

Dynamics of a rigid-flexible coupling system in a uniform flow

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Dynamics of two-dimensional flow past a rigid flat plate with a trailing closed flexible filament acting as a deformable afterbody are investigated numerically by an immersed boundary-lattice Boltzmann method for the fluid flow and a finite element method for the filament motion. The effects of Reynolds number (Re) and length ratio (Lr) on the flow patterns and dynamics of the rigid-flexible coupling system are studied. Based on our numerical results, five typical state modes have been identified in Lr – Re plane in terms of the filament shape and corresponding dynamics, i.e. static deformation, micro-vibration, multi-frequency flapping, periodic flapping and chaotic flapping modes, respectively. Benefiting from the passive flow control by using the flexible filament as a deformable afterbody, the coupled system may enjoy a significant drag reduction (up to 22%) compared with bare plate scenarios ($Lr = 1$). Maximum drag reduction achieved at $L_{c,min} \in [1.8, 2]$ is often accompanied by the onset of the system state transition. The flow characteristic and its relation to the change in hydrodynamic drag are further explored in order to reveal the underlying mechanisms of the counterintuitive dynamical behaviour of the coupled system. The scaling laws for the form drag and the friction drag, which arise from the pressure and viscous effects, respectively, are proposed to estimate the overall drag acting on the system. The results obtained in the present study may shed some light on understanding the dynamical behaviour of rigid-flexible coupling systems.

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1. Introduction

Fluid-structure interaction (FSI) phenomenon is ubiquitous in natural and engineering systems, in which a movable or deformable structure and an internal or surrounding fluid are coupled to influence the behaviour of each other (Dowell & Hall 2001; Griffith & Patankar 2020). The FSI problems may be further categorized into two subsets, i.e. fluid-rigid structure interaction and fluid-flexible structure interaction (Hua, Zhu & Lu 2014). The typical examples for the former scenario includes flow past a bluff body, e.g. cylinder (Prasanth & Mittal 2008), flat plate (Yang & Strganac 2013), sphere (Govardhan & Williamson 2005; Rajamuni, Thompson & Hourigan 2018) and other non-streamlined bodies (Derakhshandeh & Alam 2019), with the vortex-induced vibration (VIV) induced on bodies interacting with an external fluid flow (Williamson & Govardhan 2004; Choi, Jeon & Kim 2008; Raissi *et al.* 2019). The systems involving fluid-flexible structure interaction are also commonplace, e.g. swimming fish (Liu *et al.* 2017), flying birds or insects (Shyy *et al.* 2016), plant reconfiguration or flapping in a flow (Leclercq & de Langre 2018) and vibrating vocal fold (Li *et al.* 2019). Due to its important significance for understanding the fundamental principles in nature and the extensive engineering applications, currently, FSI is a topic of great attention in the fluid mechanics community (Dowell & Hall 2001; Griffith & Patankar 2020).

A concern for the FSI system is how to achieve the hydrodynamic advantages or performance enhancements by means of manipulation of surrounding fluid flows (Lighthill 1975; Alben 2009; Shoele & Mittal 2016). One interesting example is represented by biological flight and swimming. Fish could generate favourable flow structures for locomotion by adjusting the movement or deformation of their body and appendages (Wu 1961, 1971; Triantafyllou, Triantafyllou & Yue 2000; Alben & Shelley 2005; Li & Lu 2012). For example, previous experimental observations (Müller *et al.* 1997; Nauen & Lauder 2002) and numerical studies (Li & Lu 2012; Liu *et al.* 2017) have revealed that the ring-like vortical structures formed in the wake of fish swimming possess intrinsic connections with the optimization of thrust generation and power consumption. In the flight of insects, by adopting appropriate flapping kinematics, the leading-edge vortex (LEV) stays attached to and moving with the surface of the wing, which leads to the high lift in the low Re flow region (Ford & Babinsky 2013; Eldredge & Jones 2019).

Beside these active flow controls for the optimal propulsion, swimming and flying animals may achieve hydrodynamic advantages from the passive flexible deformation of the propulsors (tail fins and wings) due to flow-induced loads. Results from the experimental (Mazaheri & Ebrahimi 2010; Nakata *et al.* 2011), numerical (Kang *et al.* 2011; Zhu, He & Zhang 2014; Wang, Huang & Lu 2020) and theoretical (Michelin & Smith 2009; Alon Tzezana & Breuer 2019; Alaminos-Quesada & Fernandez-Feria 2020) studies have shown that the proper flexibility of the fin or wing is found to bear performance benefits, such as thrust enhancement, drag reduction, energy saving, etc. Furthermore, as a possible strategy to reduce the drag and resist breakage, the plants living in flow-dominated habitats are able to reduce their frontal area or reshape themselves in a more streamlined fashion, which is referred to as ‘reconfiguration’ (Alben, Shelley & Zhang 2002; Schouveiler & Eloy 2013; Alvarado *et al.* 2017; Leclercq & de Langre 2018). Compared with active flow controls, the shape self-adaptation due to flow-induced reconfiguration of flexible structure does not need the intervention of the control system

or the energy input, which may be an elegant and deft way to the aero/hydrodynamic performance of the FSI system.

Not surprisingly, the flow controls by the passive deformation and flapping of flexible structures in a natural system are found universally, as they have survived the tests of evolution over millions of years and reached a high level of adaptability and effectiveness. Therefore, it is particularly worthwhile to import these novel ideas which originate from nature into technological applications, such as flow control of vortex shedding behind bluff bodies. The bluff body flow control is not only encountered in numerous natural scenarios (Triantafyllou *et al.* 2000; Alvarado *et al.* 2017; Leclercq & de Langre 2018), but also of practical interest to many fields of engineering (Choi *et al.* 2008; Dong, Triantafyllou & Karniadakis 2008; Fan *et al.* 2020). When the fluid flows around the bluff body, the boundary layer is likely to separate into Kármán vortices alternately shedding in the wake, which would cause the increase in differential pressure resistance (form drag). The more severe the separation at the hind side, the greater the form drag. Meanwhile, the asymmetric vortex shedding would induce large unsteady side forces that, in turn, may lead to structural vibrations if the body is flexibly mounted. Therefore, for reducing drag and suppressing VIV, controls of vortex shedding characteristics of flow over a bluff body have attracted significant attention in the past (Zhao 2021). Many flow control techniques have been proposed in (i) passive form and (ii) active form. The first approach includes the splitter plate (Anderson & Szewczyk 1997; Gilliéron & Kourta 2010), segmented trailing edges (Deshpande & Sharma 2012), dimples and grooves (Bearman & Harvey 1993), etc. In these methods, global changes in the surface shape may be required for practical situations. However, it seems hard to implement under some circumstances. In the latter approach, such as blowing and suction (Schatzman *et al.* 2014), synthetic jets (Glezer & Amitay 2002), rotary oscillations (Palkin *et al.* 2018), the intervention of a complex control system or/and the energy input are necessary, limiting the applicability of this approach.

As a passive flow control technique, installing splitter plates behind a bluff body has been investigated by numerous experiments and simulations in the past (Anderson & Szewczyk 1997; Gilliéron & Kourta 2010; Wu *et al.* 2014; Sunil, Kumar & Poddar 2022). A splitter plate, attached downstream, inhibits the interaction between the separating shear layers, thereby delaying vortex shedding and resulting in a weaker Kármán vortex street in the wake (Sunil *et al.* 2022). This reduces the fluctuating lift and drag acting on the bluff body. Earlier studies were mainly limited to the rigid plates. Recently, inspired by the drag-reducing mechanism of passive flexibility in natural systems, particular attention has been devoted to the flexible splitter plate (Lācis *et al.* 2014; Wu *et al.* 2014; Sunil *et al.* 2022). It is found that a filament, with proper flexibility and length, may bring about more performance benefits in suppressing/weakening the vortex shedding as compared with a rigid splitter plate with the same length (Wu *et al.* 2014; Sunil *et al.* 2022). In addition, some studies have found that installing two or multiple flexible filaments behind a bluff body, referred to as ‘hairy coating’, can offer more drag reduction under specific conditions than a single filament (Favier *et al.* 2009; Niu & Hu 2011; Deng, Mao & Xie 2019). Favier *et al.* (2009) and Niu & Hu (2011) have performed the numerical and experimental investigations, respectively, on the passive flow control by using this self-adaptive hairy coating. They have shown that a sizable drag reduction can be achieved at the optimum combination of the considered parameters, e.g. hair length, rigidity, and density. The primary mechanism for drag reduction is the bending, adhesion and reinforcement of hairs trailing the bluff body, which reduces wake width and traps ‘dead water’ (Niu & Hu 2011).

More recently, Gao *et al.* (2020) have proposed a nature-inspired passive control of the bluff body flow for drag reduction. In their experimental study, a trailing closed filament, with a negligible weight and small bending modulus, was ‘hung’ on both edges of the rigid

flat plate placed normal to the oncoming flow. The experiment suggests that by adopting such a ‘flexible coating’, a significant drag reduction of approximately 10.0% is expected under specific conditions. Compared with the existing flow control devices, this device is easy to install and disassemble. Besides, it is supposed to have good adaptability for a wide range of flows, benefiting from its nature of shape self-adaptation.

On the other hand, the study of a rigid-flexible coupling system raises a new kind of FSI problem, in which the closed flexible structure is coupled with not only an external fluid but also an internal fluid to influence the behaviour of each other. This complex interaction may give rise to a rich variety of physical phenomena which are dictated by complex mechanisms. These extended FSI systems are common in a living body in which some fluid volume is inside the thin skins of organisms, and were treated as a flexible ring filled with fluid in a surrounding fluid flow (Jung *et al.* 2006; Shoele & Zhu 2010; Kim *et al.* 2012). However, to our knowledge, still very few studies have focused on the dynamics of this coupling system.

At present, the dynamics of the rigid-flexible coupling system remain unclear. Moreover, the in-depth understanding of the corresponding flow control mechanism for drag reduction is still lacking. Inspired by Gao *et al.* (2020), we perform numerical simulations of viscous flow past a rigid flat plate with a trailing closed flexible filament. In comparison with experimental study, numerical simulations have an advantage in the aspect of quantitative analysis, which is particularly critical for exploring relevant mechanisms underlying the complex behaviour of a system. In this paper, the influence of Reynolds number (Re) and length ratio of the filament and flat plate (Lr) on the flow patterns and dynamics of the rigid-flexible coupling system have been systematically investigated. The drag reduction and the underlying mechanisms have been examined and revealed as well.

The rest of the present paper is organized as follows. The computational model, including physical problem and mathematical formulation, numerical method and validation, is described in § 2. The result and discussion regarding dynamic states of the rigid-flexible coupling system, drag and the flow characteristics, and drag estimate are given from a comprehensive numerical investigation in § 3. Finally, the concluding remarks are addressed in § 4.

2. Computational model

2.1. Physical problem and mathematical formulation

The rigid-flexible coupling system considered in the present study is shown in figure 1(a). The rigid flat plate with a trailing closed flexible filament are immersed in a two-dimensional uniform flow with oncoming velocity U . The rigid flat plate is fixed and placed normal to the oncoming flow. The two edges of the flexible filament are attached to the edges of the flat plate with simply support boundary conditions. The other parts of the filament can move freely and deform passively due to the flow-structure interactions. The geometry of this system is described by using a dimensionless parameter $Lr = L/D$, where L and D are the length of the flexible filament and flat plate, respectively. It is noted that $Lr = 1$ corresponds to the situation without the trailing filament.

