



RESEARCH ARTICLE

# Metrology for sub-Rayleigh-length target positioning in $\sim 10^{22}$ W/cm<sup>2</sup> laser–plasma experiments

E. A. Vishnyakov<sup>1</sup>, A. Sagisaka<sup>2</sup>, K. Ogura<sup>2</sup>, T. Zh. Esirkepov<sup>2</sup>, B. Gonzalez-Izquierdo<sup>2</sup>, C. D. Armstrong<sup>3</sup>, T. A. Pikuz<sup>4</sup>, S. A. Pikuz<sup>5</sup>, W. Yan<sup>6,7</sup>, T. M. Jeong<sup>1</sup>, S. Singh<sup>8,9</sup>, P. Hadjisolomou<sup>1</sup>, O. Finke<sup>1</sup>, G. M. Grittani<sup>1</sup>, M. Nevrkla<sup>1,10</sup>, C. M. Lazzarini<sup>1,10</sup>, A. Velyhan<sup>1</sup>, T. Hayakawa<sup>2,11</sup>, Y. Fukuda<sup>12</sup>, J. K. Koga<sup>12</sup>, M. Ishino<sup>2</sup>, K. Kondo<sup>2</sup>, Y. Miyasaka<sup>2</sup>, A. Kon<sup>12</sup>, M. Nishikino<sup>2</sup>, Y. V. Nosach<sup>12</sup>, D. Khikhlukha<sup>1</sup>, I. P. Tsygvintsev<sup>13</sup>, D. Kumar<sup>1</sup>, J. Nejd<sup>1,10</sup>, D. Margarone<sup>1</sup>, P. V. Sasorov<sup>1</sup>, S. Weber<sup>1</sup>, M. Kando<sup>2</sup>, H. Kiriya<sup>12</sup>, Y. Kato, G. Korn<sup>1</sup>, K. Kondo<sup>2</sup>, S. V. Bulanov<sup>1,2</sup>, T. Kawachi<sup>12</sup>, and A. S. Pirozhkov<sup>12</sup>

<sup>1</sup>ELI Beamlines Facility, The Extreme Light Infrastructure ERIC, Dolní Břežany, Czech Republic

<sup>2</sup>Kansai Institute for Photon Science (KPSI), QST, Kyoto, Japan

<sup>3</sup>Central Laser Facility, Rutherford Appleton Laboratory, STFC, Harwell Oxford, Didcot, UK

<sup>4</sup>Institute for Open and Transdisciplinary Research Initiatives, Osaka University, Osaka, Japan

<sup>5</sup>HB11 Energy Holdings, Freshwater, Australia

<sup>6</sup>Key Laboratory for Laser Plasmas (Ministry of Education), School of Physics and Astronomy, Shanghai Jiao Tong University, Shanghai, China

<sup>7</sup>Collaborative Innovation Center of IFSA, Shanghai Jiao Tong University, Shanghai, China

<sup>8</sup>Institute of Plasma Physics ASCR, Prague, Czech Republic

<sup>9</sup>FZU – Institute of Physics ASCR, Prague, Czech Republic

<sup>10</sup>Czech Technical University in Prague, FNSPE, Prague, Czech Republic

<sup>11</sup>Institute of Laser Engineering, Osaka University, Osaka, Japan

<sup>12</sup>Institute of Physics, National Academy of Sciences of Ukraine, Kyiv, Ukraine

<sup>13</sup>ISTEQ AR, Yerevan, Armenia

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## Abstract

Tight focusing with very small  $f$ -numbers is necessary to achieve the highest at-focus irradiances. However, tight focusing imposes strong demands on precise target positioning in-focus to achieve the highest on-target irradiance. We describe several near-infrared, visible, ultraviolet and soft and hard X-ray diagnostics employed in a  $\sim 10^{22}$  W/cm<sup>2</sup> laser–plasma experiment. We used nearly 10 J total energy femtosecond laser pulses focused into an approximately 1.3- $\mu$ m focal spot on 5–20  $\mu$ m thick stainless-steel targets. We discuss the applicability of these diagnostics to determine the best in-focus target position with approximately 5  $\mu$ m accuracy (i.e., around half of the short Rayleigh length) and show that several diagnostics (in particular,  $3\omega$  reflection and on-axis hard X-rays) can ensure this accuracy. We demonstrated target positioning within several micrometers from the focus, ensuring over 80% of the ideal peak laser intensity on-target. Our approach is relatively fast (it requires 10–20 laser shots) and does not rely on the coincidence of low-power and high-power focal planes.

**Keywords:** laser–plasma interaction; precise target positioning; spectroscopy; ultra-high intensity; X-rays

## 1. Introduction

Contemporary high-intensity femtosecond laser facilities that are based on the chirped pulse amplification (CPA) concept<sup>[1]</sup> now reach subterawatt<sup>[2]</sup>, multi-terawatt<sup>[3–12]</sup> and petawatt<sup>[13–20]</sup> power levels, with a rapid increase in their

Correspondence to: E. A. Vishnyakov, The Extreme Light Infrastructure ERIC, Za Radnicí 835, 25241 Dolní Břežany, Czech Republic. Email: [eugene.vishnyakov@eli-beams.eu](mailto:eugene.vishnyakov@eli-beams.eu); A. S. Pirozhkov, Kansai Institute for Photon Science (KPSI), QST, 8-1-7 Umemidai, Kizugawa, 619-0215 Kyoto, Japan. Email: [pirozhkov.alexander@qst.go.jp](mailto:pirozhkov.alexander@qst.go.jp)

number worldwide<sup>[21–23]</sup>. Most of the high-power systems are near-infrared (NIR) facilities taking advantage of Ti:sapphire lasers, while others operate in the mid-IR<sup>[2]</sup> or visible<sup>[9,10]</sup> spectral ranges. In certain cases, two-color lasers<sup>[11]</sup> are advantageous for high-intensity laser–matter interaction experiments.

Tight focusing of intense femtosecond laser pulses into diffraction-limited focal spots or spots with high Strehl ratios  $S \geq 0.5$  and small effective radii  $r_{\text{eff}} \sim 1 \mu\text{m}$  enables the transition of the laser–matter interaction to substantially relativistic regimes<sup>[24]</sup>. One of the important parameters in the interaction processes is the peak laser intensity on-target  $I_0 = a_0^2 \times 1.37 \times 10^{18} \text{ W/cm}^2 \times (\lambda/\mu\text{m})^{-2}$ , where  $\lambda$  represents the laser wavelength and  $a_0$  is a normalized vector-potential of the laser field–electron interaction. Relativistic regimes correspond to  $a_0 > 1$ .

Most of the existing high-intensity experiments have been carried out at laser intensities from  $I_0 \sim 10^{18}$  to  $10^{21} \text{ W/cm}^2$  (from  $a_0 \sim 1$  to 30), and only a few at  $I_0 > 10^{21} \text{ W/cm}^2$ <sup>[25–33]</sup>. New regimes of laser–matter interaction require intensities  $I_0 \sim 10^{22} \text{ W/cm}^2$  and higher, leading to efficient radiation-pressure-dominant ion acceleration at  $I_0 > 10^{22} \text{ W/cm}^2$ <sup>[34,35]</sup>, radiation damping at  $I_0 > 3 \times 10^{23} (\mu\text{m}/\lambda)^{4/3} \text{ W/cm}^2$ <sup>[24]</sup> and quantum electrodynamic effects at  $I_0 > 6 \times 10^{24} \text{ W/cm}^2$ <sup>[36]</sup>. A distant goal is reaching the intensities of  $I_0 > 10^{26} \text{ W/cm}^2$  required for optically induced vacuum breakdown<sup>[37]</sup>. Recently, an intensity of  $I_0 > 10^{23} \text{ W/cm}^2$  has been experimentally demonstrated<sup>[38]</sup>. Advancing laser fields to these numbers requires comprehensive control of the spatial and temporal envelope of the laser pulses<sup>[8,39]</sup>, as well as placing the target within an extremely short Rayleigh length ( $\sim 10 \mu\text{m}$  in our case), which is a consequence of using high-aperture focusing mirrors with small  $f$ -numbers to attain focal spots with  $r_{\text{eff}} \sim \lambda$ . It is worth mentioning that laser–gas interactions are largely negatively affected by the focal-spot imperfections<sup>[40–42]</sup>, while laser–solid interactions are strongly influenced by laser pre-pulses and pedestals producing pre-plasmas on different timescales<sup>[43,44]</sup>.

Common methods for target positioning include, for example, shadowgraphy, retro-focusing and direct observation of the rear side of a solid target<sup>[45–47]</sup>. However, in the case of relatively wide and smooth mirror-like reflective tape targets, shadowgraphy cannot ensure target positioning with an accuracy of better than a few tens of micrometers<sup>[47]</sup>. At the same time, techniques for direct observation of the target surface are most advantageous in the case of single-shot experiments or while operating low-repetition-rate laser systems that typically deliver up to several full-power shots per hour<sup>[47]</sup>. In our case of 0.1-Hz laser operation, direct observation of the target surface for the precise target placement would be more time-consuming than using 10–20 full-power laser shots to find the best focus. The techniques we present in our paper can be used in experiments using laser systems with high repetition rates of 0.1–10 Hz, such as ALEPH<sup>[48]</sup>

in Colorado, Astra Gemini<sup>[49]</sup> in the UK, Apollon<sup>[50]</sup> in France, ATLAS 3000 and PFS<sup>[51]</sup> in Munich, BELLA<sup>[39]</sup> in Berkeley, CoReLS<sup>[17]</sup> in Republic of Korea, Diocles<sup>[52]</sup> in Nebraska-Lincoln, DRACO<sup>[53]</sup> in Dresden, HAPLS<sup>[54,55]</sup> at ELI-Beamlines in the Czech Republic, HERCULES<sup>[4]</sup> in Michigan, HF-PW at ELI-ALPS<sup>[56]</sup> in Hungary, HPLS<sup>[19,20]</sup> at ELI-NP in Romania, SCAPA<sup>[57]</sup> at the University of Strathclyde in Glasgow, SULF<sup>[31]</sup> in China, VEGA<sup>[58,59]</sup> in Spain, as well as commercial PULSAR laser systems in Canada<sup>[60]</sup>, Italy<sup>[61]</sup> and China<sup>[62]</sup>.

