

To the Editor of the *Mathematical Gazette*

DEAR SIR,

It would be interesting to have a large number of terms of the expression for  $\pi$  as a continued fraction with unit numerators, which starts

$$3 + \frac{1}{7+} \frac{1}{15+} \frac{1}{1+} \frac{1}{292+} \frac{1}{1+} \frac{1}{1+} \frac{1}{1+} \dots,$$

For a random irrational number (assuming that 'random' can be defined!) the probability that a denominator of the continued fraction is a given positive integer  $r$  is easily shown to be  $1/(r+1)$ . Now some irrational numbers are clearly not random. For example, quadratic irrationals recur, and  $e$  has a regular pattern. A sufficiently long expression for  $\pi$  would indicate whether  $\pi$  is random in this sense.

Of course, a continued fraction has the advantage over a decimal that it is independent of the scale of notation.

Yours etc., E. J. F. PRIMROSE

To the Editor of the *Mathematical Gazette*

DEAR SIR,

I would like to reply to one of the points raised by Mr. E. H. Lockwood (*Math. Gaz.*, 1958, **42**, 202). As a mathematician, he suggests that we should "teach our pupils to use letters to represent numbers, rather than distances, times or sums of money." As a teacher of chemistry I, along with many other teachers of the physical sciences, among whom I cite, in particular, Professor E. A. Guggenheim, instruct students in what Professor Guggenheim aptly terms the *quantity calculus* (*Journal of Chemical Education*, 1958, **35**, 606). It appears that the quantity calculus originated in the writings of A. Lodge (*Nature*, 1888, **38**, 281) and J. B. Henderson (*Math. Gaz.*, 1924, **12**, 99). In this calculus each letter, like  $P$ , symbolizes a physical quantity which is represented as the product of a measure (a real number) and an expression (often abbreviated) of the physical units which are being used. There are thus many possible representations of a physical quantity, as in the example  $P = 1 \text{ atm} = 1,013,250 \text{ dynes cm}^{-2} = 1.013250 \text{ bar} = 1.0332275 \text{ kg. cm}^{-2} = 76 \text{ cm mercury} = 29.92120 \text{ in. mercury} = 14.696006 \text{ lb. in}^{-2}$ . To illustrate I will translate into the language of the quantity calculus the following statement of Mr. Lockwood (*loc. cit.*). "At  $h$  feet above sea level the distance of the horizon is approximately  $\sqrt{3h/2}$  miles." In terms of the quantity calculus this becomes: "If  $h$  and  $d$  are the distances above sea level and to the horizon, then  $d/\text{miles} \simeq \sqrt{3h/2}$  feet." The student of physical science eventually encounters