In this system, the fluid flow is governed by the incompressible Navier–Stokes equations,

$$\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} = -\frac{1}{\rho} \nabla p + \frac{\mu}{\rho} \nabla^2 \mathbf{v} + \mathbf{f}_b, \quad (2.1)$$

$$\nabla \cdot \mathbf{v} = 0, \quad (2.2)$$

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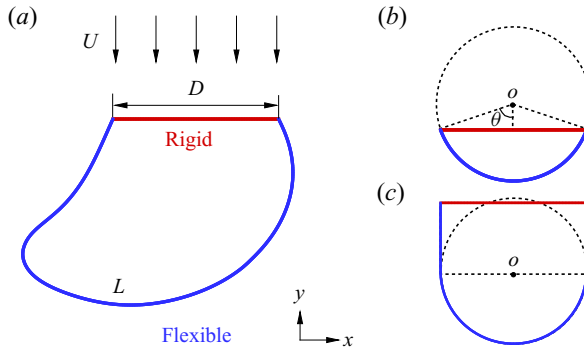


Figure 1. Schematic diagram for the rigid-flexible coupling system in a two-dimensional uniform flow (a). The rigid flat plate with length D is fixed and placed normal to the flow with oncoming velocity U . The flexible filament, severed as a deformable afterbody, is simply supported on its both edges and attached to the two edges of the flat plate. The geometry of this system is described by using a dimensionless parameter $Lr = L/D$, where L is the length of the filament. Note that $Lr = 1$ corresponds to the situation without the trailing filament. The initial shapes of the filament for the situations with $Lr < \pi/2$ and $Lr \geq \pi/2$ are illustrated in figures 1(b) and 1(c), respectively. For cases with $Lr < \pi/2$, the initial area enclosed by the flat plate and filament is set initially to a circular segment with $Lr = \theta/\sin\theta$, where θ is the semi-central angle subtending the arc. While for cases with $Lr \geq \pi/2$, the initial area is set initially to a combination of rectangle and semicircle. According to this definition, the D^2 -normalized initial enclosed area Ω_0 can be calculated by (2.5).

where $\mathbf{v} = (u, v)$ is the velocity, p the pressure, ρ the density of the fluid, μ the dynamic viscosity and \mathbf{f}_b the body force term. A uniform velocity U is set at the inlet boundary and the side boundaries of the fluid computational domain. A Neumann boundary condition is specified at the outlet boundary.

The deformation and motion of flexible filament are described by the structural equation (Doyle 2001; Connell & Yue 2007; Ye *et al.* 2017),

$$\rho_s h \frac{\partial^2 \mathbf{X}}{\partial t^2} = \frac{\partial}{\partial s} \left[Eh \left(1 - \left| \frac{\partial \mathbf{X}}{\partial s} \right|^{-1} \right) \frac{\partial \mathbf{X}}{\partial s} - \frac{\partial}{\partial s} \left(EI(\kappa - \kappa_0) \frac{\partial^2 \mathbf{X}}{\partial s^2} / \left| \frac{\partial^2 \mathbf{X}}{\partial s^2} \right| \right) \right] + \mathbf{F}_s, \tag{2.3}$$

where s is the Lagrangian coordinate along the plate, h is the structure thickness, $\mathbf{X}(s, t) = (X(s, t), Y(s, t))$ is the position vector of the plates, \mathbf{F}_s is the Lagrangian force exerted on the plates by the surrounding fluid and ρ_s is the structural density; Eh and EI are the structural stretching and bending rigidity, respectively; $\kappa = |\partial^2 \mathbf{X} / \partial s^2|$ is the local curvature of the filament with κ_0 its initial reference value. It is noted that the filament is set to be in an initial stressless reference state, according to (2.3). Moreover, the simple support boundary conditions applied at the edges of the filament are respectively given by

$$\mathbf{X} = (\pm 0.5, 0), \quad \frac{\partial^2 \mathbf{X}}{\partial s^2} = (0, 0). \tag{2.4}$$

The filament is initially placed at rest in the fluid. The initial shapes of filament for the situations with $Lr < \pi/2$ and $Lr \geq \pi/2$ are illustrated in figures 1(b) and (c), respectively. For cases with $Lr < \pi/2$, the enclosed area by the flat plate and filament is set initially to a circular segment; while for cases with $Lr < \pi/2$, the enclosed area is set initially to a combination of rectangle and semicircle. According to this definition, the relationship

between D^2 -normalized initial area (Ω_0) and length ratio (Lr) can be given as

$$\Omega_0 = \begin{cases} \frac{1}{4}(\theta/\sin^2\theta - \cot\theta), & \text{if } Lr < \frac{1}{2}\pi, \\ \frac{1}{2}Lr - \frac{1}{8}\pi, & \text{if } Lr \geq \frac{1}{2}\pi, \end{cases} \quad (2.5)$$

where $Lr = \theta/\sin\theta$, and θ is the semi-central angle subtending the arc. In the present simulations the volume leakage is negligible which is consistent with the experiment of Gao *et al.* (2020). Thus, the enclosed area $\Omega(t) \approx \Omega_0$, which merely depends on Lr .

The characteristic quantities ρ , D and U are chosen to normalize the above equations. Thus, the following dimensionless governing parameters are introduced: the Reynolds number $Re = \rho UD/\mu$, the stretching stiffness $S = Eh/\rho U^2 D$, the bending stiffness $K = EI/\rho U^2 D^3$, the mass ratio of the plates and the fluid $M = \rho_s h/\rho D$, the length ratio of the flexible filament and the rigid plate $Lr = L/D$.

2.2. Numerical method

The governing equations of the fluid-plate problem are solved numerically by an immersed boundary-lattice Boltzmann method for the fluid motion and a finite element method for the deformation of the flexible filament. The lattice Boltzmann equation with the body force model (Guo, Zheng & Shi 2002) is employed in present simulations, i.e.

$$f_i(\mathbf{x} + \mathbf{e}_i \Delta t, t + \Delta t) - f_i(\mathbf{x}, t) = -\frac{1}{\tau}[f_i(\mathbf{x}, t) - f_i^{eq}(\mathbf{x}, t)] + \Delta t F_i, \quad (2.6)$$

where $f_i(\mathbf{x}, t)$ is the distribution function for particles with \mathbf{e}_i at position \mathbf{x} and time t . The D2Q9 velocity model is applied here. Here Δx and Δt are the grid spacing and time step, respectively; τ is relaxation time associated with fluid viscosity (ν), i.e. $\tau = \nu/c_s^2 \Delta t + 0.5$, where $c_s = (\Delta x/\Delta t)/\sqrt{3}$ is the lattice sound speed. The equilibrium distribution function $f_i^{eq}(\mathbf{x}, t)$ and the force term F_i are defined as (Guo *et al.* 2002)

$$f_i^{eq} = \omega_i \rho \left[1 + \frac{\mathbf{e}_i \cdot \mathbf{v}}{c_s^2} + \frac{\mathbf{v} \mathbf{v} : (\mathbf{e}_i \mathbf{e}_i - c_s^2 \mathbf{I})}{2c_s^4} \right], \quad (2.7)$$

$$F_i = \left(1 - \frac{1}{2\tau} \right) \omega_i \left[\frac{\mathbf{e}_i - \mathbf{v}}{c_s^2} + \frac{\mathbf{e}_i \cdot \mathbf{v}}{c_s^4} \mathbf{e}_i \right] \cdot \mathbf{f}_b, \quad (2.8)$$

where ω_i is the weighting factor depending on the lattice model ($\omega_0 = 4/9$, $\omega_1 = \omega_2 = \omega_3 = \omega_4 = 1/9$, $\omega_5 = \omega_6 = \omega_7 = \omega_8 = 1/36$), and \mathbf{I} is the unit tensor. The density ρ and velocity \mathbf{v} can be calculated by

$$\rho = \sum_i f_i, \quad \rho \mathbf{v} = \sum_i \mathbf{e}_i f_i + \frac{1}{2} \mathbf{f}_b \Delta t. \quad (2.9)$$

The immersed boundary method employed in this study has been extensively used to simulate the FSI problems (Peskin 2002; Mittal & Iaccarino 2005). The Lagrangian force between the fluid and structure \mathbf{F}_s can be calculated by the penalty scheme (Goldstein, Handler & Sirovich 1993)

$$\mathbf{F}_s = \alpha \int_0^t [V_f(s, t') - V_s(s, t')] dt' + \beta [V_f(s, t) - V_s(s, t)], \quad (2.10)$$

where α and β are negative large penalty parameters which are selected based on the previous studies (Hua, Zhu & Lu 2013; Ye *et al.* 2017; Peng, Huang & Lu 2018a,c),

$V_s = \partial X / \partial t$ is the velocity of Lagrangian material point of the filament, and V_f is the fluid velocity at the position X obtained by interpolation

$$V_f(s, t) = \int \mathbf{v}(\mathbf{x}, t) \delta(\mathbf{x} - \mathbf{X}(s, t)) d\mathbf{x}. \quad (2.11)$$

The body force term \mathbf{f}_b in (2.1) represents an interaction force between the fluid and the immersed boundary to enforce the no-slip velocity boundary condition. The Lagrangian force is spread to the nearby Eulerian grids by using the expression

$$\mathbf{f}_b(\mathbf{x}, t) = - \int \mathbf{F}_s(s, t) \delta(\mathbf{x} - \mathbf{X}(s, t)) ds, \quad (2.12)$$

where $\delta(\mathbf{x} - \mathbf{X})$ is the Dirac delta function. Note that in the simulations, \mathbf{f}_b is distributed over several Eulerian grids in width by using a smoothed delta function interpolation. Thus, the leakage of internal fluid area enclosed by the flat plate and filament may arise, due to the use of the smoothed approximation to the Dirac delta function (Kim *et al.* 2012; Ye *et al.* 2017).

Here we adopt a penalty forcing scheme proposed by Kim *et al.* (2012) to diminish the area leakage effect. In the scheme, the fluid compressibility β is defined as

$$\beta = - \frac{1}{\Omega} \frac{\partial \Omega}{\partial p}, \quad (2.13)$$

where Ω is the fluid area enclosed by the plate and filament and p denotes the pressure. Integrating above the differential relation between Ω and p , and using Taylor's expansion, the pressure difference between the interior and exterior of the enclosed area can be approximated by

$$\Delta p = \frac{1}{\beta} \left(1 - \frac{\Omega}{\Omega_0} \right) + \frac{1}{\beta} \int_0^t \left(1 - \frac{\Omega}{\Omega_0} \right) dt', \quad (2.14)$$

where Ω_0 denotes the initial interior area and the last term of the equation represents historical effects. Thus, the penalty force for area conservation is calculated by using the pressure difference Δp as

$$\mathbf{F}_\Omega = \Delta p \mathbf{e}_n, \quad (2.15)$$

where \mathbf{e}_n represents the local normal unit in the direction from the interior to the exterior of the enclosed area. This force is also added to the structure motion equation (2.3) as an external force term.

Equation (2.3) is discretized by a nonlinear finite element method with a co-rotational scheme. A detailed description of the method can be found in Doyle (2001). The motion of the filament in the present study is regarded as a large-displacement and small-strain deformation problem. By using the co-rotational scheme, the original problem with the geometrical nonlinearities in global coordinates splits into two parts, i.e. the rigid body motion and pure deformation in local coordinates, which are resolved by the coordinate transformation and linear theory, respectively. A detailed description of the above numerical method can be found in our previous papers (Hua *et al.* 2013; Ye *et al.* 2017; Peng *et al.* 2018a,c; Peng, Huang & Lu 2018b).

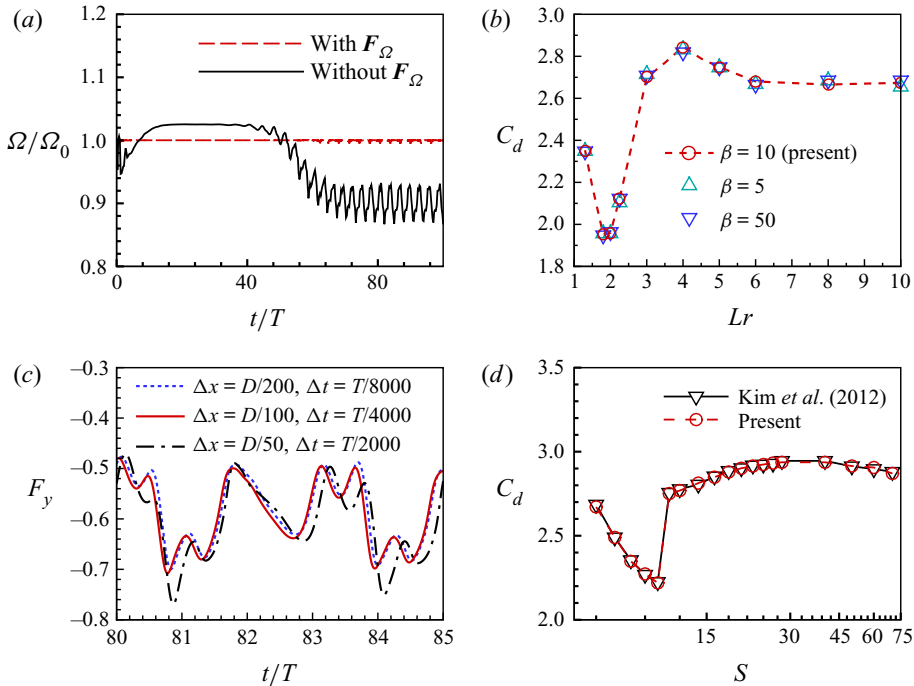


Figure 2. Validations of the present numerical method. (a) The area enclosed by the flat plate and deformable filament, Ω/Ω_0 , as a function of time for cases with and without penalty force, respectively. In these cases, $Re = 100$, $Lr = 2.5$, $K = 0.001$, $S = 1000$ and $M = 0.1$. (b) The variations of the mean drag coefficient as a function of Lr for the cases with $Re = 100$ and $\beta = 5, 10, 50$. (c) The time variations of F_y for the cases with $Lr = 2$, $Re = 100$ under different lattice spacings ($\Delta x = D/200, D/100$ and $D/50$) and time steps ($\Delta t = T/8000, T/4000$ and $T/2000$). (d) The variations of the mean drag coefficient as a function of S for the cases of a flapping ring in a uniform flow. The present results are provided to compare with the previous results (Kim *et al.* 2012). Here, $K = 0.01$, $Re = 100$ and $S = 6-70$.