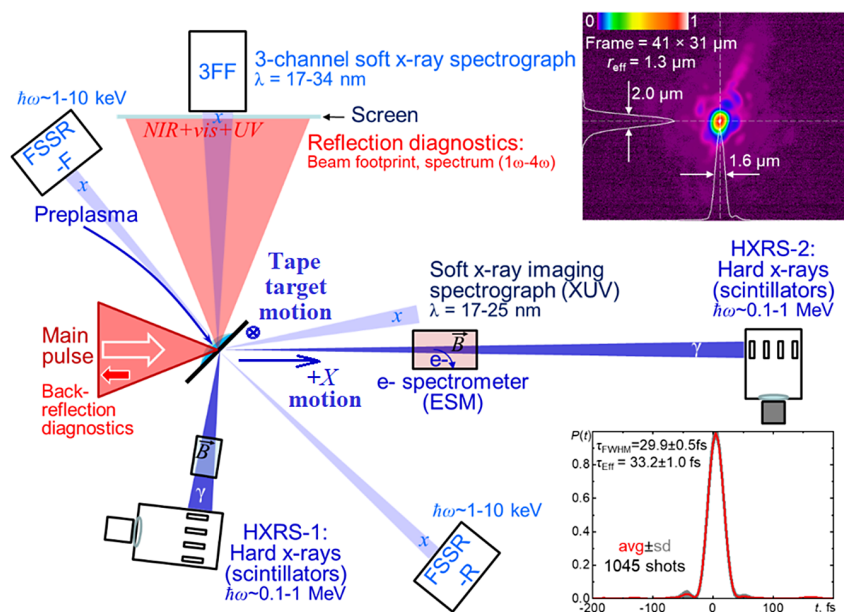
As the laser intensity at-focus is tremendously high, direct observation of the focal spot is difficult during the experiment. The focal spot can be measured prior to the experiment by attenuating the high-power laser beam after the amplifiers with the aid of wedges<sup>[8]</sup> or low-reflectivity mirrors<sup>[38]</sup> with a controlled surface quality. However, when the focal spot is small and of high quality, positioning the target within the Rayleigh length becomes non-trivial, since the Rayleigh length is approximately  $10 \mu\text{m}$  for a typical  $1\text{-}\mu\text{m}$  focal spot and a wavelength of  $0.8 \mu\text{m}$ .

Here we describe our approach to control the tight laser focusing on-target using several diagnostics during the target position scan. We show that about 10–20 full-power laser shots were required to determine the best position of the target with an accuracy of approximately  $5 \mu\text{m}$ , after which we immediately started collecting data at the best in-focus target position, with no reliance on the long-term laser stability and regardless of the long-term thermal drifts, as well as without any requirements on the focal planes for the low-power and high-power shots to be coincident. The diagnostic instruments employed here covered the IR, visible, extreme ultraviolet (XUV) and X-ray spectral ranges, observing the corresponding radiation from both the front and rear sides of the target. We report on the design of the experimental setup, the methods we used and the applicability of the diagnostics for target positioning, including the dependence on the target thickness. We demonstrate target positioning within several micrometers out of the best focus, ensuring over 80% of the ideal peak laser intensity.

## 2. Experimental setup

The experiment was carried out in the Short-F target chamber of the J-KAREN-P laser facility<sup>[7,8]</sup> at KPSI, Japan. The p-polarized laser pulses with a central wavelength of  $\lambda_0 \sim 820 \text{ nm}$ , duration of 33 fs and energy up to 12 J were focused with an  $f/1.3$  off-axis parabolic (OAP) mirror with a  $45^\circ$  deviation angle into a focal spot with an effective radius  $r_{\text{eff}} \sim 1.3 \mu\text{m}$ . The laser operated at 0.1 Hz, delivering typically several hundred full-power shots per experimental day.

The top right inset in Figure 1 shows the focal-spot profile recorded with the amplified pulse at approximately 10% of the full laser power attenuated by means of wedges<sup>[8]</sup>. We have also recorded the full-power focal-spot profile using



**Figure 1.** Experimental scheme (not to scale). The J-KAREN-P laser pulses ( $\varnothing$  280 mm, 33 fs, 10 J,  $\lambda_0 \sim 820$  nm, p-polarized) were focused into an  $r_{\text{eff}} \sim 1.3 \mu\text{m}$  focal spot on a 5–20  $\mu\text{m}$  stainless-steel tape target<sup>[26]</sup> mounted at a  $45^\circ$  incident angle. The observation direction of the back-reflection diagnostics at  $1\omega$  is shown by the red arrow. Several reflection diagnostics ( $1\omega$  and  $2\omega$  imagers,  $1\omega$ – $4\omega$  fiber spectrometer) measured the reflected beam footprint on a screen mounted perpendicular to the ‘specular reflection’ direction; a three-channel flat-field XUV spectrograph (3FF) was mounted behind a hole in the screen. The first hard X-ray spectrometer, HXRS-1, was mounted  $98^\circ$  off the main laser pulse direction. The second hard X-ray spectrometer, HXRS-2, and an electron spectrometer (ESM) were along the direction of the main laser pulse, while the imaging XUV spectrograph was  $12^\circ$  off this direction. The  $\vec{B}$  symbols represent dipole magnets removing electrons from HXRS-1 and HXRS-2 and dispersing electrons in the electron spectrometer ESM. Two soft X-ray spectrometers with spatial resolution (FSSR) were mounted out-of-plane on the target front (-F) and rear (-R) sides, respectively. The insets show spatial and temporal J-KAREN-P laser pulse profiles. A tape target of 20 mm width was mounted on a double-rotating-reel setup, which could be translated linearly along the laser axis with a  $0.1\text{-}\mu\text{m}$  step size (the ‘+X’ denotes direction away from the OAP mirror).

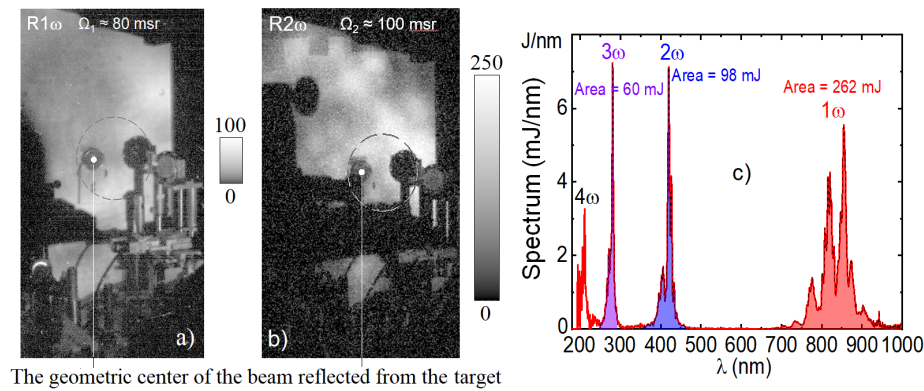
on-shot far-field measurements through a high-reflectivity, high-optical-quality mirror. Both approaches provided fully consistent results. The on-shot pulse spectrum and near-field profiles were also measured using a portion of the beam transmitted through this mirror. The full setup used for spectral measurements (including the mirror, wedges, filters, integrating sphere, fiber and spectrometer) was absolutely calibrated using the measured spectrum and the pulse energy after the OAP mirror. We found that the pulse energy determined by integrating this absolutely calibrated spectrum is more precise than the one obtained from the near-field profile, because the calibration factor of the near-field profile depends on the spectrum of the pulse and, thus, can vary day-to-day and even shot-to-shot.

The temporal laser pulse shape (Figure 1, bottom inset), with an effective width<sup>[8]</sup> of 33 fs, was measured with a commercial self-referenced spectral interferometry device (Wizzler)<sup>[63]</sup> at approximately 10% of the maximum laser power. In a separate experiment we confirmed that this method gave the same pulse duration as the full-power measurements<sup>[64]</sup>. The resulting peak intensity in-vacuum was up to  $7 \times 10^{21}$  W/cm<sup>2</sup>. The experiments presented herein were performed in a ‘medium contrast mode’ with an approximately  $10^{-10}$  nanosecond laser contrast level, which was optimized for hard X-ray generation. The temporal shape of the pre-pulse at the nanosecond timescale was also measured

on-shot by a fast photodiode. We have performed hydrodynamic simulations, showing that under our conditions, the pre-plasma scale length was a few micrometers and thus did not affect the optimum target position significantly, although it did affect the interaction physics. The small pre-plasma scale length can be proved indirectly by the fact that the pre-plasma was not visible on the  $2\omega$  interferometer, as it was completely inside the target shadow. The generation of high-order harmonics (HOHs) in the ‘specular reflection’ direction, which was detected by the three-channel flat-field (3FF) XUV spectrograph and is described in Section 7, also indicates a small pre-plasma scale length. More details on the laser contrast, pre-plasma, and physics of the hard X-ray generation will be presented elsewhere.

