

UNBIASED MULTI-PARAMETRIC ESTIMATIONS OF DISTANCES AND PECULIAR VELOCITIES OF THE GALAXIES

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Accurate estimates of distances and peculiar velocities for galaxies may be derived with the help of multi-dimensional regression analysis using two or more distance indicators p_k (corrected apparent sizes, luminosities, other distance-dependent quantities) and some calibrators q_i (velocity dispersions of the ellipticals or HI-line widths of the spirals, mean surface brightness, colours, other distance-independent quantities) together, cf. Georgiev (1992). Here an example is given for 349 spiral galaxies with axial ratio $D/d > 1.4$ from the sample of Fisher & Tully (1981). The p -values are the major axis and the blue magnitude and the q -values are the HI line width, type and axial ratio.

The deceleration laws in the nearby universe are $\log p_k = -\log V + \text{const}_k$, where using the Hubble law $\log V$ changes $\log R$ (Fig. 1). The deviations $\Delta \log V_{ik} = \Delta \log p_{ik} = \log V_i + \log p_{ik} - \text{const}_k$ are unbiased raw estimations of the peculiar velocities. The regressions $\Delta \log p_k = f_k(q_i)$ (Figs. 2 - 4) give better estimations $\langle \log V_{ik} \rangle = -\log p_{ik} + \text{const}_k - f_k(q_{ii})$. Figure 2 presents the shifted Tully-Fisher (TF) diagram and Fig. 5 shows the deceleration diagram after TF-corrections of the major axes.

The regressions $\Delta \log p_k = F_k(q_1, q_2, \dots)$ are the multi-parametric generalizations of the TF (or Faber-Jackson) relations. The initial velocity estimations in the multi-dimensional method are $\langle \log V_{ik} \rangle = -\log p_{ik} + \text{const}_k - F_k(q_{i1}, q_{i2}, \dots)$ and the final estimations $\langle \log V_i \rangle$ are obtained by the linear regression $\log V = G(\langle \log V_1 \rangle, \langle \log V_2 \rangle, \dots)$. The mean-square value of the final peculiar velocity estimations $\delta \log V_i = \log V_i - \langle \log V_i \rangle$ occurs about 1.2 times lower than that obtained by the pure TF-method (Fig. 6).

The general multi-dimensional method is performed by one C-program of the author including the graphics library of Dr. L. Georgiev (1991).

References

- Fisher, J.R. & Tully, R.B., 1981. *Astrophys. J. Suppl.*, **47**, 139.
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Georgiev, Ts., 1992. *Sov. Astron. Let.* **18** (*Pis'ma v Astron. Zh.*, **18**, 739).

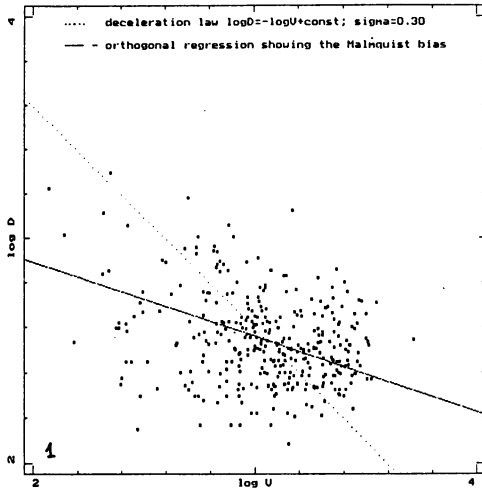


Figure 1. The observed deceleration diagram where V is the corrected Hubble velocity and D is the corrected apparent major axis: 1 - the deceleration law $\log D = -\log V + \text{const}$; $\sigma = 0.30$; 2 - the orthogonal regression showing the Malmquist bias.

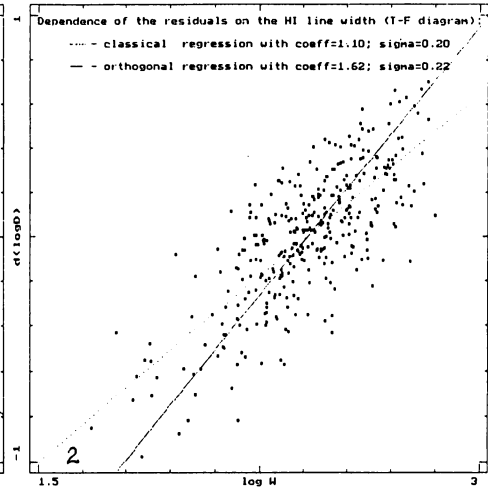


Figure 2. Shifted TF-diagram where $d(\log D)$ is the deviation from the deceleration law given in Fig. 1: 1 - classical regression; $\text{coeff.} = 1.10$; $\sigma = 0.20$; 2 - orthogonal regression; $\text{coeff.} = 1.62$; $\sigma = 0.22$.