2.3. Validation

Based on our convergence studies with different computational domains, the computational domain for fluid flow is chosen as $20D \times 50D$ in the x and y directions. The domain is large enough so that the blocking effects of the boundaries are not significant. In the x and y directions the mesh is uniform with spacing $\Delta x = \Delta y = D/100$. The filament is discretized with a mesh size of $\Delta s = D/100$. The time step is $\Delta t = T/4000$ for the simulations of fluid flow and filament motion, with $T = D/U$.

Figure 2(a) shows the time histories of the changes in area with and without the penalty forcing strategy for the case with $Re = 100$, $Lr = 2.5$, $K = 0.001$, $S = 1000$ and $M = 0.1$. It is seen that the maximum area leakage is $\sim 0.5\%$ and $\sim 12\%$ for the cases with and without the penalty force, respectively. The results indicate when the penalty forcing strategy is adopted, the area conservation is improved significantly and satisfied for the present study.

To examine the effect of β on the results of simulations, figure 2(b) shows the variations of the mean drag coefficient as a function of Lr for the cases with $Re = 100$ and varying β , i.e. $\beta = 5, 10$ and 50 . It is found that the choice of β does not affect the overall drag of the coupling system for all the cases with $Lr \in (1, 10]$. Whereas, it should be noted that a very small value of β may cause numerical instability, while a very large value of β may not

guarantee volume conservation. In our simulations, $\beta = 10$, which can ensure the volume conservation and numerical stability at the same time.

Also, the grid spacing and time step independence studies are performed. [Figure 2\(c\)](#) shows the time-dependent F_y of the afterbody calculated under the different lattice spacings and time steps for the typical case with $Lr = 2$, $Re = 100$. It is confirmed that $\Delta x = D/100$ and $\Delta t = T/4000$ are sufficient to achieve accurate results in the present simulations with $Re = 100$. Further verification shows that $\Delta x = D/100$ and $\Delta t = T/4000$ are also sufficient to accurately simulate the flows at higher Re , e.g. $Re = 800$ (not shown in [figure 2c](#)). Hence, in all of our simulations, $\Delta x = D/100$ and $\Delta t = T/4000$ were adopted.

To further validate the present numerical method, we simulate a flexible ring flapping in a uniform flow. [Figure 2\(d\)](#) shows the mean drag coefficients of the ring as functions of S for $K = 0.01$ and $Re = 100$. It is seen that the present results agree well with those of Kim *et al.* (2012).

In addition, the numerical strategy used in this study has been validated and successfully applied to a wide range of flows, such as the dynamics of fluid flow over flexible filaments (Tian *et al.* 2010) or loops (Ye *et al.* 2017), and self-propulsion of flapping flexible plates (Hua *et al.* 2013; Peng *et al.* 2018a,c).

3. Results and discussion

In the study, the effects of the length ratio ($1 \leq Lr \leq 10$) and Reynolds number ($10 \leq Re \leq 800$) are investigated. It is noted that $Lr = 1$ corresponds to the situation without the trailing filament. In all our simulations, the mass ratio ($M = 0.1$), bending stiffness ($K = 0.001$) and stretching stiffness ($S = 1000$) are fixed. The mass ratio is fixed at $M = 0.1$, which matches the case of a flexible afterbody in the wind tunnel ($M \sim O(10^{-1}-10^0)$). A large value of the stretching stiffness S is chosen such that the stretching deformation of the filament can be neglected. We chose a very small bending stiffness K so that the filament is fully compliant with the surrounding flow, which is consistent with the previous experiments (Gao *et al.* 2020).

3.1. Dynamic states of the rigid-flexible coupling system

In this section we present the dynamic states of the rigid-flexible coupling system in a flow. Based on a variety of simulations for a wide range of parameters considered here, we have identified five typical modes of dynamic behaviours in terms of the filament motion and flow pattern, i.e. static deformation (SD) mode, micro-vibration (MV) mode, multi-frequency flapping (MFF) mode, periodic flapping (PF) mode, and chaotic flapping (CF) mode, respectively.

[Figure 3\(a\)](#) shows the instantaneous vorticity contour and shape deformation of the filament for the case with $Re = 10$, $Lr = 2.25$, corresponding to the SD mode. Animations are also given in supplementary movie 1. It is seen that for the SD mode, the filament adapts to the streamlines of the surrounding flow and undergoes a static deformation with the fluid loading. The steady wake downstream of the plate is formed because of the low Re . Specifically, the shear layers with opposite vorticity formed at the edges of the plate, attached to the reshaped afterbody and then dissipated downstream (see [figure 3a](#)). In addition, the snapshot of the reshaped filament for other cases with $Re = 10$ and $Lr = 1.1, 1.5, 4, 6, 8, 10$ are also plotted with solid green lines in [figure 3\(f\)](#). It is shown that for the SD mode, the filament appears stationary and has reflectional symmetry about its midline, behaving like a rigid body. As Lr increases, the filament sequentially appears

as ‘plate-like’ (e.g. $Lr = 1.1$), ‘cylinder-like’ (e.g. $Lr = 1.5$) and ‘slender’ (e.g. $Lr = 10$) shapes, which is consistent with experimental observations (Gao *et al.* 2020). It is noted that for the cases with large Lr , the rear part of the filament is squeezed by the surrounding fluid, yielding a rounded tip at the end of the afterbody. Figure 3(b) shows the instantaneous vorticity contour and shape deformation of the filament for the case with $Re = 100$, $Lr = 1.3$, corresponding to the MV mode. A video showing the vortex shedding and filament vibration is also included in supplementary movie 2. As we can see, the shear layers begin to separate at the edges of the flat plate and then form a pair of alternately shedding vortices, i.e. Kármán vortices. The figure also illustrates the development and spatial organization of the Kármán vortices in the far wake. It is seen that the alternate vortices convect downstream parallel to the centreline as two rows of vortices having opposite rotation. A snapshot of the deformation configurations of the filament is shown in figure 3(g). For the MV mode, the flexible filament experiences a particularly small vibration, along with the alternate shedding of the Kármán vortices. To further describe the dynamics of the filament, figure 4(a) shows the time variation of the lift coefficient (C_l) for the overall system and transverse position of the filament midpoint (x_m) for the case with $Re = 100$, $Lr = 1.3$. Here the lift coefficient is defined as $C_l = \langle F_x \rangle / \frac{1}{2} \rho U^2 D$, where $\langle q \rangle := (1/(t_1 - t_0)) \int_{t_0}^{t_1} q(t) \cdot dt$ and $q(t)$ is an integrable physical quantity. In the computations, $t_1 - t_0$ is chosen as 10 times $1/f_1$, where f_1 is the dominant frequency of the integrand. As shown in figure 4(a), C_l changes with time periodically around its averaged value zero. It is also seen that the filament vibration amplitude in terms of the peak-to-peak value of x_m is less than $0.04D$ (see inset within figure 4a). According to the power spectrum density (PSD) of C_l (see figure 4e), an isolated frequency ($f_1 = 0.178$) of lift change, which is equal to that of the vortex shedding and the filament micro-vibration, is observed. Note that compared with the MV mode, the lift for the SD mode case is time invariant, i.e. $C_l = 0$, thus, the time variation and PSD of C_l for the SD mode are not given in figure 4.

The behaviours of the flow pattern and the filament deformation for the case with $Re = 100$ and $Lr = 2.25$, corresponding to the MFF mode, are shown in figures 3(c,h), and animated in supplementary movie 3. In this case, the Kármán vortex street is also found in the wake of the coupled system (see figure 3c). It is noted that the distance between the two rows of vortices having opposite rotation becomes smaller, compared with that for the MV mode cases. Moreover, the filament experiences a flapping motion with a larger amplitude with the pick-to-pick value of $x_m \approx 0.34D$, as shown in figures 3(h) and 4(b). The curve of $C_l(t)$ in figure 4(b) shows a distinct pick (or valley) near the maximum (or minimum) value of x_m , indicating the in-phase relation between the variations of C_l and x_m . As shown in figure 4(f), the PSD of C_l suggests multiple discrete frequencies for the filament flapping, e.g. $f_1 = 0.155$, $f_2 = 0.472$, $f_3 = 0.789$, etc., whereas the first frequency f_1 , i.e. vortex shedding frequency, is dominant.

As Lr becomes larger, the dynamic state of the system may switch from the MFF mode to PF mode. Here we use the case with $Re = 100$ and $Lr = 6$ as an example for the PF mode, as shown in figure 3(d,i) and supplementary movie 4. It is seen that for the PF mode, the filament flaps periodically; meanwhile, the separated shear layers become unstable, resulting in periodic alternate shedding of vortices. Different from the multiple discrete frequencies for the filament flapping in the MFF mode, an isolated frequency for the PF mode cases is found, e.g. $f_1 = 0.155$ for $Lr = 6$ and $Re = 100$, as shown in figure 4(g). In addition, the phase difference $\Delta\varphi$ between the maximum C_l and the maximum x_m is about π , indicating the out-phase relation between time variations of C_l and x_m (see figure 4c).

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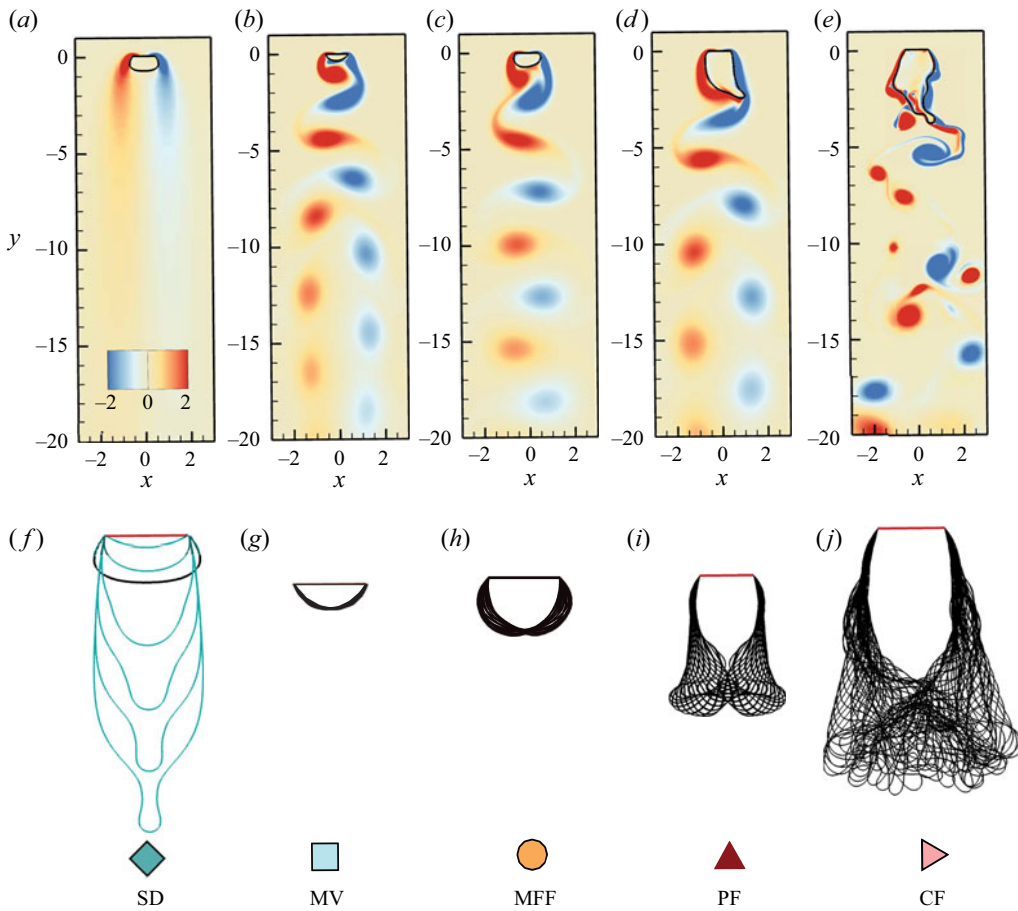


Figure 3. Behaviours of the flow patterns and deformations of filament shapes: (a–e) the instantaneous vorticity contours, and (f–j) the envelopes (solid black lines) of the flexible filaments for five distinct modes with $Re = 10$, $Lr = 2.25$ (a,f), $Re = 100$, $Lr = 1.3$ (b,g), $Lr = 2.25$ (c,h), $Lr = 6$ (d,i) and $Re = 800$, $Lr = 9$ (e,j), corresponding to the static deformation (SD), micro-vibration (MV), multi-frequency flapping (MFF), periodic flapping (PF) and chaotic flapping (CF) modes, respectively. Animated visualisations of the dynamic states for these modes have also been provided in supplementary movies available at <https://doi.org/10.1017/jfm.2022.466>. For the SD mode, the snapshot of the filament deformation shapes for other cases with $Re = 10$ and $Lr = 1.1, 1.5, 4, 6, 8, 10$ are also plotted with solid green lines in figure 3(f).