Figure 1 shows the experimental scheme: the main laser pulse, the 5-to-20- $\mu\text{m}$ -thick stainless-steel (SUS) tape target<sup>[26]</sup> mounted  $45^\circ$  off-normal and the diagnostics discussed herein:

- (front) reflected beam footprint diagnostics (at frequencies  $1\omega$ ,  $2\omega$  and  $3\omega$ );
- (front) back-reflection diagnostics (at  $1\omega$ , the diagnostics are outside Figure 1);
- (rear) XUV imaging spectrograph for wavelengths 17–25 nm;



The geometric center of the beam reflected from the target

**Figure 2.** The fields of view of the  $1\omega$  (a) and  $2\omega$  (b) cameras imaging a PTFE screen mounted perpendicular to the ‘specular reflection’ direction. The geometric center of the reflected beam is marked with white circles. The dashed ellipses denote the spectrometer observation area. (c) Typical absolutely calibrated reflected spectrum. The energy values calculated within the  $(n \pm 0.25)\omega_0$  spectral bandwidths (colored) are given for harmonic orders  $n = 1, 2, 3$ .

- (rear) magnetic electron spectrometer (ESM) for 20–100 MeV electrons;
- (rear) two hard X-ray spectrometers (HXRS-1 and HXRS-2) for 0.1–10 MeV photons;
- (front and rear) two soft X-ray focusing spectrometers with spatial resolution (FSSR-F (front) and FSSR-R (rear)) for 0.7–10 keV photons;
- (front) 3FF XUV spectrograph,  $\lambda = 17\text{--}34$  nm.

Here (front) and (rear) correspond to the observation on the front and rear sides of the target, respectively. In the latter case, the radiation was going through the target or was generated directly on its rear side.

As electromagnetic pulses (EMPs) from high-power laser-plasma interaction are known to cause problems in electronics<sup>[65]</sup>, we made attempts to minimize their influence. In previous experiments we tried different motorized platforms from several companies and, finally, we found that Kohzu Precision can produce custom motorized stages and control electronics that are highly resistant to EMPs. In particular, these stages were used in our experiments for 3D target translations and rotations. EMPs did not affect our tape movement, as its control system was relatively simple and robust. At the same time, some computers and cameras related to a few diagnostics were affected by the EMPs from time to time, and had to be restarted.

Before each experiment, the initial position of the tape target was determined with an approximately 100  $\mu\text{m}$  accuracy as follows. We used a focal-spot monitor consisting of an apochromatic objective lens and a high-dynamic-range charge-coupled device (CCD) camera and set a micro-needle to mark the desired focus position. The needle was positioned by illuminating it with a  $\lambda = 785$  nm alignment beam (LD7 in Figure 2 of Ref. [8]) with an axial accuracy of a few  $\mu\text{m}$ , limited by the objective depth-of-focus. Then the focal-spot quality was measured as described in Ref. [8]. In this process, the OAP mirror was adjusted to bring the

focus to the needle position, with a typical axial accuracy of better than  $\pm 5$   $\mu\text{m}$ , which was around a half of the Rayleigh length. Up to this point, all the positioning steps were implemented with a few-to-several- $\mu\text{m}$  accuracy.

Then, an SUS tape target of 20-mm width was set to the needle position. We tried several methods (see the Appendix), but we were not able to control the target position with a better than 100- $\mu\text{m}$  accuracy, since the SUS target was mirror-like reflective, wrinkle-free and non-transparent. Finally, we marked the position of the needle on the camera of a  $2\omega$  interferometer<sup>[66]</sup>, which observed the target along its 20-mm-long side. After removing the needle, the target orientation was adjusted by the target rotation stage to the narrowest shadow on the  $2\omega$  interferometer camera, so the tape was along the probe beam with an approximately  $0.1^\circ$  accuracy (therefore, the incidence angle was  $45^\circ$ ). After that, the target was placed at the needle position with an accuracy determined by smearing of the tape image along the observation direction, caused by the defocused images of the  $\pm 10$  mm tape edges, as well as the possible bending of the target edges, which was small in our case on the 100- $\mu\text{m}$  scale, but may be not negligible on the required sub-10- $\mu\text{m}$  scale. From this initial position, the target was shifted by 200  $\mu\text{m}$  towards the OAP mirror (the negative direction in the figures). Then we irradiated the target with high-power laser pulses, performing a target position scan with 10  $\mu\text{m}$  (sometimes 5  $\mu\text{m}$ ) steps. We note that the shot-to-shot target position variations along the laser axis were less than the depth-of-focus of the focal-spot monitor objective lens ( $< 2$   $\mu\text{m}$ ), and the short-term laser pointing stability was approximately 2–3  $\mu\text{rad}$ , which did not affect the focusing. We stopped the scan after passing the optimum position determined consistently with several X-ray and optical diagnostics. Comparison of the final target position with the initial one determined by the interferometer revealed that the initial target position accuracy was around 50  $\mu\text{m}$ .

Hereafter we describe each of the diagnostics listed above (Figure 1). For convenience, the results of all the diagnostics

are given in the same section as their description. The applicability of each instrument for determination of the best in-focus target position is discussed.

### 3. Front-side near-infrared to visible-ultraviolet reflection diagnostics

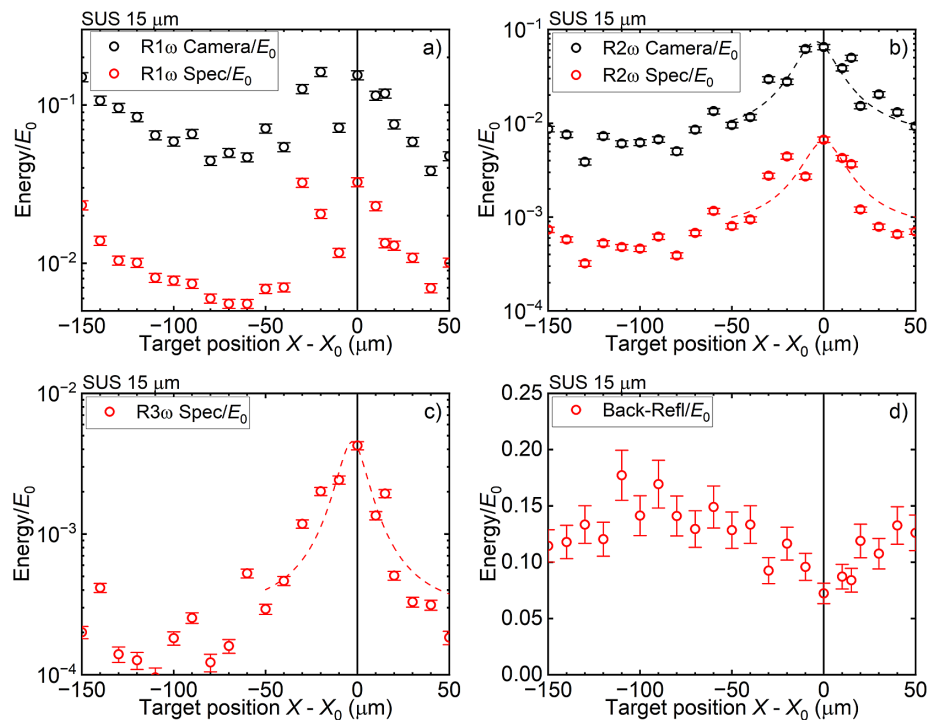
Several NIR-to-ultraviolet (UV) diagnostics<sup>[67–69]</sup> were mounted in the ‘specular reflection’ direction ( $90^\circ$  from the laser incidence direction). Two imaging cameras observed the spatial distributions of  $1\omega$  ( $\sim 700$ – $1000$  nm) and  $2\omega$  ( $\sim 390$ – $410$  nm) radiation scattered from a polytetrafluoroethylene (PTFE; Teflon) screen mounted in the ‘specular reflection’ direction of the laser pulses (see Figure 1). The spectrum of the reflected beam was measured using the same PTFE screen, with a NIR-vis-UV optical fiber spectrometer ( $1\omega$ – $4\omega$ ) having 200–1000 nm total spectral bandwidth.

The fields of view of the two cameras, partially clipped by other instruments, are shown in Figures 2(a) and 2(b). The acceptance angles were  $\Omega_1 \approx 80$  msr and  $\Omega_2 \approx 100$  msr for the  $1\omega$  and  $2\omega$  cameras, respectively. The absolute sensitivity of the  $1\omega$  camera together with its filters was calibrated using a small portion of the main laser beam, resulting in  $(7.1 \pm 1.5) \times 10^{-7}$  J/count. The absolute sensitivity of the spectrometer with a relatively calibrated spectral response was

cross-calibrated with the  $1\omega$  camera, providing an absolute calibration reference for the whole 200–1000 nm spectral region. The  $2\omega$  camera was afterwards cross-calibrated with the spectrometer. The area observed with the spectrometer (dashed ellipses in Figures 2(a) and 2(b)) had an acceptance angle of  $\Omega_s \approx 8$  msr. A typical spectrum is shown in Figure 2(c). The absolute energies could be determined for the first to third harmonics within the corresponding spectral ranges of  $(n \pm 0.25)\omega_0$ , where  $n$  is the harmonic order. The spectrometer had low sensitivity in the  $\lambda < 200$  nm spectral region, and its sensitivity calibration was unreliable there, as we used two types of commercial calibrated light sources (namely, a black-body source and a deuterium-tungsten halogen lamp) with calibration data given in the spectral range of  $\lambda > 200$  nm. Thus, we did not consider the fourth harmonic signal for the target positioning goals.

