected}) = (-0.37) \delta^{18}\text{O} + 1.87 = 1.25\text{‰}, \Delta^{**} = 1.13\text{‰}$$

$$^{14}\text{a}^{\text{SYS}} = [2.5 \cdot 100 + 0.37 \cdot \Delta^{**} \cdot 99]/[2.5 + 0.37 \cdot \Delta^{**}] = 99.86\%$$

$$^{14}\text{a}(\text{fin}) = (76.81/99.86) \cdot 100\% = 76.92\%$$

$$\text{modeled age} = -8033 \ln[^{14}\text{a}(\text{fin})/100] = 2107 \text{ years.}$$

This approach yields realistic “recent activity” values for $^{14}\text{a}^{\text{SYS}}$. There are a few exceptions with $\Delta > 0$, which is not possible for a 100% marine environment: GrA-1773, 1777, 1778 and 3664. Also for GrA-1777, 1778 and 3664 the derived temperature becomes unrealistically low. These shells apparently originate from colder, more northern regions of the North Sea. When we analyze them using the relation

$$^{13}\delta(\text{expected}) = -0.37^{18}\delta(\text{measured}) + 2.87 \quad [37]$$

we do obtain realistic results. This equation is valid for aragonite (Mook, 2006). It differs 1‰ in $^{13}\delta$ from the calcite equation. For these 3 shells the aragonite results are shown in the table.

Also observe that the temperature for GrA-1778 using $^{18}\delta = +5.56\text{‰}$ results in a temperature which is clearly an impossible value. We suspect (but can not prove from our records) that this measurement is not recorded correctly. Assuming it must be $^{18}\delta = +2.56\text{‰}$ we do obtain realistic results. The C isotope measurements (and thus the measured ^{14}C age) are valid.

In the main datatables, the accepted dates are shown in Table A13. This submodel is named model “T.” In Table A13, the 4 shells analyzed using aragonite are GrA-1773, 1777, 1778 and 3664. They can be identified by their values for $^{13}\delta(\text{expected})$. In case of stagnant waters model S is used; model T does not apply.

Appendix F) note for users: on reservoir confusions and recommendation

For “standard” marine samples the following general numbers apply: the reservoir effect is 400 years; shells have $\delta^{13}\text{C} = 0\text{‰}$. These numbers lead to the following.

- The reference value for normalization (the fractionation correction) is $\delta^{13}\text{C} = -25\text{‰}$, which corresponds to 50‰ in $\delta^{14}\text{C}$ (Mook 2006) or 5% in ^{14}a . This in turn corresponds to 400 years (for not too old samples).
- This happens to be the same value as the reservoir effect, by coincidence.

Therefore, both effects cancel: normalized dates in BP (a 400-year effect) require subtraction of the reservoir effect (also 400 years), hence not normalized dates automatically include the reservoir effect. This is well known but nevertheless has led and still leads to confusion in the users community.

When marine ^{14}C dates are not corrected (normalized) for fractionation, they do not require correction for the reservoir effect. But then they are formally not in BP, which includes fractionation correction by convention. The literature includes such dates, not corrected for fractionation but published in BP, leading users to subsequently subtract 400 years. But then the reservoir effect has been taken into account twice. The literature also includes marine dates corrected for both fractionation and reservoir effect, reported in BP; and also marine dates correctly not reported in BP, but which were interpreted as such nevertheless.

BP is not always what you think it is, sometimes it is not even BP . . .

In case of doubt, one has to go back to the basic numbers: the activity ratio ^{14}a measured relative to the oxalic acid standard, and the measured $\delta^{13}\text{C}$ value. These can be obtained from the laboratory that performed the measurements—provided the records did not get lost over the years, for example by closure of the laboratory or by no-longer-readable floppy discs. All of this is known to have happened.

For not pure marine samples, the situation is more complex as is made clear in the present article. This has led us to stay in the aquatic system for our analysis, not normalizing ^{14}C dates to $\delta^{13}\text{C} = -25\text{‰}$ which is representative for the terrestrial timescale. For this we introduced the property $^{14}\text{a}^{\text{SYS}}$, the ^{14}C activity ratio of the system when the fossil to be dated was alive. This circumvents subtraction of the reservoir effect (i.e. offset between aquatic and terrestrial age), it has been incorporated. In this article we do not use BP for the final shell age, but ^{14}C years.

For shell dates laboratories should report the stable isotope ratios $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ as usual, and the ^{14}C dates in BP (or F^{14}C) as is common practice—but also the measured activity ratio ^{14}a as defined in Mook and van der Plicht (1999); i.e. not normalized (corrected for fractionation). A good but rare example is a series of shells, measured conventionally (code KI) in the 1970s in Kiel (Erlenkeuser et al. 1975). The ^{18}O isotope was not measured. The shells are modern (containing the bomb peak) and originate from the German Bight. The authors state that results are calculated with the Libby half-life and refer to 95% of the NBS oxalic acid activity, in accordance with the latest ^{14}C conference (that would have been the 1972 conference). They also clearly state that the data are not corrected for isotopic effects. Hence these reported ^{14}C measurements are equivalent to our ^{14}a .