Figures 3(e) and 3(j) show the behaviours of the flow pattern and the filament deformation for the case with $Re = 800$, $Lr = 9$, corresponding to the CF mode. A video showing the dynamics of this case is also provided in supplementary movie 5. Here, we note that even though the flexible afterbody may deform greatly and flap strongly in the CF mode, the self-contact phenomenon has not been observed during the process of the different parts of the afterbody approaching and moving away from each other. Unlike the ordered flow patterns in the MV, MFF and PF modes, the chaotic vortical structures are found in the wake of the coupled system for the CF mode case (see figure 3e). The shear layers attached to the filament start to roll up at the forepart of the afterbody and then break into eddies with varying sizes irregularly shedding in the wake (see figure 3e), accompanied by the chaotic flapping of the filament (see figure 3j). Furthermore, the curves of $C_l(t)$ and $x_m(t)$ illustrate the dynamic disorder of the coupled system, as shown in

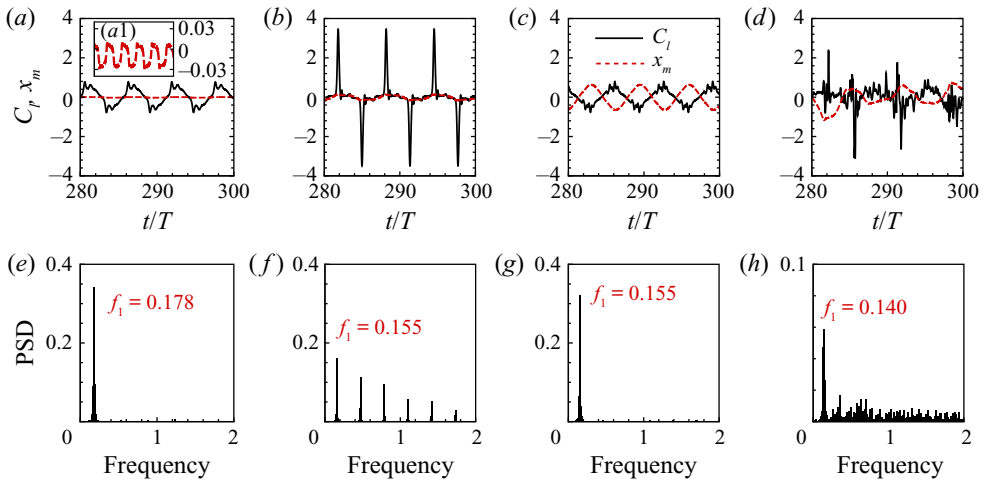


Figure 4. Time variations of the lift coefficient C_l (solid line) of the overall system and the transverse position x_m (dashed line) of the midpoint of filament (*a–d*), and power spectrum density (PSD) of $C_l(t)$ (*e–h*) for cases with $Re = 100$, $Lr = 1.3$ (*a,e*), $Lr = 2.25$ (*b,f*), $Lr = 6$ (*c,g*) and $Re = 800$, $Lr = 9$ (*d,h*), corresponding to the MV, MFF, PF and CF modes, respectively. Inset: enlargement of the variation of x_m versus time for the MV mode with $Re = 100$, $Lr = 1.3$ (*a1*).

figure 4(*d*). Moreover, figure 4(*h*) shows the PSD of C_l for the case with $Re = 800$, $Lr = 9$. As one can see, figure 4(*h*) shows a broadband spectrum, indicating a non-periodic behaviour of the coupled system. Moreover, a high peak is found at $f_1 = 0.140$ (see figure 4(*h*)), showing the dominant flapping frequency for the filament flapping and vortex shedding. In the discussion above, it is interesting to note that there is an obvious difference in the phase relation between C_l and x_m for the MFF and PF modes. To further illustrate this point, the variations of the phase difference $\Delta\varphi$ between the maximum C_l and the maximum x_m as functions of Lr for different Re are shown in figure 5(*a*). It is seen that the system mode switches from the MFF mode to PF mode as Lr increases, resulting in a jump of $\Delta\varphi$, e.g. $\Delta\varphi \approx 0$ for the MFF mode case with $Re = 100$, $Lr = 2$ and $\Delta\varphi \approx \pi$ for the PF mode case with $Re = 100$, $Lr = 7$. Moreover, the root-mean-square (rms) values of the transverse position of the filament midpoint, $x_{m,rms}$, as functions of Lr for various Re , are shown in figure 5(*b*). It is revealed that as the increase of Lr , $x_{m,rms}$ follows obviously different variations within different mode regions. For example, when $Re > 50$, the $x_{m,rms}$ first increases linearly within the MV mode region ($Lr < 2$), and then experiences an enormous increase by following a logarithmic growth law until reaching its maximum value at $Lr \approx 3.5$. After that, $x_{m,rms}$ gradually decreases and stabilizes. Therefore, one can distinguish the boundaries between the distinct modes through the curve profiles of $\Delta\varphi$ and $x_{m,rms}$. Our results indicate that the occurrence of the motion states of the system depends mainly on the length ratio Lr and Reynolds number Re . The phase diagram for the five modes in the $H-Re$ plane is shown in figure 6. Each symbol in the figure represents a case we simulated. It is seen that the SD mode occurs mainly in the low Re region (say $Re = 10$). As Re increases, the transition from a steady to unsteady state for flow past the coupled system is found at a critical $Re \in (25, 50)$ for $1 \leq Lr < 4$, or $\in (10, 25)$ for $4 \leq Lr \leq 10$. In the moderate Re region (say $Re = 100$), the MV, MFF, PF and CF modes appear in succession as Lr increases from 1.1 to 10; when Re is large enough (say $Re = 800$), only the MV and CF modes occur.

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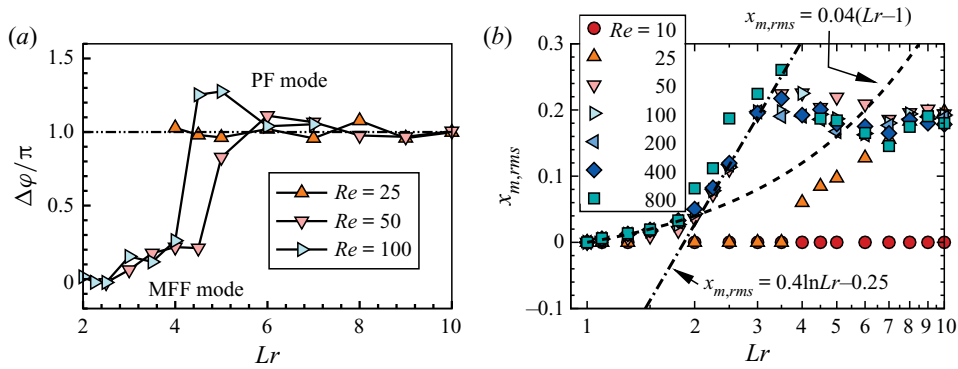


Figure 5. (a) Phase difference between the peaks of C_l and x_m , and (b) the root-mean-square value of the transverse position of the filament midpoint, $x_{m,rms}$, as functions of Lr for various Re .

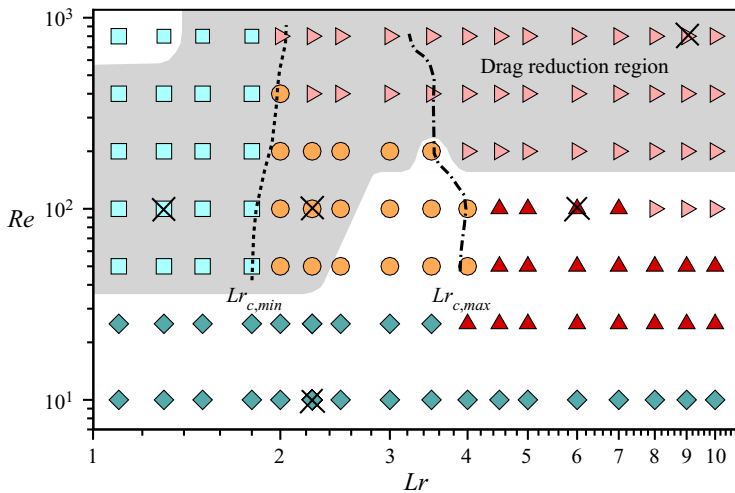


Figure 6. Overview of the five typical mode regions on the Lr - Re plane, where the symbols \diamond , \square , \circ , Δ and \triangleright represent the SD, MV, MF, PF and CF modes, respectively. The drag reduction region (DRR) is marked by the grey colour. The $Lr_{c,max}$ (or $Lr_{c,min}$) trajectory along which the system experiences a local maximum (or minimum) drag is plotted by the dashed (or dash-dotted) line on the phase plane. The typical cases in figure 3 are marked by the symbols \times .

3.2. Drag and the flow characteristics

The drag acting on the coupled system by the surrounding fluid is further investigated to better understand the relationship between the drag variations and the mode transitions. The jump in the fluid force across the plate or filament at a certain Lagrangian point, i.e F_s , can be decomposed into two parts: one is the normal force F^n in which the pressure component dominates, the other is the tangential force F^τ which comes from the viscous effects. These forces are defined as

$$F_s = [-p\mathbf{l} + \mathbf{T}] \cdot \mathbf{n} = F^n + F^\tau = (F_x, F_y), \tag{3.1}$$

$$F^n = (F_s \cdot \mathbf{n}) \cdot \mathbf{n} = (F_x^n, F_y^n), \tag{3.2}$$

$$F^\tau = (F_s \cdot \boldsymbol{\tau}) \cdot \boldsymbol{\tau} = (F_x^\tau, F_y^\tau), \tag{3.3}$$