Along with the ‘specular reflection’ diagnostics, we also used  $1\omega$  back-reflection beam diagnostics. The main purpose of the back-reflection diagnostics is laser safety, as a significant portion of the laser energy can be back-reflected and consequently damage the compressor gratings and/or laser amplifiers. However, this instrument could potentially be useful for determining the best focus position in certain cases.

Figure 3 shows the normalized energy (with respect to the total pulse energy on-target) detected with all the



**Figure 3.** Normalized energy from the four reflection beam diagnostics versus the target position  $X$  (‘-’ denotes the direction towards the OAP mirror, and  $X_0$  corresponds to the best focus position). All values are normalized by the on-target pulse energy  $E_0$ . The plots in (a) and (b) are for the  $1\omega$  and  $2\omega$  diagnostics, respectively, where the upper data (black) are from the imagers, while the lower data (red) are integrated from the  $1\omega$ – $4\omega$  spectrometer within  $(1 \pm 0.25)\omega_0$  and  $(2 \pm 0.25)\omega_0$ , correspondingly. (c) The  $3\omega$  data integrated within the  $(3 \pm 0.25)\omega_0$  band from the  $1\omega$ – $4\omega$  spectrometer. (d) The normalized back-reflected energy.

NIR-vis-UV reflection diagnostics, including the  $1\omega$  (Figure 3(a)) and  $2\omega$  (Figure 3(b)) imagers,  $1\omega$ – $4\omega$  spectrometer (Figures 3(a)–3(c)) and the  $1\omega$  back-reflection (Figure 3(d)), recorded for the scanned target position. Here  $X_0$  represents the best focus position, which was consistently determined by multiple diagnostics for each SUS thickness, as described in detail in Section 9. Thus,  $X - X_0$  denotes the SUS target displacement from the best focus position.

Figure 3(a) shows normalized energy determined from the  $1\omega$  ‘specular reflection’ diagnostics, both the  $1\omega$  imager and spectrometer signal within the  $(1 \pm 0.25)\omega_0$  band. The data from both instruments were in good correlation. There was a double-peak structure in the vicinity of the best focus and a gradual signal increase from both diagnostics towards  $X - X_0 \sim -150 \mu\text{m}$ , as the interaction probably entered the highly reflective plasma mirror regime. These multi-peak features made the  $1\omega$  diagnostics not useful for determination of the best target position.

Figure 3(b) shows the dependence of the  $2\omega$  normalized energy on  $X - X_0$ , determined from the  $2\omega$  imager (upper points) and spectrometer signal within the  $(2 \pm 0.25)\omega_0$  band (lower points). Both cases reveal single-peak structures that can be approximated with Lorentzian fits, giving the best focus position with approximately  $4 \mu\text{m}$  discrepancy and  $24 \mu\text{m}$  full width at half maximum (FWHM), indicating that  $2\omega$  ‘specular reflection’ diagnostics determine the best focus position with an approximately  $12 \mu\text{m}$  accuracy.

Figure 3(c) depicts the energy of the  $3\omega$  radiation determined from the  $1\omega$ – $4\omega$  spectrometer via integration within the  $(3 \pm 0.25)\omega_0$  spectral band. In the  $3\omega$  case, the peak was even more prominent, with small data point fluctuations, indicating an approximately  $5 \mu\text{m}$  target position accuracy.

Figure 3(d) shows the dependence of the normalized back-reflected energy on the relative target position, revealing a broad dip, instead of a peak at the  $X_0$  position, and a broad peak at  $X - X_0 \approx -100 \mu\text{m}$ . Thus, the  $1\omega$  back-reflection, along with other  $1\omega$  reflection diagnostics, was not suitable for determination of the best focus position.

#### 4. Rear-side extreme ultraviolet spectrograph and electron spectrometer

Behind the target, three diagnostics were placed: an XUV imaging spectrograph, an ESM and HXRS-2. In this section we describe the first two instruments, while HXRS-2 will be discussed in the next section, along with the HXRS-1 diagnostics of the same type.

##### 4.1. XUV imaging spectrograph

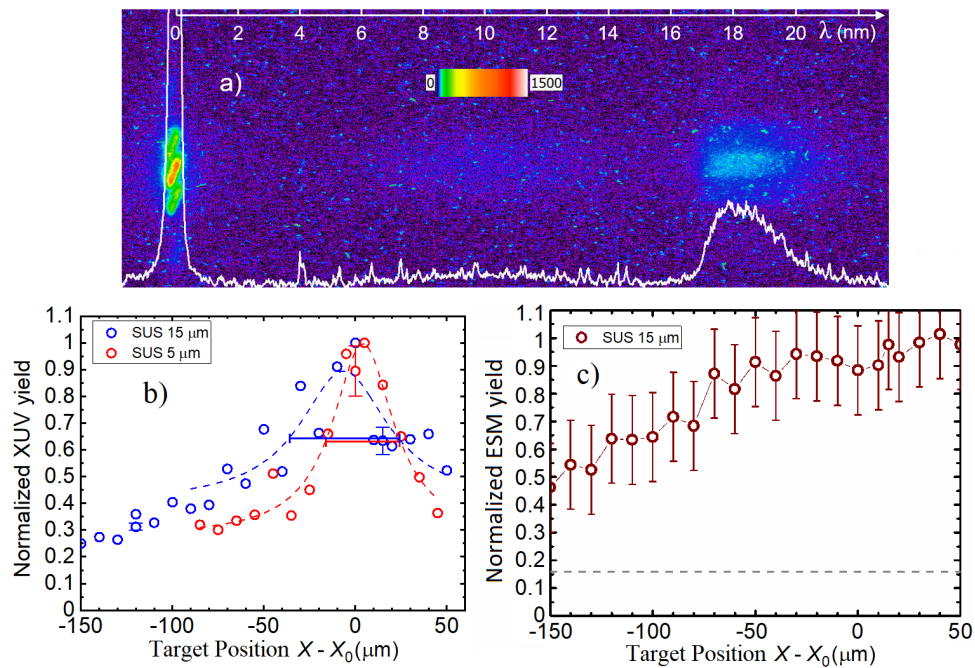
An XUV imaging spectrograph based on a Mo/Si aperiodic multilayer mirror (MM)<sup>[70–72]</sup> and a transmission diffraction grating was mounted  $12^\circ$  off the laser direction. The XUV acceptance angle was  $3.6 \text{ msr}$ , corresponding to an

approximately  $2^\circ$  cone half-angle. The operating range,  $17$ – $25 \text{ nm}$ , was defined by the multilayer structure optimized for maximum uniform reflectance in the  $12.5$ – $25 \text{ nm}$  range<sup>[73,74]</sup> and absorption cutoff at the aluminum  $L_{2,3}$  edge at  $\lambda \approx 17 \text{ nm}$  in the optical blocking filters. Imaging spectrographs of this type are used in different forms, for example in the combination of an MM with a transmission grating<sup>[75]</sup> or a varied line space (VLS) reflection grating<sup>[76,77]</sup>. Such XUV spectrographs have been employed in experiments on coherent soft X-ray generation via frequency upshift of the laser pulse reflected from a relativistic ‘flying mirror’<sup>[78]</sup> and via the BISER mechanism<sup>[41]</sup>.

A spherical aperiodic Mo/Si MM with a radius of curvature of  $R = 1000 \text{ mm}$  was mounted in a geometry providing  $M \approx 2.1$  spatial magnification. We used two Al-based free-standing absorption filters to block the NIR-vis-UV radiation: the first filter ( $0.65 \mu\text{m}$  thick Al) was mounted in front of the mirror and operated in the double-pass regime, while the second filter (Al/Zr multilayer<sup>[79]</sup>,  $0.2 \mu\text{m}$ ) was in front of the CCD. A free-standing transmission diffraction grating with a groove density of  $5000 \text{ lines/mm}$  was situated  $139 \text{ mm}$  from the CCD chip.

Figure 4(a) shows a typical XUV spectrum for a  $5\text{-}\mu\text{m}$ -thick SUS target close to the best focus position ( $X_0$ ). The XUV spectrum contained the zeroth diffraction order and a spectrally resolved continuous first diffraction order in the  $17$ – $22 \text{ nm}$  spectral region. The zeroth diffraction order was triple-shaped due to diffraction on the grating support structure, which was perpendicular to the dispersion direction. Each spot in the zeroth diffraction order image was elongated due to the astigmatism introduced by the spherical focusing MM operating at a small, but non-zero, incidence angle. The spectrum decay at  $\lambda > 20 \text{ nm}$  was due to absorption of the Al/Zr multilayer filter<sup>[79]</sup>. Taking the typical CCD spectral sensitivity<sup>[80,81]</sup> and the spectral filter transmission into account, the total XUV radiation yield on the target rear side was estimated to be approximately  $(26 \pm 3) \times 10^{-10} \text{ J/sr}$  for the  $5\text{-}\mu\text{m}$ -thick SUS target and  $(3.8 \pm 0.8) \times 10^{-10} \text{ J/sr}$  for the  $15\text{-}\mu\text{m}$ -thick SUS target.

