

Editor-in-Chief:

J. N. SRIVASTAVA, Colorado State University, Fort Collins, Colorado 80523, U.S.A.

Aims and Scope

This new journal has been established to provide a common medium for the dissemination of significant information in all branches of statistical planning and related inference problems. By statistical planning is meant any work concerned with the collection of data either from experiments or investigations and whether it is collected in one or several attempts. It will encompass problems of handling or transmission of data or information. The journal aims to stimulate research, to help workers avoid duplication of effort and to promote the use of statistical planning techniques in various scientific fields. The inclusion of a non-technical summary with most papers is proposed, so that applied statisticians may become familiar with theoretical advances and theoretical researchers may be aware of new unsolved mathematical problems in applied fields.

Among the many important subjects to be covered are:

(a) All Areas of Application

Agriculture, Biology, Genetics, and Medicine and Clinical Trials Engineering and Industry Earth Sciences; Weather Modification Physical Sciences Psychology, Economics and Other Social Sciences

- (b) Experimental Design Theory
- (c) Sampling Theory
- (d) Combinatorial Mathematics Related to Statistical Planning
- (e) Information Theory
- (f) Computer Oriented Problems
- (g) Search Theory and Search Design

(This is a relatively new and potentially very important field, where the problem is not only to estimate or test hypotheses regarding parameters, but also to "search" important parameters. The theory involves a mixture of stochastic processes, information theory, combinatorial mathematics, and statistics).

(h) Statistical Inference

(i) Inference in Search Linear Models

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Authors of papers within the scope of the journal are cordially invited to submit typed manuscripts in triplicate to

The Editor-in-Chief, Prof. J. N. Srivastava, Department of Statistics, Colorado State University, Fort Collins, Colorado 80523, U.S.A.

Subscription Information:

IOURNAL OF STATISTICAL PLANNING AND INFERENCE will be published in volumes of 4 issues (approx. 400 pages per volume), one volume per year. The first two issues are scheduled to appear in the summer of 1976. Thereafter quarterly issues will appear in March, June, September and December.

Subscription price volume 1, 1976/1977: US \$44.95 / Dfl. 112.00 (including postage)

If you require further information and/or a free specimen copy of the first issue when available, please write directly to the publisher.

Editorial Board

All contributions will be refereed by members of a large international Editorial Board. The Board consists of distinguished workers from all over the world and ensures not only widespread geographical coverage but excellent representation of the various areas and sub-areas dealt with in the journal.

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CONFERENCE

ON

GRAPHICAL METHODS IN STATISTICS

This conference, organised by the Manchester-Sheffield School of Probability and Statistics, will be held at

THE UNIVERSITY OF SHEFFIELD, U.K.

over the period 28-30 March 1977.

The conference aims to cover a range of topics in this important and developing area of statistics, including the utilisation of graphical methods in the analysis of large-scale data and the impact of sophisticated computer graphical facilities on the development of statistical method and on the teaching of statistics. Programme plans are already well advanced and an international group of speakers will present talks on various aspects of the conference theme.

The initial keynote lecture will be delivered by Professor D. R. Cox of Imperial College, London.

For further information on any aspects of the conference including requests for registration material, please communicate with:

The Conference Secretary, Department of Probability and Statistics, University of Sheffield, Sheffield, S3 7RH. Telephone: Sheffield (0742) 78555 U.K. ext. 269.

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Price per copy: £0.50 (US\$1.25; \$A.1.00).

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This title was issued as a special supplement to Adv. Appl. Prob. Volume 7 No. 3. A limited number of copies are still available at the price of £1.50 (US\$3.50; \$A.2.40).

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This magazine addresses itself primarily to young mathematicians in schools, colleges of education and universities. Its object is to discuss the entire range of modern mathematical disciplines in an informative but informal manner and to relate discoveries in mathematics to progress in the natural sciences, technology, social studies and business management.

The Editors believe that the process of learning is a dialogue and consequently they wish to promote active participation by readers. Correspondence on any subject relating to mathematics and mathematical education is welcomed. There is also a problem section, and readers are encouraged to submit their solutions, the best of which are published.