where \mathbf{I} is the unit tensor, \mathbf{T} the viscous stress tensor, $\boldsymbol{\tau}$ the unit tangential vector, \mathbf{n} the unit normal vector and $[\]$ denotes the jump in a quantity across the immersed boundary. The system experiences a fluid drag in the y direction, i.e. $-F_y = -(F_y^n + F_y^\tau)$. Thus, the corresponding time-averaged drag coefficients are defined as $C_d = -\langle F_y \rangle / \frac{1}{2} \rho U^2 D$, $C_d^n = -\langle F_y^n \rangle / \frac{1}{2} \rho U^2 D$ and $C_d^\tau = -\langle F_y^\tau \rangle / \frac{1}{2} \rho U^2 D$, respectively. Figure 7(a) shows the fluid drag curves versus Lr at different Re for the overall system. Here the drag is normalized by that for the bare plate scenario. It is seen that the drag curves show two distinct tendencies depending on the Re . For the flow at a low Reynolds number (say $Re = 10$ or 25), the drag almost monotonically increases with the increase of Lr . For the higher Reynolds flow (e.g. cases with $Re \geq 50$), the drag first decreases from $C_d/C_{d,Lr=1} = 1$ as Lr increases, and reaches a local minimum at $Lr = L_{r,c,min}$. After that, the drag curve shows a sharp rise until the second threshold at $Lr = L_{r,c,max}$, where the system experiences a local maximum drag. When $Lr > L_{r,c,max}$, the fluid drag generally shows a slow decline as Lr increases. Moreover, we denote the $L_{r,c,min}$ (or $L_{r,c,max}$) trajectory in the Lr - Re plane, as shown in figure 6. It is found that the emergencies of local minimum (or maximum) drags at $L_{c,min} \in [1.8, 2]$ (or $L_{c,max} \in [3.5, 4]$) are often accompanied by the system state transitions. Furthermore, it is interesting to note that benefiting from the passive flow control by using the trailing filament as a deformable afterbody, the system may experience a counterintuitive reduction in fluid drag, corresponding to the scenarios within the grey region ($C_d/C_{d,Lr=1} < 1$) marked in figure 7(a). Compared with the bare plate, the system enjoys a dramatic drag reduction (up to approximately 22%) at $Lr \approx L_{c,min}$ for $Re \geq 50$. The considerable reductions in drag are also observed for cases with large Lr and high Re , e.g. $Lr > 5$ and $Re \geq 400$. As shown in figure 6, we denote the drag reduction region (DRR) in the Lr - Re phase plane for the overall system. The critical value of Re , i.e. Re_c , separating the DRR and drag increase region (DIR) generally depends on Lr . Specifically, $Re_c \in (25, 50)$ for $1 \leq Lr \leq 2$ while $Re_c \in (100, 200)$ for $4 \leq Lr \leq 10$; Re_c increases as the increase of Lr for $2 < Lr < 4$. The DRR almost covers the region with $Re > Re_c$ except for the cases with $Re = 800$, $Lr = 1.1$ and 1.3 . Compared with the experiment (Gao *et al.* 2020) with a higher $Re \sim 2700$ – 5500 , our simulations also show that the counterintuitive drag reduction due to the flow-induced reconfiguration of filament may arise in the low-moderate Re (~ 10 – 10^3) flow region. The experimental data from Gao *et al.* (2020) with $Re = 4400$ which is based on the speed of uniform inflow $U_\infty = 1.54 \text{ m s}^{-1}$ are plotted in figure 7(a). It is worth noting that, although the numerical results are not in perfect agreement with the experimental data (which to some extent is expected given the higher Re flow in the soap film experiments), similar trends in drag variation have been found in the experiments and present simulations; in particular, the $L_{r,c,min}$ (or $L_{r,c,max}$) obtained from the experiment is very close to that from the simulations with $Re \geq 400$ (see figure 7a). The experimental and numerical results have shown together that this kind of device, referred to as a ‘flexible coating’, may have a high level of adaptability and effectiveness for the flow control for reducing drag of the bluff body in a flow.

Further, the drag-reducing effect by using a flexible afterbody is compared with that using a rigid one for the typical cases as listed in table 1. The geometry of a rigid afterbody is represented by the time-averaged shape of a flexible one with identical Lr . It is found that for the cases with $Lr = L_{r,c,min}$ (i.e. cases 1–4), the drag reduction can be achieved by using a flexible or rigid afterbody, whereas the ‘flexible coating’ may give rise to more benefit in drag reduction of the system, especially in the higher Re region considered here, e.g. $Re = 800$ (case 4 in table 1). These facts suggest that suitably adding a flexible coating to a rigid body may lead to additional reduction in drag relative to conventional flow control devices/measures, e.g. rigid splitter plates or other streamlining, in which the FSI effect

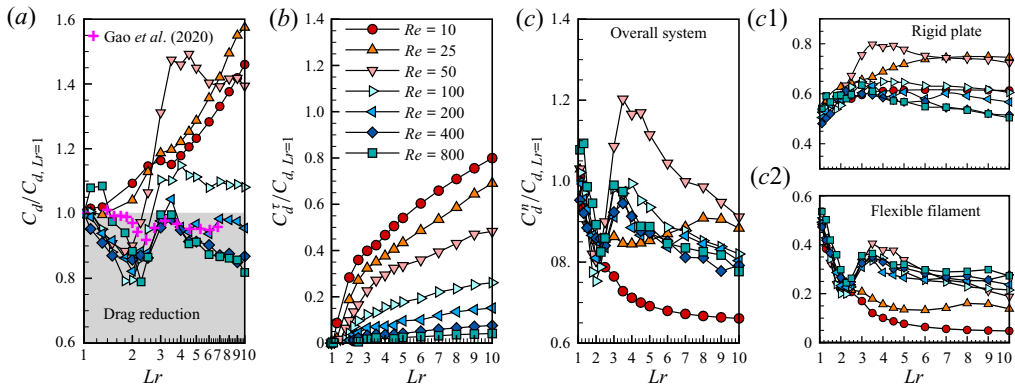


Figure 7. (a) Fluid drag acting on the coupled system normalized by the drag of the isolated rigid plate, i.e. $C_d/C_{d,Lr=1}$ as functions of Lr for various Re . The drag for the system can be decomposed into two parts, i.e. the tangential one $C_d^t/C_{d,Lr=1}$ (b) which comes from the viscous effects, and the normal one $C_d^n/C_{d,Lr=1}$ (c) in which the pressure component dominates. Inset: $C_d^n/C_{d,Lr=1}$ for the rigid plate (c1) and the flexible filament (c2), respectively. For the overall system, $C_d/C_{d,Lr=1} < 1$ corresponds to the drag reduction scenarios, which is located in the grey region in figure 7(a). Also, the experimental data (Gao *et al.* 2020) with $Re = 4400$, which is based on the speed of uniform inflow $U_\infty = 1.54 \text{ m s}^{-1}$, are plotted in figure 7(a).

	Re	$Lr_{c,min}$	Flexible C_d ($C_d/C_{d,Lr=1}$)	Rigid C_d ($C_d/C_{d,Lr=1}$)
Case 1	50	1.8	1.85 (0.885)	1.86 (0.890)
Case 2	100	1.8	1.95 (0.790)	2.05 (0.831)
Case 3	200	2.0	2.15 (0.821)	2.24 (0.855)
Case 4	800	2.25	2.31 (0.789)	2.70 (0.922)
Case 5	100	3.0	2.70 (1.094)	1.98 (0.803)

Table 1. Comparison for the drag coefficients (C_d and $C_d/C_{d,Lr=1}$) of the overall systems with the flexible and rigid afterbodies for typical cases. Here, for cases 1–4, the length ratio $Lr = Lr_{c,min}$, at which the maximum reduction in drag is achieved in the flexible scenarios (see figure 7a). The geometry of a rigid attachment is represented by the time-averaged shape of the flexible afterbody with the identical Lr .

is not included. Moreover, it should be noted that a flexible afterbody may also lead to a larger fluid drag of the overall system compared with a rigid one when Lr is larger, e.g. case 5 in table 1.

Figures 7(b) and 7(c) show the contributions to the total drag from the viscous and pressure stresses for the system, i.e. $C_d^t/C_{d,Lr=1}$ and $C_d^n/C_{d,Lr=1}$, respectively. For the SD mode cases with $Re = 10$, it is seen that, as Lr increases, the friction contribution increases from approximately zero to 0.8, while the pressure contribution reduces from approximately 1 to 0.65. Thus, for the whole system, the form drag predominates at the small Lr , but is no longer the exclusively dominating force at the large Lr , where the skin friction drag cannot be neglected. As Re increases, the friction drag is greatly reduced, e.g. $C_d^t/C_{d,Lr=1} < 0.25$ for $Re \geq 100$, resulting in the form drag predominating in the total drag for high Re cases. Because of this, it is seen from figures 7(a) and 7(c) that the form drag changes with a similar tendency as that of the total drag within the high Re region. We further show the form drag curves at varying Re for the rigid and flexible parts in inset figures 7(c1) and 7(c2), respectively. It is observed that when Lr is close to 1, e.g. $Lr = 1.1$, where the flow pattern is similar to that of the bare plate scenario, the trailing

filament contributes almost the same form drag as the rigid plate, as shown in [figure 7\(c2\)](#). As Lr further increases, the form drag on the filament for all Re cases decreases firstly until the first threshold at $Lr_{c,min}$, where the form drag reduction is up to nearly 30 % in comparison with that at $Lr = 1$. After $Lr > Lr_{c,min}$, the filament experiences the distinct form drag variations for the low Re region (e.g. $Re = 10$) and high Re region (e.g. $Re > 100$), respectively (see [figure 7\(c2\)](#)), which is similar to that for the overall system as shown in [figure 7\(c\)](#). Moreover, it is noted that as Lr increases, small changes in the form drag of the rigid plate are observed at most Re , e.g. $Re = 10$ or ≥ 100 . These facts indicate that the drag reduction for the coupled system is mainly derived from the passive controls for the favourable flow over the flexible trailing filament.

To further explore the underlying mechanisms of the counterintuitive drag reduction behaviour of the coupled system, the corresponding flow characteristics are investigated in the following. [Figure 8](#) shows the time-averaged vorticity and pressure contours around the structures, as well as the vertical component of fluid loads on their surfaces for typical cases. For the isolated plate in the flow, i.e. the case with $Re = 100$ and $Lr = 1$ as shown in [figures 8\(a,e,i\)](#), it is clear in a time-averaged sense that a low-pressure region on the lower surface and a high-pressure region on the upper surface of the plate ([figure 8e](#)), which is induced by the opposite vortex pair ([figure 8a](#)) and the fluid deceleration effect, respectively, dominate nearly the overall drag of the plate ([figure 8i](#)). Unlike the isolated plate case, for the case with $Re = 100$ and $Lr = 2$ in [figure 8\(b,f,j\)](#), the vortex pair is stretched downstream, and the vorticity in the shear layer is mainly distributed on both sides of the filament. This vorticity distribution induces a weakened low-pressure region directly below the filament ([figure 8b,f](#)), leading to an obvious drag reduction ([figure 8j](#)). It is noted that because the flow separation occurs early due to the large reverse pressure gradient near the front outer surface of the filament (see [figure 8f](#)), the contribution of viscous friction to the total drag is negligible in comparison with that of the pressure (see [figure 8j](#)). For the case with $Re = 100$ and $Lr = 3.5$, as shown in [figure 8\(c,g,k\)](#), the filament achieves a more streamlined time-averaged shape by adapting itself to the surrounding fluid, which is helpful for the shear layers attaching to the surfaces ([figure 8c](#)). In this case, as shown in [figure 8\(k\)](#), the fluid drags contributed by the pressure and the friction mainly distribute on the top/bottom and side surfaces of the enclosed loop, respectively; the form drag is still dominant, but the friction drag is no longer negligible. Thus, compared with the bare plate scenario, although the form drag slightly reduces, the total drag increases due to the addition of friction (see [figure 7](#)). For the case with $Re = 10$ and $Lr = 9$, as shown in [figure 8\(d,h,l\)](#), it is seen that unlike the cases discussed above, the filament is subjected to a considerable friction drag and a negligible form drag, owing to its highly streamlined steady deformation. Thus, in this case, the form drag and the friction drag are almost contributed by the rigid plate and the flexible filament, respectively (see [figure 8l](#)).