The integrated yields in the zeroth and the first diffraction orders were proportional, with a higher signal-to-noise ratio in the zeroth order. Figure 4(b) gives the dependence of the normalized integrated zeroth order signal on  $X - X_0$  for  $5$  and  $15 \mu\text{m}$  target thicknesses. The Lorentzian-fit curves show that the target thickness affected the precision of the target positioning:  $60 \mu\text{m}$  FWHM for the  $15\text{-}\mu\text{m}$ -thick target and a narrower  $40 \mu\text{m}$  FWHM for the  $5\text{-}\mu\text{m}$ -thick target. Deviations of the fitted peaks from the optimal target position were within approximately  $5 \mu\text{m}$  for both thicknesses, meaning that the XUV imaging spectrograph provided target positioning with an approximately  $20$ – $30 \mu\text{m}$  accuracy for  $5$ -to- $15\text{-}\mu\text{m}$  targets. For  $20\text{-}\mu\text{m}$  targets, the XUV signal-to-noise ratio was lower than unity, so precise target positioning was not achievable. The vertical error bars in Figure 4(b)



**Figure 4.** (a) Typical spatially resolved XUV spectrum;  $\lambda = 0$  denotes the zeroth diffraction order. (b) Dependence of the integrated zeroth order on the target position ( $-$  is towards the OAP mirror) for 5- $\mu\text{m}$ - and 15- $\mu\text{m}$ -thick targets, and their Lorentzian fits. (c) Dependence of the integrated ESM yield on the target position for a 15- $\mu\text{m}$ -thick target. The dashed line shows the ESM noise level.

represent solely statistical errors due to shot-to-shot signal variations.

#### 4.2. Electron spectrometer

The magnetic ESM was mounted on the laser axis (Figure 1) 509  $\pm$  1 mm from the target. The spectrometer consisted of a 3-mm-diameter collimator, a 100-mm-long dipole magnet with 0.95 T magnetic field, a 150-mm-long LANEX screen and an optical camera with a camera lens and a green spectral filter. The ESM covered the 20–100 MeV energy range.

The dependence of the ESM signal on  $X - X_0$  for a 15- $\mu\text{m}$ -thick target is shown in Figure 4(c); similar dependences were observed for all target thicknesses under study. The ESM signal had a broad sloped plateau within  $\pm 60$   $\mu\text{m}$  from the best focus, with a not-so-pronounced peak at  $X = +40$   $\mu\text{m}$ , making this instrument not suitable for precise target positioning.

### 5. Rear-side hard X-ray spectrometers (HXRS-1 and HXRS-2)

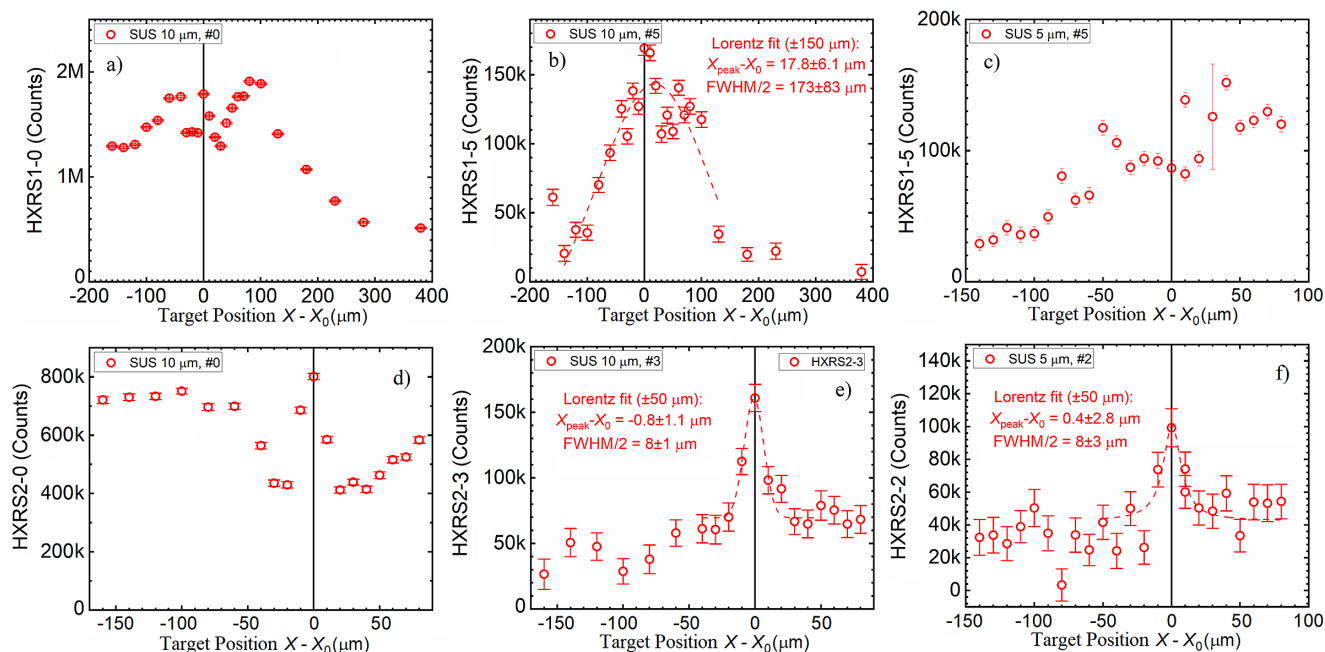
Two HXRSs<sup>[82,83]</sup> were mounted behind the target (Figure 1): HXRS-1 was 98° from the laser axis, approximately along the laser electric field direction, 1.7 m from the target, and HXRS-2 was on the laser axis, behind the ESM, 4.2 m from the target.

Each of the two HXRS instruments consisted of a linear X-ray absorption array built of 10 LYSO ( $\text{Lu}_{1.8}\text{Y}_{0.2}\text{SiO}_5$ ) scintillator crystal plates of 2 mm thickness and 10 mm  $\times$  30 mm area, with 2-mm-thick tungsten filters between each

pair of plates from #4 to #9 (the numeration of the plates starts from #0). The fluorescence emitted from the LYSO array was monitored with a complementary metal oxide semiconductor (CMOS) camera. Dipole magnets (Figure 1) in front of the HXRSs prevented electrons from reaching the instruments. The scintillator sensitivity allowed for registering hard X-ray radiation with the photon energies from approximately 20 keV to 10 MeV, the best sensitivity being 0.1–2 MeV. The harder X-ray radiation was detected by deeper scintillators with higher numbers in the array. A full description of the HXRS design and data processing is given in Ref. [84]. In our setup the plate #9 signal was unreliable as, in addition to the X-rays coming through the other scintillators and tungsten filters in the array, its response included X-rays reflected from the walls of the experimental area. This did not affect other scintillators due to the surrounding lead shielding.

Figure 5 presents data from HXRS-1 (top) and HXRS-2 (bottom). The scintillator plate number in the array is shown next to the instrument name. The thicker the target, the stronger the recorded HXRS signal was. Figures 5(a) and 5(d) show typical scintillator plate #0 dependences for both instruments, exemplified by dependences for 10- $\mu\text{m}$ -thick targets. The plots contain multi-peak structures, making this channel unsuitable for precise target positioning, although the central peak might be attributed to the best target position.

Figures 5(b) and 5(e) show middle scintillator plate signals for 10- $\mu\text{m}$ -thick targets for HXRS-1 and HXRS-2, respectively. The middle plates were most reliable for thick



**Figure 5.** HXRS scintillator plate signals versus target position  $X$  ( $-$  is towards the OAP mirror,  $X_0$  is the best focus). (a)–(c) HXRS-1 (off-axis), (d)–(f) HXRS-2 (on-axis). (a) HXRS-1 plate #0, 10- $\mu\text{m}$ -thick SUS. (b) HXRS-1 plate #5, 10- $\mu\text{m}$ -thick SUS. (c) HXRS-1 plate #5, 5- $\mu\text{m}$ -thick SUS. (d) HXRS-2 plate #0, 10- $\mu\text{m}$ -thick SUS. (e) HXRS-2 plate #3, 10- $\mu\text{m}$ -thick SUS. (f) HXRS-2 plate #2, 5- $\mu\text{m}$ -thick SUS. Lorentzian fits are shown, where applicable. Scintillator plate #0 was the closest to the interaction point. The error bars in all the frames are due to the CMOS camera noise.

target positioning due to high signal-to-noise ratios and single peaks in the dependences. There was a narrow peak for the on-axis HXRS-2 (Figure 5(e), 16  $\mu\text{m}$  FWHM fit), and a broad peak for the off-axis HXRS-1 (Figure 5(b),  $>300$   $\mu\text{m}$  FWHM). This shows that the target positioning precision was approximately 5  $\mu\text{m}$  for the on-axis HXRS-2, while it was more than 100  $\mu\text{m}$  for the off-axis HXRS-1.

Even with the thinnest 5- $\mu\text{m}$  SUS target, the on-axis HXRS-2 middle scintillators were still capable of positioning the target with an approximately 5  $\mu\text{m}$  accuracy (Figure 5(f)), although with a lower signal-to-noise ratio than for thicker targets. The off-axis HXRS-1 middle scintillators were not applicable for determining the best in-focus position of 5- $\mu\text{m}$  SUS targets (Figure 5(c)).