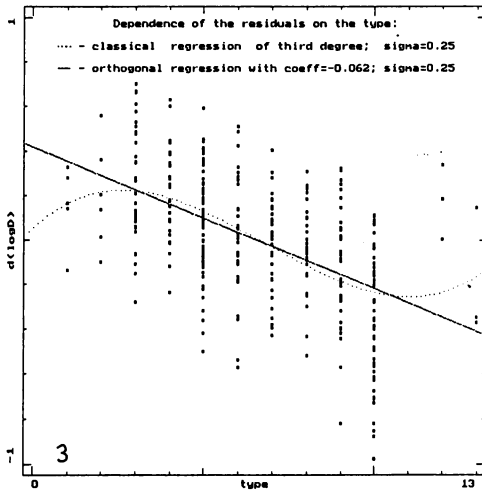


Figure 3. Dependence of the deviations from the deceleration law on the type and the axial ratio of the galaxy.

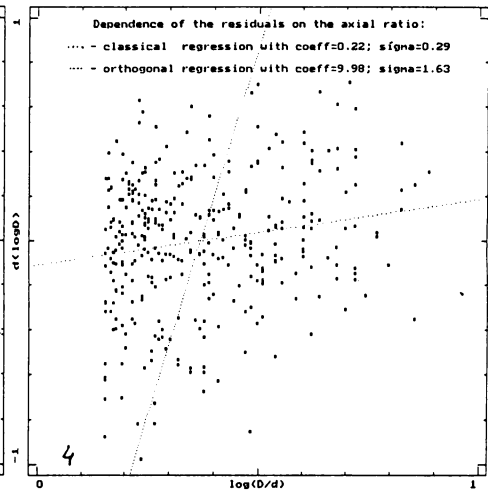


Figure 4. Dependence of the deviations from the deceleration law on the type and the axial ratio of the galaxy.

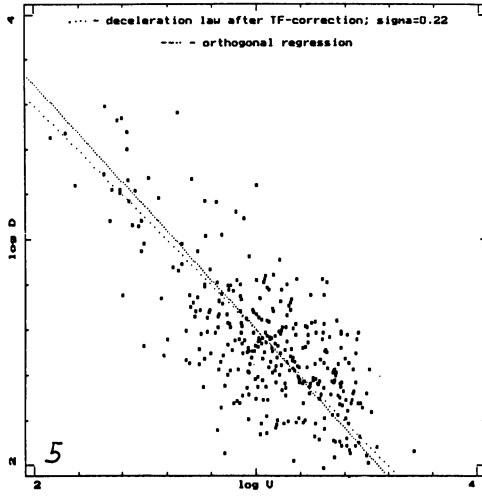


Figure 5. The deceleration diagram after TF-correction which illustrates our unbiased performance of the TF-method; $\sigma = 0.22$.

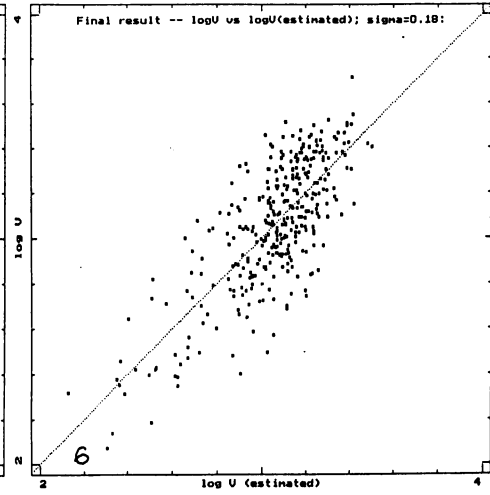


Figure 6. Comparison between the observed velocities and the velocities obtained by the full multi-parametric method; $\sigma = 0.18$.