[Figure 9](#) shows the unsteady behaviours for the typical cases with $Re = 100$, $Lr = 1, 2$ and 3.5 . For the bare plate scenario ($Re = 100$, $Lr = 1$), the shear layers separate at the edges of the flat plate and form a pair of counter-rotating vortices alternately shedding in the wakes (see [figure 9g](#)), which causes the periodic fluctuations in pressure on the lower surface of the plate, as we can see in the curve of $F_y(t)$ (see [figure 9a](#)). From the instantaneous flow field around the plate at instant A, corresponding to the valley in the curve of $F_y(t)$ as shown in [figure 9\(a\)](#), it is clear that the maximum instantaneous drag is attributed to the low-pressure region induced by the vortex which moves just below the plate at instant A, as shown in [figure 9\(d\)](#). For the case with $Re = 100$ and $Lr = 2$, a similar situation is observed in the instantaneous flow field (see [figure 9e](#)) at instant B when the

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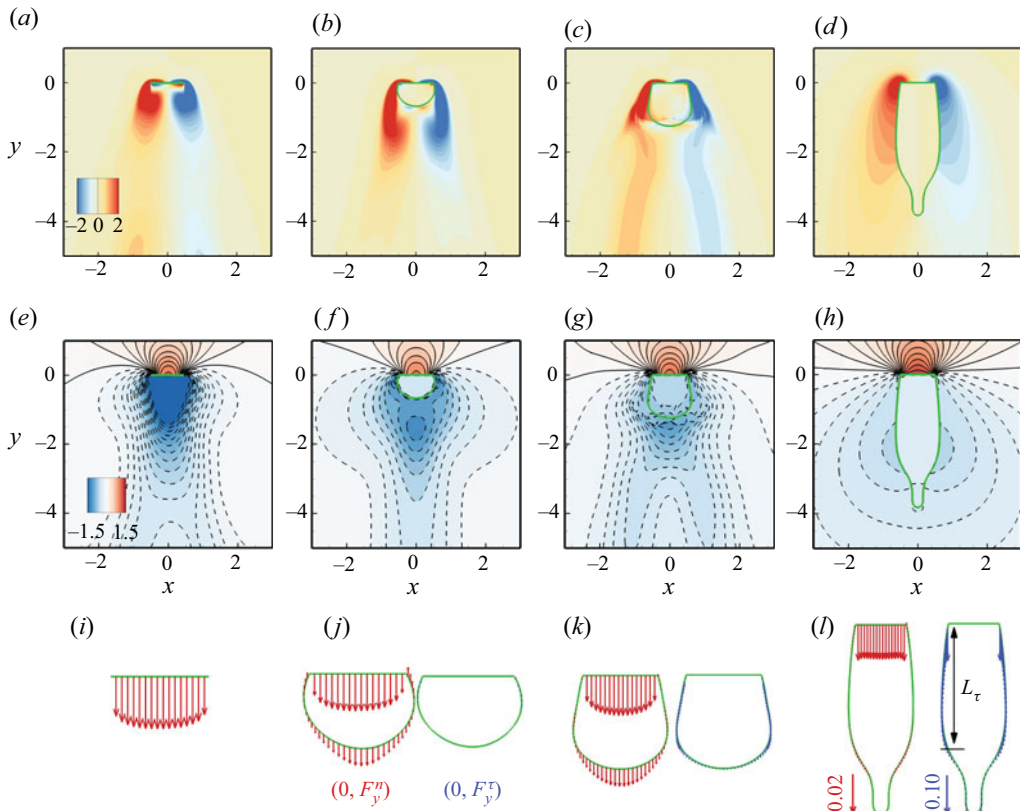


Figure 8. Time-averaged vorticity (a–d) and pressure (e–h) contours around the coupled system, and the distribution of the y component of time-averaged normal and tangential force (i–l) for the typical cases with $Re = 100, Lr = 1$ (a,e,i), 2 (b,f,j), 3.5 (c,g,k) and $Re = 10, Lr = 8$ (d,h,l), respectively. The two vectors, i.e. $(0, F_y^n)$ (red colour) and $(0, F_y^\tau)$ (blue colour), are plotted along the plate and filament, illustrating the spatial distribution of the fluid drags contributed by the pressure and friction, respectively.

maximum instantaneous drag is achieved, as shown in figure 9(b). The difference from the bare plate case is that the moving vortex is weaker and, thus, the induced low-pressure region is weakened, resulting in a smaller drag peak. For the case with $Re = 100$ and $Lr = 3.5$, a dramatic peak is found in the curve of $F_y(t)$ at instant C as shown in figure 9(c). From figure 9(f), we can see that at the trailing end of the afterbody, the local high and low pressure appear on the inner and outer surfaces, respectively, which is responsible for the sharp increase of the drag at instant C. It is also noted that at this moment, the left shear layer with positive vorticity is able to maintain attachment to the reshaped and moving surface (see figures 9f,i), and such attached flow will provide a considerable contribution to friction drag (figure 8k).

From the discussion above, the generation, movement and shedding of vortices around the coupled system play a prominent role in the dynamic characteristics, especially the fluid drag of the system. We further explore the vortex structures in the far field and their relation to changes in drags. For cases with $Re = 100, Lr = 1, 2$ and 3.5, as shown in figure 9(g,h,i), the Kármán vortex streets, associated with the averaged drag force (Griffin & Ramberg 1975; Li & Lu 2012), are observed in wakes. Here, the Kármán vortex street is characterized by the distance between its two staggered rows of vortices, w , the streamwise

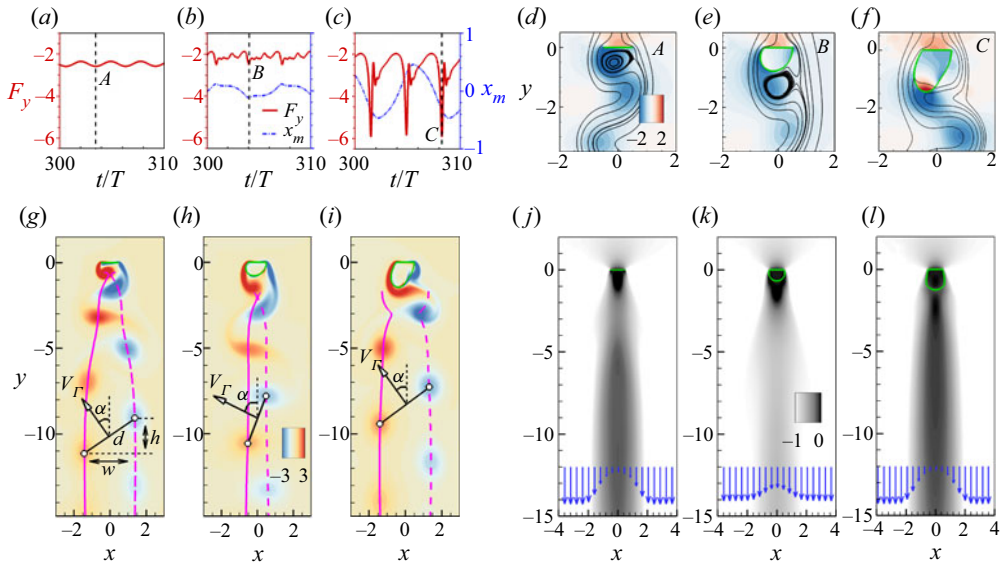


Figure 9. The unsteady behaviours of the coupled system: (a–c) the y component of fluid force for the system, F_y , and the transverse position of the filament midpoint, x_m , as functions of time for $Re = 100$, $Lr = 1$ (a), 2 (b) and 3.5 (c); (d–f) the instantaneous pressure contours and streamlines around the coupled system at instant A for $Re = 100$, $Lr = 1$ (d), instant B for $Re = 100$, $Lr = 2$ (e) and instant C for $Re = 100$, $Lr = 3.5$ (f); (g–i) the instantaneous vortical structures in the far field for $Re = 100$, $Lr = 1$ (g), 2 (h) and 3.5 (i). The paths of the vortex with positive (anticlockwise rotation) and negative (clockwise rotation) circulation are plotted by the solid and dashed lines, respectively. The position of the vortex core is identified by $x_c = \int x\omega_z dS / \int \omega_z dS$ and $y_c = \int y\omega_z dS / \int \omega_z dS$. (j–l) The time-averaged velocity deficit induced by the vortex street in the wake for $Re = 100$, $Lr = 1$ (j), 2 (k) and 3.5 (l). The contours show the magnitude of the time-averaged velocity in the y direction, and the velocity profiles in the far field are also illustrated by the vectors $(0, v)$ at $y = -12$.

separation between the adjacent vortices having opposite rotation, h , and the vortex circulation Γ . The position of the vortex core is defined as $x_c = \int x\omega_z dS / \int \omega_z dS$ and $y_c = \int y\omega_z dS / \int \omega_z dS$. For the system, the averaged drag force is relevant to the reverse jet flow in the vertical direction induced by the vortices. As illustrated in figure 9(g), according to the vortex-dipole model (Godoy-Diana *et al.* 2009), the vertical component of the dipole-induced velocity is

$$V_y^\Gamma = V^\Gamma \cos\alpha = \frac{\Gamma}{2\pi d} \times \cos\alpha = \frac{\Gamma w}{2\pi(w^2 + h^2)}, \quad (3.4)$$

where $\cos\alpha = w/d$ and $d = \sqrt{h^2 + w^2}$. For comparison of three typical cases with $Re = 100$ and $Lr = 1, 2$ and 3.5, the parameters of Kármán vortex streets are given in table 2. It is seen that compared with the bare plate case ($Re = 100$, $Lr = 1$), the vortex street width for the drag reduction case ($Re = 100$, $Lr = 2$) is significantly narrower, which results in a substantial increase of α and decrease of the value of $\cos\alpha$. This would result in a weakened reverse jet flow with a smaller V_y^Γ according to (3.4). However, for the case with $Re = 100$ and $Lr = 3.5$, the enhanced reverse jet flow with larger V_y^Γ , corresponding to the increased drag, is mainly attributed to the more increase of vortex circulation Γ , relative to the less decrease (or increase) of the value of $\cos\alpha$ (or d).

Further, figure 9(j–l) shows the time-averaged vertical velocity contours and velocity profiles in the wake for the three cases. As we can see, the velocity deficit (wake profile), induced by Kármán street with the reverse jet, arises in the far field for all the cases,

	Re	Lr	Γ	w	h	α (deg.)	V_y^Γ
Case 1	100	1	3.77	2.82	1.99	35.3	0.14
Case 2	100	2	4.51	1.04	2.77	69.5	0.085
Case 3	100	3.5	4.50	2.79	2.20	38.3	0.16

Table 2. Parameters of Kármán vortex streets for cases with $Re = 100$ and $Lr = 1, 2$ and 3.5 . Here, Γ , w , h and α are the parameters determined based on the flow field. Here V_y^Γ is calculated by using (3.4).

indicating the onset of net fluid drag acting on the system. Moreover, it is seen that compared with that for the bare plate case ($Re = 100, Lr = 1$), the intensity of reverse jet flow is weakened for the drag reduction case ($Re = 100, Lr = 2$), but enhanced for the drag increase case ($Re = 100, Lr = 3.5$), respectively. And a weakened (or enhanced) reverse jet can be considered as a prognosticator of a further drop (or increase) in drag. These findings indicate that the flexible filament coating to a rigid plate may offer favourable flow controls for the vortex dynamics in the near field and in the far field, which brings in sizable drag reduction for the overall system.

3.3. Drag estimate

In this section the form drag and the friction drag, which come from the pressure and viscous effects, respectively, are further estimated. According to the Blasius solution (Schlichting & Gersten 2016) for the flow along a very thin flat plate, the friction drag on one side of the flat plate $\sim \rho U^2 L_f (UL_f/\nu)^{-1/2}$, where U is free-stream velocity and L_f is the length of the flat plate, indicating that the friction drag is proportional to $U^{3/2}$ and to $L_f^{1/2}$. From the discussion above, it is revealed that the friction drag mainly originates from the attached shear layer on the outer surface of the filament. Therefore, by assuming the friction drag on the filament surface follows the same scaling rule, we have $C_d^\tau \sim (L_\tau/Re)^{1/2}$, where L_τ is the dimensionless characteristic length of the frictional layer scaled by D and $Re = \rho UD/\mu$. Thus, the coefficient of friction drag on the filament can be estimated by

$$C_d^\tau = 2k_\tau \sqrt{\frac{L_\tau}{Re}}, \quad (3.5)$$

where $L_\tau = (Lr - 1)/2$ and k_τ is a dimensionless constant coefficient.