## 6. Front-side and rear-side soft X-ray focusing spectrometers with spatial resolution

Two soft X-ray FSSRs have been assembled on both the front (FSSR-F) and rear (FSSR-R) target sides. The FSSRs were based on spherically bent mica and quartz crystals, respectively ( $2d = 2.36$   $\text{\AA}$  in the latter case) with a curvature radius of  $R = 150$  mm to ensure radiation focusing and high spectral resolution, up to an approximately  $10^4$  value<sup>[85–87]</sup>.

The FSSR instruments were mounted out-of-plane, 786 and 819 mm above the horizontal plane containing the laser axis for the FSSR-F and FSSR-R instruments, respectively. FSSR-F was mounted at an in-plane angle of  $8.5^\circ \pm 0.1^\circ$  from the target normal and an out-of-plane angle of  $17.6^\circ \pm 0.1^\circ$ , with a distance from the FSSR-F

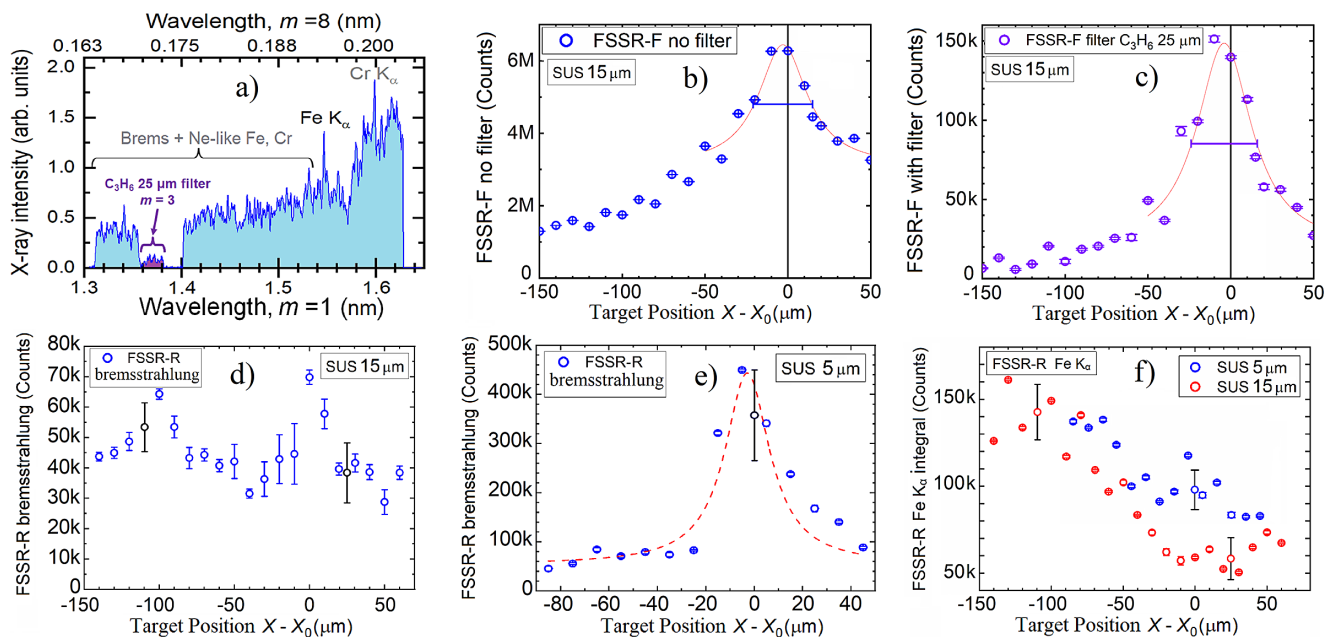
crystal to the interaction point of 2600 mm. The mica crystal employed in FSSR-F gave a resolving power of  $\lambda/\Delta\lambda \sim 2500$  at the central wavelength of  $\lambda_0 = 0.1875$  nm in the  $m = 8$  diffraction order corresponding to a wavelength of 1.5 nm in the first diffraction order.

FSSR-R was mounted at an in-plane angle of  $10.1^\circ \pm 0.1^\circ$  from the target normal and an out-of-plane angle of  $23.1^\circ \pm 0.1^\circ$ . The quartz crystal provided  $\lambda/\Delta\lambda \sim 3000$  resolving power at a wavelength of  $\lambda_0 = 0.1812$  nm in the  $m = 8$  diffraction order, corresponding to  $\lambda = 1.45$  nm in the first diffraction order. The distance from the FSSR-R crystal to the interaction point was 2045 mm.

An example of the spectrum registered with FSSR-F is shown in Figure 6(a). The spectrum covered a 1.31–1.63 nm range of wavelengths in the first diffraction order. In this spectrum, the spectral components of the other diffraction orders overlapped, thus making it possible to observe Fe  $K_\alpha$  ( $\lambda = 0.194$  nm) in the  $m = 8$  diffraction order and Cr  $K_\alpha$  ( $\lambda = 0.229$  nm) in the  $m = 7$  diffraction order. Most of the signals registered with the FSSR-F and FSSR-R detectors in the vicinity of the best in-focus target position were bremsstrahlung emitted from the laser–solid interaction. Spectral filters composed of 2- $\mu\text{m}$ -thick  $\text{C}_3\text{H}_6$  and 0.4- $\mu\text{m}$ -thick Al were placed in front of the CCD camera for the FSSR instruments. An additional narrow strip of a 25- $\mu\text{m}$ -thick  $\text{C}_3\text{H}_6$  as a spectral filter allowed for suppressing the bremsstrahlung radiation in the  $m = 3$  diffraction order.

Figures 6(b)–6(f) give the FSSR-F and FSSR-R data. Figures 6(b) and 6(c) show the FSSR-F spectrally integrated





**Figure 6.** (a) A typical FSSR-F spectrum recorded in the vicinity of the best in-focus target position. The spectrum covers wavelengths from 0.165 to 1.63 nm in different diffraction orders from  $m = 1$  to  $m = 8$ . Strong characteristic lines Fe  $K_{\alpha}$  ( $\lambda = 0.194$  nm) and Cr  $K_{\alpha}$  ( $\lambda = 0.229$  nm) were observed in  $m = 8$  and  $m = 7$  diffraction orders, respectively. The continuous signal corresponds to bremsstrahlung. A narrow strip of a 25- $\mu\text{m}$   $\text{C}_3\text{H}_6$  filter allows for observing a narrow portion of the spectrum, suppressing emission from lower diffraction orders ( $m = 1$ ,  $m = 2$ ). (b), (c) FSSR-F data for 15- $\mu\text{m}$  SUS targets, integrated within an area without (b) and with (c) the 25- $\mu\text{m}$ -thick  $\text{C}_3\text{H}_6$  filter. (d), (e) FSSR-R integrated bremsstrahlung signal for 15- $\mu\text{m}$  (d) and 5- $\mu\text{m}$  (e) SUS targets. (f) FSSR-R Fe  $K_{\alpha}$  integrated signals for 15- and 5- $\mu\text{m}$  SUS targets. The black error bars correspond to statistical shot-to-shot signal variations, while the smaller colored error bars are due to CCD camera noise. Lorentzian fits are shown, where applicable.

signals without a spectral filter (which was a sum of the two regions with blue shading in Figure 6(a)) and with the 25- $\mu\text{m}$   $\text{C}_3\text{H}_6$  spectral filter (with violet shading in Figure 6(a)), respectively, for the 15- $\mu\text{m}$  SUS target. A clear approximately 40- $\mu\text{m}$  FWHM single peak occurs in both cases, assuring the best in-focus target positioning with a better than 20  $\mu\text{m}$  accuracy.

Figures 6(d) and 6(e) show spectrally integrated bremsstrahlung signals (in the 1.35–1.54 nm spectral region in the first order of diffraction) from FSSR-R for 15- and 5- $\mu\text{m}$ -thick targets, respectively. Multi-peak behavior was observed for the 15- $\mu\text{m}$  target (Figure 6(d)), with one of the peaks ( $\sim 20$   $\mu\text{m}$  FWHM) corresponding to the best in-focus target position. The second peak can be explained by the fact that soft X-rays can be effectively generated from large-area spots at a relatively low intensity. Since the distance between the peaks was approximately 100  $\mu\text{m}$ , this can give a 10  $\mu\text{m}$  accuracy if the target is put within a 50  $\mu\text{m}$  range from the best focus position using other diagnostics.

