



Corrigendum: A certain structure of Artin groups and the isomorphism conjecture

S.K. Roushon

DOI: <https://doi.org/10.4153/S0008414X2000036X>. Published by Cambridge University Press, 21 May 2020.

Abstract. In this note, we give an alternate proof of the Farrell–Jones isomorphism conjecture for the affine Artin groups of type \tilde{B}_n .

In [4], Flechsig pointed out an error in [6, Proposition 4.1], which was needed to deduce the Farrell–Jones isomorphism conjecture for the affine Artin groups $\mathcal{A}_{\tilde{B}_n}$ ($n \geq 3$) of type \tilde{B}_n .

In this note, we give an alternate argument to prove the conjecture.

Theorem 0.1 *The Farrell–Jones isomorphism conjecture wreath product with finite groups (FICwF) is true for $\mathcal{A}_{\tilde{B}_n}$ ($n \geq 3$).*

Proof Consider the following hyperplane arrangement complement.

$$W = \{w \in \mathbb{C}^n \mid w_i \neq \pm w_j, \text{ for all } i \neq j; w_k \neq \pm 1, \text{ for all } k\}.$$

In [2, Section 3], the following homeomorphism was observed. Let $\mathbb{C}^* = \mathbb{C} - \{0\}$.

$$\begin{aligned} \mathbb{C}^* \times W &\simeq X := \{x \in \mathbb{C}^{n+1} \mid x_i \neq \pm x_j, \text{ for all } i \neq j; x_1 \neq 0\}. \\ (\lambda, w_1, w_2, \dots, w_n) &\mapsto (\lambda, \lambda w_1, \dots, \lambda w_n). \end{aligned}$$

In [2, Lemma 3.1], it was then proved that the hyperplane arrangement complement X is simplicial, in the sense of [3].

From [5], it follows that *FICwF* is true for $\pi_1(X)$, since X is a finite real simplicial arrangement complement. Hence, *FICwF* is true for $\pi_1(W)$, as $\pi_1(W)$ is a subgroup of $\pi_1(X)$ and *FICwF* has hereditary property (see [6]).

Next, note that there are the following two finite sheeted orbifold covering maps:

$$\begin{aligned} W &\rightarrow PB_n(Z) := \{z \in Z^n \mid z_i \neq z_j, \text{ for all } i \neq j\} \\ (w_1, w_2, \dots, w_n) &\mapsto (w_1^2, w_2^2, \dots, w_n^2) \end{aligned}$$

Received by the editors August 10, 2023; accepted February 19, 2024.

Published online on Cambridge Core February 23, 2024.

AMS subject classification: 19B99, 19G24, 20F36, 57R67, 57N37.

Keywords: Artin group, isomorphism conjecture, Whitehead group, reduced projective class group, surgery obstruction group, Waldhausen A-theory.



and $PB_n(Z) \rightarrow B_n(Z) := PB_n(Z)/S_n$. Here, $Z = \mathbb{C}(1, 1; 2)$ (see [6]) is the orbifold whose underlying space is $\mathbb{C} - \{1\}$, and 0 is an order 2 cone point. And, the symmetric group S_n is acting on $PB_n(Z)$ by permuting coordinates.

Therefore, $\pi_1(W)$ embeds in $\pi_1^{orb}(B_n(Z))$ as a finite index subgroup. Hence, $FICwF$ is true for $\pi_1^{orb}(B_n(Z))$, since $FICwF$ passes to finite index overgroups (see [6]). Next, recall that in [1] Allcock showed that $\mathcal{A}_{\tilde{B}_n}$ is isomorphic to a subgroup of $\pi_1^{orb}(B_n(Z))$, and hence $FICwF$ is true for $\mathcal{A}_{\tilde{B}_n}$ by the hereditary property of $FICwF$. ■

References

- [1] D. Allcock, *Braid pictures of Artin groups*. Trans. Amer. Math. Soc. 354(2002), no. 9, 3455–3474.
- [2] F. Callegaro, D. Moroni, and M. Salvetti, *The $K(\pi, 1)$ problem for the affine Artin group of type \tilde{B}_n and its cohomology*. J. Eur. Math. Soc. (JEMS) 12(2010), 1–22.
- [3] P. Deligne, *Les immeubles des groupes de tresses généralisés*. Invent. Math. 17(1972), 273–302.
- [4] J. Flechsig, *Braid groups and mapping class groups for 2-orbifolds*. Preprint, 2023, arXiv:2305.04273.
- [5] J. Huang and D. Osajda, *Helly meets Garside and Artin*. Invent. Math. 225(2021), no. 2, 395–426.
- [6] S. K. Roushon, *A certain structure of Artin groups and the isomorphism conjecture*. Canad. J. Math. 73(2021), no. 4, 1153–1170.

School of Mathematics, Tata Institute, Homi Bhabha Road, Mumbai, India

e-mail: roushon@math.tifr.res.in