Figure 10(a) shows the variation of C_d^τ as $(L_\tau/Re)^{1/2}$. As we can see, all the data from the present simulations appear to collapse into a straight line described by (3.5) with $k_\tau \approx 1.8$, indicating that the friction drags calculated by (3.5) agree well with the numerical results. It is noted that the constant coefficient k_τ derived from the Blasius solution for the flat plate boundary layer is 1.328, which is smaller than $k_\tau = 1.8$ from the numerical results. One should also note that the Blasius solution with $k_\tau = 1.328$ is only valid in the limit of $Re \gg 1$, which is not the case with low-moderate Re in the present simulation. In spite of this, our numerical results indicate that $(L_\tau/Re)^{1/2}$ may serve as a practicable metric for scaling the friction drags. On the other hand, the form drag arises from the pressure difference on the upper and bottom surfaces of the enclosed system, which is closely related to filament flapping and deformable shape. Thus, the transverse characteristic length of the afterbody is a more important factor than the streamwise length for scaling the form drag. Since the afterbody is subjected to a shape deformation or

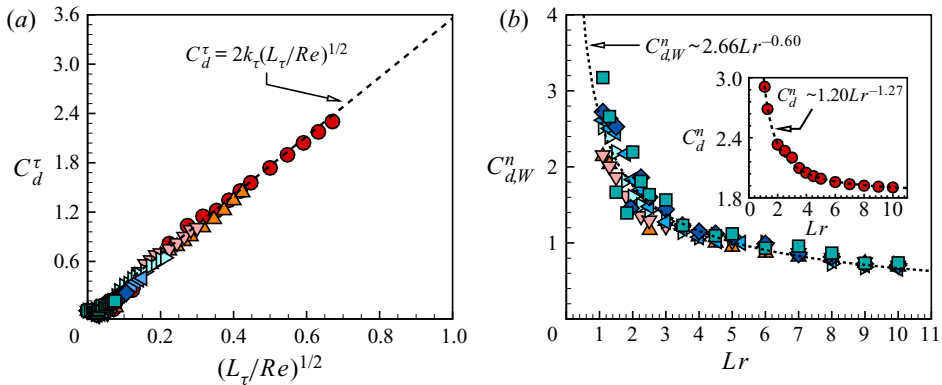


Figure 10. Scaling laws for the friction drag (a) and the form drag (b) acting on the coupled system, which come from viscous effects and pressure differences, respectively. The friction drags C_d^τ and the renormalised form drag $C_{d,W}^n$ are plotted as functions of $(L_\tau/Re)^{1/2}$ and Lr , respectively. A new drag coefficient, $C_{d,W}^n$, is normalised using the maximum width of the afterbody envelope W , instead of D . Inset gives the variation of C_d^n versus Lr for $Re = 10$. Results indicate that the friction drags follow the scaling law of $C_d^\tau \sim (L_\tau/Re)^{1/2}$ for all the Re numbers considered here; while the form drags follow the scaling laws of $C_{d,W}^n \sim Lr^{-0.60}$ for $Re \geq 25$ and $C_d^n \sim Lr^{-1.27}$ for $Re = 10$, respectively. Legend is identical to that in figure 7.

strong flapping for most cases in our simulations, the flat plate width D can not serve as a good characteristic length for scaling the form drag, as shown in figure 7. Therefore, we here adopted the maximum width of the afterbody envelope W as a characteristic length to renormalise the form drag, i.e. $C_{d,W}^n = C_d^n \times 1/W^* = -\langle F_y^n \rangle / \frac{1}{2} \rho U^2 W$, where the dimensionless quantity $W^* = W/D$.

Figure 10(b) shows the variation of $C_{d,W}^n$ versus Lr for $Re \geq 25$. It is shown that the symbols with $Re \geq 25$ appear to collapse nearly into a curve described by $C_{d,W}^n = 2.66Lr^{-0.60}$. It is also noted that the symbols in the large- Lr region (say $Lr > 3$) are closer to the scaling curve than those in the small- Lr region. The results in figure 10(b) suggest that W is a reasonable characteristic length for scaling form drag in flapping regions, especially in large-amplitude flapping regions, i.e. $Lr > 3$ (see figure 4b). While for the static deformation region with $Re = 10$, W is no longer a characteristic length for the form drag. As shown in the inset in figure 10(b), the coefficient C_d^n can be merely described by Lr , i.e. $C_d^n = 1.20Lr^{-1.27} + 1.84$. Thus, the form drag on the system for all the Re numbers considered can be estimated by

$$C_d^n = a \times \frac{W^{*n}}{Lr^b} + c, \quad \text{where} \quad \begin{cases} a = 2.66, b = 0.60, c = 0, n = 1, & \text{if } Re \geq 25, \\ a = 1.20, b = 1.27, c = 1.84, n = 0, & \text{if } Re = 10. \end{cases} \quad (3.6)$$

Finally, the overall drag coefficient can be estimated by

$$C_d' = C_d'^\tau + C_d'^n = 2k_\tau \sqrt{\frac{L_\tau}{Re}} + a \times \frac{W^{*n}}{Lr^b} + c. \quad (3.7)$$

It is noted that for a short afterbody, e.g. $Lr < 3$, the transverse characteristic length is no longer the only dominant metric for scaling drag, and, thus, the deviation of C_d^n estimated is slightly larger, compared with that for a slender afterbody, as shown in figure 10(b). In order to eliminate this error, a correction factor γ based on the drag of a bare rigid plate

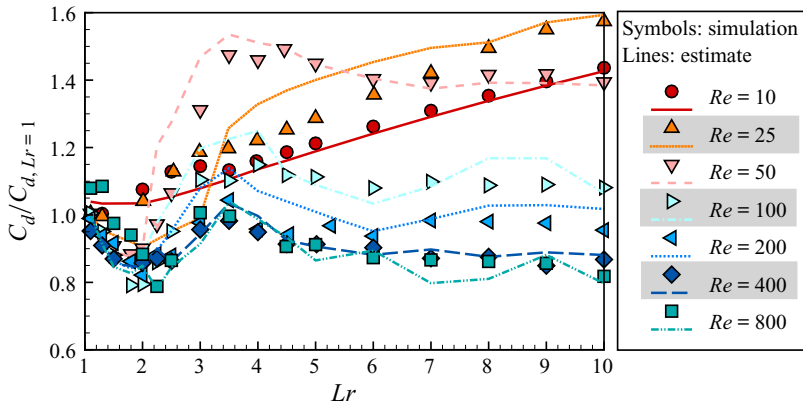


Figure 11. The overall fluid drags $C_d/C_{d,Lr=1}$ as a function of Lr . All the data in figure 7(a) are plotted again in figure 11 with the same symbols, and each curve in figure 11 denotes the estimated drag calculated using (3.8) for each Re , respectively.

is introduced. Therefore, the modified drag estimate formula is expressed by

$$C_d'' = 2k_\tau \sqrt{\frac{L_\tau}{Re}} + \gamma \times \left(a \frac{W^{*n}}{Lr^b} + c \right), \quad (3.8)$$

where $\gamma = C_{d,Lr=1}/C'_{d,Lr=1} = C_{d,Lr=1}/C_{d,Lr=1}$ for $Lr < 3$, and $\gamma = 1$ for $Lr \geq 3$.

Figure 11 shows the variations of $C_d/C_{d,Lr=1}$ as a function of Lr for $Re = 10-800$. All the data in figure 7(a) are plotted again in figure 11 with the same symbols, and each curve in figure 11 denotes the estimated drag calculated using (3.8) for each Re , respectively. It is seen that the estimate curves, which are based on the scaling laws for friction drag and form drag, show a similar tendency to those in the simulations. Moreover, we note that a good degree of agreement between the numerical and estimate data is observed at even high- Re and large- Lr regimes, in which the flow is highly unsteady and the filament flaps strongly. The drag scaling laws proposed here are helpful for understanding the underlying mechanism of the drag variations and may give valuable insight into the dynamics of this type of FSI system.

4. Concluding remarks

In summary, we carried out a numerical investigation on the dynamics of fluid flow past a rigid flat plate with a trailing closed flexible filament acting as a deformable afterbody. We have found the five distinct modes of the system state according to the filament motion and flow pattern, i.e. SD, MV, MFF, PF and CF modes. It was indicated that the occurrence of the system mode depends mainly on Lr and Re . The phase diagram for the typical modes in the $Lr-Re$ plane were plotted.

The drag variations show two distinct tendencies in lower and higher Re regions. For the flow at low Reynolds number, the drag almost monotonically increases with an increase of Lr . While for the higher Reynolds flow, all the $C_d(Lr)$ curves indicate the existence of the local minimum (or maximum) drags at $L_{c,min} \in [1.8, 2]$ (or $L_{c,max} \in [3.5, 4]$). Besides, we also noted that the $L_{c,min}$, or $L_{c,max}$, trajectory generally separates different mode regions in the $Lr-Re$ plane. In other words, as Lr changes, the overall system may reach its local minimum or maximum drag, along with the emergence of state transition. Moreover, it was interesting to note that benefiting from the passive flow control by using the trailing

filament as a deformable afterbody, the system may experience a counterintuitive reduction in fluid drag. Compared with the bare plate, the system enjoys a dramatic drag reduction up to approximately 22%; and the considerable reductions in drag were also observed for cases with large Lr and high Re , e.g. $Lr > 5$ and $Re \geq 400$.

The analysis of time-averaged and instantaneous flow fields shows that drag reduction is mainly attributed to favourable control for the shedding and movement of vortices around the flexible afterbody. The velocity deficit (wake profile) induced by the Kármán vortices arises in the far field, indicating the onset of net fluid drag acting on the system. To explore the relations between drag and vortical wake, the characteristics of Kármán vortex streets in the far field for typical cases are quantitatively described by using w , h and Γ . For the drag reduction case, the vortex street width (w) is significantly narrower and, thus, the strength of the reverse jet is weakened.

The drag decomposition shows that the form drag predominates at the small Lr but is no longer the exclusively dominating force at large Lr , where the skin friction drag cannot be neglected. As Re increases, the friction drag is greatly reduced, resulting in the form drag predominating in the total drag for high Re cases. Finally, the overall drag is estimated based on the scaling laws for the friction drag and the form drag. Our results show that the friction follows a similar scaling rule as that in the Blasius boundary layer, i.e. $C_d^r \sim (L_\tau/Re)^{1/2}$; and the form drag can be scaled by the length ratio, Lr , and the maximum envelope width of the afterbody, W^* , i.e. $C_d^n \sim W^*/Lr^{0.6}$ for $Re \geq 25$ and $C_d^n \sim 1/Lr^{1.27}$ for $Re = 10$.

Although the geometric shape is simplified and the simulation is two dimensional, our preliminary study is still indispensable for understanding the complex dynamics of this new kind of rigid-flexible coupling system. It also inspires a novel flow control method for the aero/hydrodynamic performance enhancement. For example, by suitably adding a flexible coating to a rigid body, some favourable flow features for reducing drag on a two-dimensional bluff body are achieved. Unlike the experiments with the higher $Re \sim 2700\text{--}5500$ (Gao *et al.* 2020), we have performed a series of numerical simulations at the low-moderate $Re \sim 10\text{--}10^3$. Nevertheless, a similar trend in drag variation has been found in the experiments and the present simulations with $Re > 100$. In particular, the locations of the local minimum and maximum drags, i.e. $Lr_{c,min}$ and $Lr_{c,max}$, respectively, are very close for the experiments and simulations with $Re \geq 400$. The results from the experimental (Gao *et al.* 2020) and the present numerical studies have showed together that the counterintuitive drag reduction exists for flows with quite a wide range of Re , which indicate that the passive controls may have high adaptability and effectiveness. However, for three-dimensional bluff bodies in many real-life situations, such as athletes or some vehicles, the vortical flows are essentially three-dimensional and highly turbulent (Park *et al.* 2006). Thus, the two-dimensional simulations with the low-moderate Re in the present study can not represent the three-dimensional situations with high Re . This raises the question of whether the ‘flexible coating’, as a passive flow control device, is still effective for reducing drag on a three-dimensional bluff body. The effects of the three-dimensional body shape and the higher Re on the dynamic behaviour of this new class of system is beyond the scope of the present study but will be a focus of our future research.

Supplementary movies. Supplementary movies are available at <https://doi.org/10.1017/jfm.2022.466>.