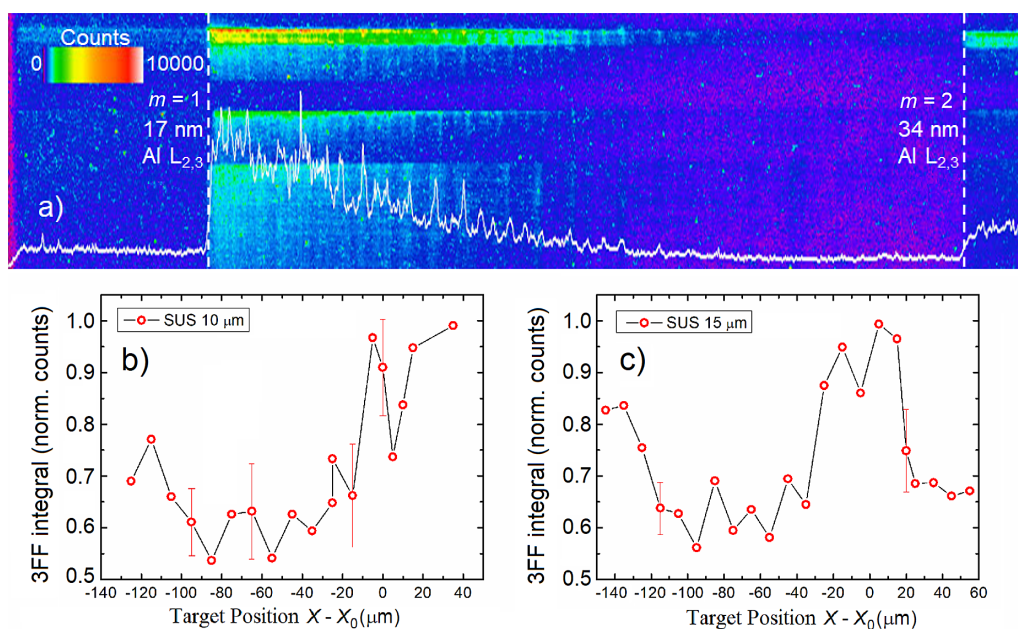
Figure 6(f) shows dependences of the Fe  $K_{\alpha}$  signals integrated in the 0.1925–0.1942 nm spectral region in the eighth diffraction order on  $X - X_0$  for the 15- and 5- $\mu\text{m}$ -thick SUS targets. Contrary to the previous cases, the Fe  $K_{\alpha}$  signals increased when the target moved away from the best focus. Thus, the Fe  $K_{\alpha}$  line was not suitable for the target positioning.

## 7. Three-channel flat-field spectrograph

The 3FF grazing incidence spectrograph<sup>[88]</sup> was mounted in the ‘specular reflection’ direction behind a hole in the screen used for the NIR-vis-UV diagnostics. The 3FF is a slit-less version of a flat-field spectrograph employing a VLS grating operating at a grazing incidence angle of  $4.2^\circ$  (i.e.,  $85.8^\circ$  off-normal), designed for recording a broad spectral region of 5–90 nm<sup>[88–90]</sup>. For a spatial resolution and a better signal-to-noise ratio, three gold-coated grazing incidence mirrors having shapes of elliptical cylinders were employed. The horizontal acceptance angles were slightly different for the three channels:  $0.15^\circ$  for the shallow-angle mirror,  $0.20^\circ$  for the central mirror and  $0.26^\circ$  for the high-deviation-angle mirror.

The VLS grating manufactured by Hitachi on a spherical substrate with  $R = 5649$  mm had an average central groove density of 1200 lines/mm. The vertical acceptance angle of  $0.087^\circ$  was defined by the  $r = 2425$  mm distance from the source to the center of the VLS grating, and by the  $50 \text{ mm} \times 30 \text{ mm}$  grating aperture. Thus, the acceptance angles for the three channels were  $3.9 \times 10^{-6}$ ,  $5.2 \times 10^{-6}$  and  $7.0 \times 10^{-6}$  sr, respectively. A single-pass 0.65- $\mu\text{m}$ -thick Al filter was mounted in front of the 3FF spectrometer, defining the 17–34 nm operating spectral range.

It is well known that relativistic laser–solid interaction is an intense source of HOH generated mostly in the ‘specular reflection’ direction<sup>[91,92]</sup>. However, since the harmonics’



**Figure 7.** (a) 3FF spectrum with harmonics. The upper and lower parts correspond to the shallow- and high-deviation-angle mirrors, respectively. Dashed lines show the Al filter cutoff ( $\lambda = 17$  nm) in the first and second diffraction orders. (b), (c) Integrated 3FF signal versus target position for 10- and 15- $\mu\text{m}$  SUS targets, respectively. The error bars correspond to shot-to-shot signal variations.

divergence can be narrow, we did not observe them in many shots, partly due to the small acceptance angles. Also, HOH generation depends on the pre-plasma scale length<sup>[93,94]</sup> and intensity, defined in our case by the laser contrast and  $X - X_0$  shift.

Figure 7(a) shows a typical 3FF spectrum with HOH. Figures 7(b) and 7(c) show the dependences of the 3FF signal on  $X - X_0$  for 10- and 15- $\mu\text{m}$ -thick SUS targets, respectively. The 3FF data had an approximately 50  $\mu\text{m}$  broad peak in the vicinity of the best focus, with a clear dip of the signal near the middle. There was a lower peak at  $X - X_0 \sim 120\text{--}140$   $\mu\text{m}$ . Within the main 3FF peak, the estimated dimensionless amplitude  $a_0$  was greater than 10, reaching approximately 60 at focus. Therefore, the main HOH generation mechanism was the relativistic oscillating mirror<sup>[95,96]</sup>.

We did not observe harmonics in many shots, probably due to the small acceptance angles. Along with this, the optimum combination of the laser intensity and the pre-plasma scale length might not be satisfied in every shot. The presence of the HOH had been recorded within the  $\pm 25$   $\mu\text{m}$  distance from the best in-focus target position only, while the relative difference in the integrated signals from the shots with and without harmonics was around 20%.

Thus, the 3FF spectrometer can determine the best in-focus target position with an approximately 25  $\mu\text{m}$  accuracy, using both the integrated 3FF signal and visual observation of harmonics. The dip in the 3FF signal close to the best focus position  $X_0$  can be used to place the targets with an approximately 5  $\mu\text{m}$  accuracy, although this result may be laser-contrast-dependent.

## 8. Discussion

As the laser was operated at a relatively low repetition rate of 0.1 Hz, we wanted to minimize the time spent on the search for the best target position. We used typically 10–20 shots during 3–11 minutes for the scans presented here, where the latter time was due to manual analysis of readings from many instruments operating simultaneously. All the data acquisition and saving procedures were automated, including automatic file naming with the shot number, for both facility instruments and our metrology. Further, our software automatically indicated the number of counts within our regions of interest. However, the software did not automatically plot the data versus target position figures. This was done in a separate figure plotting software, which typically took an extra 2–3 minutes for each target thickness. Obviously, this can be automated to speed up the process.

With only two or three instruments best suited for the target positioning, this time can be reduced down to 1.5–3 minutes with the same laser repetition rate. Our goal was to place the target with an accuracy of better than  $\pm Z_R$ , where  $Z_R \approx 10$   $\mu\text{m}$  is the Rayleigh length. We used 10  $\mu\text{m}$  steps (sometimes 5  $\mu\text{m}$  steps), so that the best near-focus target positions were within  $\pm 5.0$   $\mu\text{m}$  (or  $\pm 2.5$   $\mu\text{m}$ ) from the ‘perfect’ position. Therefore, even in the worst case, the peak intensity on-target was higher than 0.8 (0.94) of the ideal estimated peak value of  $7 \times 10^{21}$  W/cm<sup>2</sup>. Assuming random defocusing within the  $\pm 5$  and  $\pm 2.5$   $\mu\text{m}$  ranges, the intensity was  $0.93 \pm 0.06$  and  $0.98 \pm 0.02$  of the ideal value, respectively.

**Table 1.** Accuracy of the instruments for the best in-focus target positioning.

Name of the instrument	Peak FWHM ( $\mu\text{m}$ )	Peak shift ( $\mu\text{m}$ )	Estimated <sup>a</sup> accuracy ( $\mu\text{m}$ )	Comment
Reflection 'specular direction' camera, $1\omega$	$\sim 60$	$\sim 20$	$\sim 30$	Multi-peak
Reflection 'specular direction' camera, $2\omega$	$24 \pm 6$	$< 5$	$\sim 12$	
Reflection 'specular direction' spectrometer, $1\omega$	$\sim 70$	$\sim 30$	$\sim 30$	Multi-peak
Reflection 'specular direction' spectrometer, $2\omega$	$24 \pm 10$	$< 5$	$\sim 12$	
Reflection 'specular direction' spectrometer, $3\omega$	$18 \pm 6$	$< 4$	$\sim 5$	
Back-reflection camera		Not applicable		No peak
Rear-side XUV – thin targets	$40 \pm 6$	$< 5$	$\sim 20$	
Rear-side XUV – thick targets	$60 \pm 26$	$< 10$	$\sim 30$	Weak signal
Rear-side ESM	$\sim 120$	$\sim 40$	$\sim 60$	Plateau-like
Rear-side HXRS-1 (off-axis) – thin targets	$\sim 120$	$\sim 50$	$\sim 60$	No clear peak
Rear-side HXRS-1 (off-axis) – thick targets	$\sim 200$	$\sim 20$	$\sim 100$	Broad peak
Rear-side HXRS-2 (on-axis) – thin targets	$16 \pm 6$	$< 4$	$\sim 5$	Weak signal
Rear-side HXRS-2 (on-axis) – thick targets	$16 \pm 2$	$< 2.5$	$\sim 5$	
Front-side FSSR-F	$40 \pm 10$	$< 5$	$\sim 20$	
Rear-side FSSR-R – bremsstrahlung integral	$24 \pm 8$	$< 5$	$\sim 12$	Double-peak
Rear-side FSSR-R – Fe $K_{\alpha}$ integral		Not applicable		Multi-peak
'Specular reflection' 3FF spectrometer – integral	$\sim 50$	$\sim 10$	$\sim 25$	Multi-peak
'Specular reflection' 3FF spectrometer – HOH	$\sim 50$	$\sim 10$	$\sim 25$	
'Specular reflection' 3FF spectrometer – central dip	$\sim 10$	$\sim 5$	$\sim 5$	Contrast-dependent

<sup>a</sup>Estimated accuracy was a half-step size for the clean peaks, and a half width at half maximum (HWHM) for instruments with notable data fluctuations.