For completeness we mention that variations in reservoir effects are taken into account by the calibration curve Marine20 (Heaton et al. 2020).

Appendix G) example calculations

Below follow illustrative examples of model calculations, to guide the reader through the complexity of the formulas. Calculations are given for the models P, R and S. The activities ^{14}a are given in %, the stable isotope ratios δ in ‰.

g1) example “isotopic exchange”, $\Delta < 0$, model R

GrA-3186, *Cardium* shell from Maasdijk (Zuid Holland)

measured values: $^{14}\text{a} = 38.89 \pm 0.20$, $\delta^{13}\text{C} = -5.19$, $\delta^{18}\text{O} = -5.76$

calculated values:

$$\text{Eq. [10], } ^{13}\delta(\text{corrected}) = 1.20 \text{ } ^{18}\delta(\text{measured}) + 0.30 = -6.61$$

$$\text{Eq. [17], } \Delta = ^{13}\delta(\text{corrected}) - ^{13}\delta(\text{measured}) = -1.42 (\Delta < 0)$$

$$\text{Eq. [14], } ^{14}\text{a}^{\text{SYS}}(\text{est}) = 1.50 \text{ } ^{18}\delta(\text{measured}) + 98.50 = 89.86$$

$$\text{Eq. [15], } ^{14}\text{a}(\text{fin}) = ^{14}\text{a}(\text{measured}) / ^{14}\text{a}^{\text{SYS}}(\text{est}) = 43.28$$

$$\text{Eq. [16], } \text{estuary age} = -8033 \ln[^{14}\text{a}(\text{final})] = 6727 \text{ years}$$

$$\text{Eq. [18], } ^{14}\text{C age} = 6727 + 109 \Delta = 6727 + 155 = 6882$$

modeled ^{14}C age = 6880 ± 40 years, calibrated 7830–7615 calBP (95.4%, rounded to 5)

g2) example “secondary carbonate,” $\Delta > 0$, model P

GrN-18358, *Cardium* shell from Almere (Flevoland)

measured values: $^{14}\text{a} = 60.68 \pm 0.73$, $\delta^{13}\text{C} = -4.44$, $\delta^{18}\text{O} = -1.21$

calculated values:

$$\text{Eq. [9], } ^{13}\delta(\text{corrected}) = 1.64 \text{ } ^{18}\delta(\text{measured}) - 0.14 = -2.12$$

$$\text{Eq. [17], } \Delta = ^{13}\delta(\text{corrected}) - ^{13}\delta(\text{measured}) = 2.32 (\Delta > 0)$$

The total contribution for the second carbonate is given by equation [28], which requires the following input data:

$$\text{Eq. [13], } ^{14}\text{a}^{\text{SYS}}(\text{est}) = 2.05 \text{ } ^{18}\delta(\text{measured}) + 97.95 = 95.46$$

$$\text{Eq. [24], with } \gamma = 1: ^{14}\text{a}^{\text{SYS}}(\text{sec}) = 2 \text{ } ^{18}\delta(\text{measured}) + 97.00 = 94.58$$

$$\text{Eq. [28], } ^{14}\text{a}^{\text{SYS}}(\text{tot}) = (2.5^{14}\text{a}(\text{est}) + F \Delta \text{ } ^{14}\text{a}^{\text{SYS}}(\text{sec})) / (2.5 + F \Delta) = 95.24 \text{ with } F = 0.37$$

Now the final modeled age can be calculated:

Eq. [29], $^{14}\text{a}(\text{fin}) = 100 [^{14}\text{a}(\text{measured})/^{14}\text{a}^{\text{SYS}}(\text{tot})] = 63.72$

Eq. [30], ^{14}C age = $-8033 \ln(^{14}\text{a}(\text{fin})/100) = 3620$ years

modeled ^{14}C age = 3620 ± 95 , calibrated 4235–3645 calBP (95.4%, rounded to 5)

g3) example “stagnant water,” model S

GrN-32946, *Cardium glaucum* shell from Oostum (Groningen)

measured values: $^{14}\text{a} = 77.68 \pm 0.53$, $\delta^{13}\text{C} = -9.18$

calculated values:

Eq. [31], $\Delta^* = 1.5 - ^{13}\delta = 10.7$

$^{14}\text{a}(\text{sec}) = 97$ (see Appendix D)

Eq. [32], $^{14}\text{a}^{\text{SYS}}(\text{tot}) = [250 + F \Delta^* ^{14}\text{a}^{\text{SYS}}(\text{sec})]/(2.5 + 9.42) = 97.63$ with $F = 0.88$

Eq. [29], $^{14}\text{a}(\text{fin}) = 100 ^{14}\text{a}(\text{measured})/^{14}\text{a}(\text{tot}) = 79.57$

Eq. [30], ^{14}C age = $-8033 \ln(^{14}\text{a}(\text{fin})) = 1836$ ^{14}C years

modeled ^{14}C age = 1835 ± 55 , calibrated age 1885–1600 calBP (95.4%, rounded to 5)