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REFERENCES

- ALAMINOS-QUESADA, J. & FERNANDEZ-FERIA, R. 2020 Propulsion of a foil undergoing a flapping undulatory motion from the impulse theory in the linear potential limit. *J. Fluid Mech.* **883**, A19.
- ALBEN, S. 2009 Wake-mediated synchronization and drafting in coupled flags. *J. Fluid Mech.* **641**, 489–496.
- ALBEN, S. & SHELLEY, M.J. 2005 Coherent locomotion as an attracting state for a free flapping body. *Proc. Natl Acad. Sci. USA* **102**, 11163–11166.
- ALBEN, S., SHELLEY, M. & ZHANG, J. 2002 Drag reduction through self-similar bending of a flexible body. *Nature* **420**, 479–481.
- ALON TZEZANA, G. & BREUER, K.S. 2019 Thrust, drag and wake structure in flapping compliant membrane wings. *J. Fluid Mech.* **862**, 871–888.
- ALVARADO, J., COMTET, J., DE LANGRE, E. & HOSOI, A.E. 2017 Nonlinear flow response of soft hair beds. *Nat. Phys.* **13**, 1014–1019.
- ANDERSON, E. & SZEWCZYK, A. 1997 Effects of a splitter plate on the near wake of a circular cylinder in 2 and 3-dimensional flow configurations. *Exp. Fluids* **23**, 161–174.
- BEARMAN, P.W. & HARVEY, J.K. 1993 Control of circular cylinder flow by the use of dimples. *AIAA J.* **31** (10), 1753–1756.
- CHOI, H., JEON, W.-P. & KIM, J. 2008 Control of flow over a bluff body. *Annu. Rev. Fluid Mech.* **40**, 113–139.
- CONNELL, B.S.H. & YUE, D.K.P. 2007 Flapping dynamics of a flag in a uniform stream. *J. Fluid Mech.* **581**, 33–67.
- DENG, J., MAO, X. & XIE, F. 2019 Dynamics of two-dimensional flow around a circular cylinder with flexible filaments attached. *Phys. Rev. E* **100**, 053107.
- DERAKHSHANDEH, J.F. & ALAM, M.D.M. 2019 A review of bluff body wakes. *Ocean Engng* **182**, 475–488.
- DESHPANDE, P.J. & SHARMA, S.D. 2012 Spanwise vortex dislocation in the wake of segmented blunt trailing edge. *J. Fluids Struct.* **34**, 202–217.
- DONG, S., TRIANTAFYLLOU, G.S. & KARNIADAKIS, G.E. 2008 Elimination of vortex streets in bluff-body flows. *Phys. Rev. Lett.* **100** (20), 204501.
- DOWELL, E.H. & HALL, K.C. 2001 Modeling of fluid-structure interaction. *Annu. Rev. Fluid Mech.* **33** (1), 445–490.
- DOYLE, J.F. 2001 *Nonlinear Analysis of Thin-Walled Structures: Statics, Dynamics, and Stability*. Springer.
- ELDRIDGE, J.D. & JONES, A.R. 2019 Leading-edge vortices: mechanics and modeling. *Annu. Rev. Fluid Mech.* **51**, 75–104.
- FAN, D., YANG, L., WANG, Z., TRIANTAFYLLOU, M.S. & KARNIADAKIS, G.E. 2020 Reinforcement learning for bluff body active flow control in experiments and simulations. *Proc. Natl Acad. Sci.* **117** (42), 26091–26098.
- FAVIER, J., DAUPTAIN, A., BASSO, D. & BOTTARO, A. 2009 Passive separation control using a self-adaptive hairy coating. *J. Fluid Mech.* **627**, 451–483.
- FORD, C.W.P. & BABINSKY, H. 2013 Lift and the leading-edge vortex. *J. Fluid Mech.* **720**, 280–313.
- GAO, S., PAN, S., WANG, H.C. & TIAN, X.L. 2020 Shape deformation and drag variation of a coupled rigid-flexible system in a flowing soap film. *Phys. Rev. Lett.* **125** (3), 034502.
- GILLIÉRON, P. & KOURTA, A. 2010 Aerodynamic drag reduction by vertical splitter plates. *Exp. Fluids* **48** (1), 1–16.
- GLEZER, A. & AMITAY, M. 2002 Synthetic jets. *Annu. Rev. Fluid Mech.* **34** (1), 503–529.
- GODOY-DIANA, R., MARAIS, C., AIDER, J.-L. & WESFREID, J.E. 2009 A model for the symmetry breaking of the reverse Bénard–von Kármán vortex street produced by a flapping foil. *J. Fluid Mech.* **622**, 23–32.
- GOLDSTEIN, D., HANDLER, R. & SIROVICH, L. 1993 Modeling a no-slip flow boundary with an external force field. *J. Comput. Phys.* **105** (2), 354–366.
- GOVARDHAN, R.N. & WILLIAMSON, C.H.K. 2005 Vortex-induced vibrations of a sphere. *J. Fluid Mech.* **531**, 11–47.
- GRIFFIN, O.M. & RAMBERG, S.E. 1975 On vortex strength and drag in bluff-body wakes. *J. Fluid Mech.* **69** (4), 721–728.
- GRIFFITH, B.E. & PATANKAR, N.A. 2020 Immersed methods for fluid–structure interaction. *Annu. Rev. Fluid Mech.* **52**, 421–448.
- GUO, Z.L., ZHENG, C.G. & SHI, B.C. 2002 Discrete lattice effects on forcing terms in the lattice Boltzmann method. *Phys. Rev. E* **65**, 046308.

- HUA, R.-N., ZHU, L. & LU, X.-Y. 2013 Locomotion of a flapping flexible plate. *Phys. Fluids* **25**, 121901.
- HUA, R.-N., ZHU, L. & LU, X.-Y. 2014 Dynamics of fluid flow over a circular flexible plate. *J. Fluid Mech.* **759**, 56–72.
- JUNG, S., MARECK, K., SHELLEY, M. & ZHANG, J. 2006 Dynamics of a deformable body in a fast flowing soap film. *Phys. Rev. Lett.* **97**, 134502.
- KANG, C.-K., AONO, H., CESNIK, C.E.S. & SHYY, W. 2011 Effects of flexibility on the aerodynamic performance of flapping wings. *J. Fluid Mech.* **689**, 32–74.
- KIM, B., HUANG, W.-X., SHIN, S.J. & SUNG, H.J. 2012 Flexible ring flapping in a uniform flow. *J. Fluid Mech.* **707**, 129–149.
- LĀCIS, U., BROSSE, N., INGREMEAU, F., MAZZINO, A., LUNDELL, F., KELLAY, H. & BAGHERI, S. 2014 Passive appendages generate drift through symmetry breaking. *Nat. Commun.* **5** (1), 5310.
- LECLERCQ, T. & DE LANGRE, E. 2018 Reconfiguration of elastic blades in oscillatory flow. *J. Fluid Mech.* **838**, 606–630.
- LI, Z., CHEN, Y., CHANG, S. & LUO, H. 2019 A reduced-order flow model for fluid–structure interaction simulation of vocal fold vibration. *J. Biomech. Engng* **142** (2), 021005.
- LI, G.-J. & LU, X.-Y. 2012 Force and power of flapping plates in a fluid. *J. Fluid Mech.* **712**, 598–613.
- LIGHTHILL, M.J. 1975 *Mathematical Biofluidynamics*, vol. 17. SIAM.
- LIU, G., REN, Y., DONG, H., AKANYETI, O., LIAO, J.C. & LAUDER, G.V. 2017 Computational analysis of vortex dynamics and performance enhancement due to body–fin and fin–fin interactions in fish-like locomotion. *J. Fluid Mech.* **829**, 65–88.
- MAZAHERI, K. & EBRAHIMI, A. 2010 Experimental investigation of the effect of chordwise flexibility on the aerodynamics of flapping wings in hovering flight. *J. Fluids Struct.* **26** (4), 544–558.
- MICHELIN, S. & SMITH, S.G.L. 2009 Resonance and propulsion performance of a heaving flexible wing. *Phys. Fluids* **21**, 071902.
- MITTAL, R. & IACCARINO, G. 2005 Immersed boundary methods. *Annu. Rev. Fluid Mech.* **37**, 239–261.
- MÜLLER, U.K., VAN DEN HEUVEL, B.L.E., STAMHUIS, E.J. & VIDELER, J.J. 1997 Fish foot prints: morphology and energetics of the wake behind a continuously swimming mullet (*Chelon labrosus* Risso). *J. Expl Biol.* **200**, 2893–2906.
- NAKATA, T., LIU, H., TANAKA, Y., NISHIHASHI, N., WANG, X. & SATO, A. 2011 Aerodynamics of a bio-inspired flexible flapping-wing micro air vehicle. *Bioinspir. Biomim.* **6** (4), 045002.
- NAUG, J.C. & LAUDER, G.V. 2002 Hydrodynamics of caudal fin locomotion by chub mackerel, *Scomber japonicus* (scombridae). *J. Expl Biol.* **205**, 1709–1724.
- NIU, J. & HU, D.L. 2011 Drag reduction of a hairy disk. *Phys. Fluids* **23**, 101701.
- PALKIN, E., HADŽIABDIĆ, M., MULLYADZHANOV, R. & HANJALIĆ, K. 2018 Control of flow around a cylinder by rotary oscillations at a high subcritical Reynolds number. *J. Fluid Mech.* **855**, 236–266.
- PARK, H., LEE, D., JEON, W.-P., HAHN, S., KIM, J., KIM, J., CHOI, J. & CHOI, H. 2006 Drag reduction in flow over a two-dimensional bluff body with a blunt trailing edge using a new passive device. *J. Fluid Mech.* **563**, 389–414.
- PENG, Z.-R., HUANG, H. & LU, X.-Y. 2018a Collective locomotion of two closely spaced self-propelled flapping plates. *J. Fluid Mech.* **849**, 1068–1095.
- PENG, Z.-R., HUANG, H. & LU, X.-Y. 2018b Collective locomotion of two self-propelled flapping plates with different propulsive capacities. *Phys. Fluids* **30** (11), 111901.
- PENG, Z.-R., HUANG, H. & LU, X.-Y. 2018c Hydrodynamic schooling of multiple self-propelled flapping plates. *J. Fluid Mech.* **853**, 587–600.
- PESKIN, C.S. 2002 The immersed boundary method. *Acta Numerica* **11**, 479–517.
- PRASANTH, T.K. & MITTAL, S. 2008 Vortex-induced vibrations of a circular cylinder at low Reynolds numbers. *J. Fluid Mech.* **594**, 463–491.
- RAISSI, M., WANG, Z., TRIANTAFYLLOU, M.S. & KARNIADAKIS, G.E. 2019 Deep learning of vortex-induced vibrations. *J. Fluid Mech.* **861**, 119–137.
- RAJAMUNI, M.M., THOMPSON, M.C. & HOURIGAN, K. 2018 Transverse flow-induced vibrations of a sphere. *J. Fluid Mech.* **837**, 931–966.
- SCHATZMAN, D., WILSON, J., ARAD, E., SEIFERT, A. & SHTENDEL, T. 2014 Drag-reduction mechanisms of suction-and-oscillatory-blowing flow control. *AIAA J.* **52** (11), 2491–2505.
- SCHLICHTING, H. & GERSTEN, K. 2016 *Boundary-Layer Theory*. Springer.
- SCHOUVEILER, L. & ELOY, C. 2013 Flow-induced draping. *Phys. Rev. Lett.* **111**, 064301.
- SHOELE, K. & MITTAL, R. 2016 Energy harvesting by flow-induced flutter in a simple model of an inverted piezoelectric flag. *J. Fluid Mech.* **790**, 582–606.
- SHOELE, K. & ZHU, Q. 2010 Flow-induced vibrations of a deformable ring. *J. Fluid Mech.* **650**, 343–362.

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- SHYY, W., KANG, C.-K., CHIRARATTANANON, P., RAVI, S. & LIU, H. 2016 Aerodynamics, sensing and control of insect-scale flapping-wing flight. *Proc. Math. Phys. Engng Sci.* **472** (2186), 20150712.
- SUNIL, P., KUMAR, S. & PODDAR, K. 2022 Flow past a rotationally oscillating cylinder with an attached flexible filament. *J. Fluid Mech.* **930**, A3.
- TIAN, F.-B., LUO, H., ZHU, L. & LU, X.-Y. 2010 Interaction between a flexible filament and a downstream rigid body. *Phys. Rev. E* **82** (2), 026301.
- TRIANTAFYLLOU, M.S., TRIANTAFYLLOU, G.S. & YUE, D.K.P. 2000 Hydrodynamics of fishlike swimming. *Annu. Rev. Fluid Mech.* **32** (1), 33–53.
- WANG, W., HUANG, H. & LU, X.-Y. 2020 Optimal chordwise stiffness distribution for self-propelled heaving flexible plates. *Phys. Fluids* **32**, 111905.
- WILLIAMSON, C.H.K. & GOVARDHAN, R. 2004 Vortex-induced vibrations. *Annu. Rev. Fluid Mech.* **36**, 413–455.
- WU, T.Y.-T. 1961 Swimming of a waving plate. *J. Fluid Mech.* **10**, 321–344.
- WU, T.Y.-T. 1971 Hydromechanics of swimming of fishes and cetaceans. In *Advances in Applied Mechanics*, vol. 11, pp. 1–63. Elsevier.
- WU, J., QIU, Y.L., SHU, C. & ZHAO, N. 2014 Flow control of a circular cylinder by using an attached flexible filament. *Phys. Fluids* **26**, 103601.
- YANG, Y. & STRGANAC, T.W. 2013 Experiments of vortex-induced torsional oscillation of a flat plate in cross flow. *AIAA J.* **51** (6), 1522–1526.
- YE, H., WEI, H., HUANG, H. & LU, X.-Y. 2017 Two tandem flexible loops in a viscous flow. *Phys. Fluids* **29** (2), 021902.
- ZHAO, M. 2021 *Bluff Body Overflow and Drag Reduction Control*, pp. 57–88. Springer.
- ZHU, X., HE, G. & ZHANG, X. 2014 How flexibility affects the wake symmetry properties of a self-propelled plunging foil. *J. Fluid Mech.* **751**, 164–183.