In Table 1 we summarize all the information presented in the previous sections. In most cases our scans were single-shot at each position, and the accuracy was estimated for this approach. The main limiting factors were shot-to-shot fluctuations and available experimental time. By multi-shot averaging, one can reduce the influence of the shot-to-shot fluctuations.

The best target positioning accuracy of better than  $5 \mu\text{m}$  was achieved using on-axis HXRS-2 inner scintillators and the third-order harmonic ( $3\omega$ ) instrument mounted in the 'specular reflection' direction. The  $2\omega$ , FSSR-F, FSSR-R, 3FF and XUV diagnostics provided an accuracy of approximately  $10\text{--}20 \mu\text{m}$ . The instruments that were best suited for the precise target positioning goals had peaks with good symmetrical shape and low data fluctuations, which means that the accuracy was better than half width at half maximum (HWHM) and corresponded to a half-step of the scanning. On the other hand, if the data fluctuations are high enough, then the accuracy should be estimated as the HWHM of the fitted peak.

Several diagnostics, such as  $1\omega$  reflection, ESM, low X-ray photon energy plates #0 of HXRS-1 and HXRS-2 and Fe  $K_{\alpha}$  yield were not suitable for determination of the best target position, since their highest signals were reached from out-of-focus large-area low-intensity interactions.

In this paper, we presented the diagnostics as useful means to find the best target position. If the main purpose of an experiment is hard X-ray generation, then our optimization with the HXRS-2 spectrometer immediately provides the best target position. At the same time, all our selected diagnostics operating at the target front and rear sides, in the optical, XUV and X-ray regions, provided the same best target positions as the hard X-ray (MeV) diagnostics, within their respective accuracy limits. In addition, this was

proved for each of the target thicknesses tested. Considering a small (a few  $\mu\text{m}$ ) pre-plasma length, it is unlikely that some other point in space, rather than the focus, would give a maximum for all the diverse diagnostics simultaneously. Thus, we conclude that the targets were placed at the best focus position.

Let us mention that we have investigated signals from many diagnostics, while most of the instruments we used in our study are not necessary at many high-power-laser facilities for the goal of best target positioning. In experiments similar to ours, given specific space constraints, an experimental team can choose two or three reliable diagnostics from the set described herein, and this should be enough for precise target positioning. Furthermore, we anticipate that by placing some of the instruments at similar but not exactly the same positions as described in this paper, using slightly different in-plane and out-of-plane angles, one can obtain similar results for the best target positioning purpose. However, this has to be proved in a separate dedicated study.

As for the types of targets that can be precisely placed at the best focus position using our method, we can highlight three important requirements:

(1) the target must be reproducibly positioned with a few micrometers accuracy;

(2) the positioning of the target before each shot should be fast, ideally faster than the laser system inverse repetition rate (for slower target positioning systems, the procedure becomes correspondingly longer; in the case of very long shot-to-shot intervals, the thermal laser stability on the extended time periods should be also tested and controlled);

(3) the targets used for the position scan should be identical or almost identical to keep the diagnostics output consistent (after that, other target types can be used, if placement to the same position is guaranteed).

We expect that any kind of target that complies with these three requirements can be precisely placed at the best focus position using our method. From our point of view, tape targets are the best for this purpose. Liquid targets can also be feasible. With the abovementioned restrictions, thin foils and nanostructured targets can also be used.

Compared to the well-established methods<sup>[45–47]</sup>, our proposed technique does not need coincidence or calculatable difference<sup>[97,98]</sup> between the positions of low-power and high-power focal planes. Furthermore, as the main experimental data shots immediately follow the focusing scan without changing the laser mode, moving instruments in and out or replacing filters in the laser diagnostics, the influence of long-term instabilities and thermal drifts was minimized. At the same time, our method relies on shot-to-shot reproducible laser parameters and the target position, which is relatively easily achievable with high-repetition-rate lasers and tape targets, while it can be challenging for less stable lasers or other target supply systems.

## 9. Conclusions

We have investigated the usefulness of 11 diagnostics (Table 1) for the best in-focus target positioning in order to have the highest on-target laser intensity in a relativistic laser–solid interaction experiment. The main challenge was to put the solid target within an extremely short Rayleigh length of approximately 10  $\mu\text{m}$ . We found that several diagnostics can ensure this accuracy.

The sharpest and most reliable diagnostic instrument was the rear-side on-axis HXRS-2 made of 10 LYSO scintillator crystal plates with the best sensitivity of the inner crystals to radiation energy of 0.1–2 MeV<sup>[82,83]</sup>. The prominent and clean signal maxima allowed us to find the best in-focus target position with an accuracy of better than 5  $\mu\text{m}$ , determined by a half step size during the target position scan.

Several other instruments were also capable of positioning the target within a comparable accuracy of approximately 5–10  $\mu\text{m}$ . They were low-order harmonics ( $2\omega$ ,  $3\omega$ ) mounted in the ‘specular reflection’ direction<sup>[67–69]</sup>. At  $2\omega$ , a camera and fiber spectrometer provided consistent results.

The integrated bremsstrahlung signal over the 0.7–10 keV range (but not the  $K_{\alpha}$  radiation) recorded with the rear-side FSSR-R instrument could also give an approximately 10  $\mu\text{m}$  accuracy. However, the FSSR-R data had a double-peak shape with peak separation of approximately 100  $\mu\text{m}$ , requiring a correct peak selection by means of other diagnostics. The front-side FSSR-F accuracy was approximately 20  $\mu\text{m}$ .

The rear-side XUV spectrometer ( $\lambda = 17\text{--}22\text{ nm}$ ) provided around 20  $\mu\text{m}$  accuracy for targets with thickness of less than or equal to 10  $\mu\text{m}$ . For 15- $\mu\text{m}$  targets, the signal-to-noise ratio became low and the peak width increased, so the accuracy was around 30  $\mu\text{m}$ . For 20- $\mu\text{m}$  targets, XUV diagnostics were not applicable due to the low signal-to-noise ratio.

The ‘specular reflection’ 3FF spectrograph (17–34 nm) showed a multi-peak dependence, with approximately 30% probability of HOH registration within  $\pm 25\text{ }\mu\text{m}$  from the best focus. If the correct peak was picked by means of other diagnostics, the 3FF provided approximately 25  $\mu\text{m}$  target positioning accuracy. The central peak in the dependency had a dip at the best focus position for all target thicknesses, suggesting a better, approximately 5  $\mu\text{m}$  accuracy (although it may be laser-contrast-dependent).

All front-side  $1\omega$  diagnostics, as well as the rear-side ESM and off-axis HXRS-1, were not applicable for target positioning, because the estimated precision of those instruments was worse than 30  $\mu\text{m}$ . We note that some of these might be used as auxiliary diagnostics to roughly place the target with an approximately 30–100  $\mu\text{m}$  accuracy.

Employing the best diagnostics, we consistently performed the best in-focus target positioning with an estimated accuracy of around 5  $\mu\text{m}$  and discrepancy of less than 5  $\mu\text{m}$  between many instruments, resulting in the intensity on-target of at least 80% (94% for some scans) of the ideal estimate of  $7 \times 10^{21}\text{ W/cm}^2$ .

## Appendix A

Here we describe the target positioning methods that we have tried, but found that they cannot provide the required approximately 10  $\mu\text{m}$  accuracy.

### A.1. Imaging the target surface with a focal-spot monitor

This method is often used with transparent targets using the attenuated defocused laser beam transmitted through the target. However, in our case of non-transparent stainless-steel tapes it was not usable. A variation of this method with white-light illumination from the rear side of the target required significant light power, due to the high imaging system magnification, which led to target heating and notable bending, which we confirmed by varying the illumination light power. We note that the thermal bending problem can be avoided by using a confocal microscope, which requires much lower light power; however, we did not have this technique as a facility device and decided not to implement it as a part of our experiment, because, even though this device might really help us precisely position the target at a plane coincident with the focal plane of the low-power laser beam in a mode used for the alignment, this does not guarantee that the full-power-mode beam would have focus at the same plane with the required sub-10- $\mu\text{m}$  accuracy.

### A.2. Imaging the edge of the non-transparent target with a focal-spot monitor

This method is often used with relatively narrow targets, when the possible errors in the target translation direction do not lead to significant defocusing. However, in our case

of 20-mm-wide tapes, the direction error in the target translation by a distance of 10 mm could lead to a substantial target position mismatch. We note that narrower tapes could not be used in our case, as this increased significantly the frequency of the tape breaking under the exposure to the full-power shots, as we experienced in previous experiments. Also, any possible target edge bending may cause additional positioning errors. The final reason was the same as in the previous method. Even though the technical difficulties of this method can be potentially overcome, the target would be positioned at the low-power-mode focal plane, which is not necessarily the same as for the high-power beam.

In summary, we state that the methods described in this appendix can be used for the initial target positioning with an approximately 100  $\mu\text{m}$  accuracy before the experiment. Our choice of pre-positioning the target using the interferometry line, as described in the main text, was a matter of convenience, because it also ensured alignment of the target rotation angle with an approximately  $0.1^\circ$  accuracy.

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