

THE
BULLETIN
OF
SYMBOLIC LOGIC

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Articles should be of broad interest and accessible to a wide audience of logicians. They may be purely expository, survey, or historical articles, or they may contain, in addition, new ideas or results or new approaches to old ones.

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