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In addition to these Review Papers, *Advances* is also designed to be a medium of publication for (1) longer research papers in Applied Probability, which may include expository material, (2) expository papers on branches of mathematics of interest to probabilists, (3) papers outlining areas in the biological, physical, social and technological sciences in which probability models can be usefully developed, and finally, (4) papers in Applied Probability presented at conferences which do not publish their proceedings.

In short, the main function of *Advances* is to define areas of recent progress and potential development in Applied Probability. As with the *Journal of Applied Probability, Advances* undertakes to publish papers accepted by the Editors within 15 months of their submission.

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Volume 8 No. 3 of Advances contains the following papers:

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J. D. BIGGINS	The first- and last-birth problems for a multitype age-dependent
	branching process
PHILIP C. PROROK	The theory of periodic screening II: doubly bounded recurrence
	times and mean lead time and detection probability estimation
DAVID MANNION	Random packing of an interval
HARRY COHN	Finite non-homogeneous Markov chains: Asymptotic behaviour
CRISTINA GZYL	Some results about Markov processes on subsets of the state space
ESA NUMMELIN	Limit theorems for α -recurrent semi-Markov processes
LAJOS TAKÁCS	On fluctuation problems in the theory of queues
ANDREW D. BARBOUR	Networks of queues and the method of stages
JOHN HASLETT	The control of a multipurpose reservoir

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10% discount is allowed to subscribers who order current issues of both the *Journal* and *Advances* at the same time direct from the Editorial Office. The prices are as follows:

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All enquiries about the *Journal*, as well as other subscriptions and orders for back numbers should be sent to the Executive Editor, Miss M. Hitchcock, Department of Probability and Statistics, The University, Sheffield S3 7RH, England. The price of back numbers varies from volume to volume, and enquiries should be sent to the Executive Editor. Cheques, money orders, etc. should be made out to *Applied Probability*; cheques on U.S., U.K. and Australian banks will be acceptable.

Notes for Contributors

Submission of papers

It is a condition of publication in the Journal of Applied Probability that papers shall not previously have appeared elsewhere, and will not be reprinted without the written permission of the Trust. The copyright of all published papers shall be vested in the Trust. It is the general policy of the Journal not to accept for publication papers which cannot appear in print within 15 months of their date of submission. Authors will receive 50 reprints of their papers free, and joint authors a proportional share of this number. Additional reprints will be provided at cost.

Manuscripts should be written in English or French; manuscripts in other languages may be accepted by the Editors, but will appear (subject to the author's agreement) in English or French translation in the *Journal*. Authors are requested to comply with the following instructions in submitting their papers:

Authors in Britain, Europe, North and South America should send *three copies* of their submissions to the Applied Probability Office in Sheffield.

Authors in Australasia and the Far East should send *three copies* of their submissions to the Editorin-Chief, Dr. J. Gani, in Canberra.

The Editor-in-Chief and the Applied Probability Office are in direct contact by Telex, and full details of the papers submitted either in Sheffield or Canberra are available in both centres.

Alternatively, authors may submit papers to any one of the Editors listed on the inside front cover. In this case, *two copies* of the submission should be sent to the Editor concerned, and *one copy*, with a copy of the covering letter, should be sent to the Applied Probability Office in Sheffield.

Journal conventions

It will be of help to the Editors if the following conventions are adopted:

- a) The manuscript should be typewritten, using double spacing, on one side of the paper only.
- b) Each paper submitted should be accompanied by
 - (i) a short abstract of approximately 4–10 lines giving a non-mathematical description of the subject matter and results;
 - (ii) a list of keywords detailing the contents for the purpose of computerised information retrieval.

c) References should be indicated in the text by the name of the author(s) and the date, thus: Feller (1961), and the full references listed at the end of the article in alphabetical order. Journal references should include the title of the article cited, the title of the journal (abbreviated in the style of the *International Journal of Abstracts: Statistical Theory and Method*), the volume, and inclusive page numbers. Book references should give the full title, the publisher, and the place of publication. For example:

Feller, W. (1961) A simple proof of renewal theorems. Comm. Pure Appl. Math. 14, 285–293. Robinson, E. A. (1959) An Introduction to Infinitely Many Variates. Griffin, London.

d) Type faces should be carefully distinguished on the manuscript using the following standard methods of marking:

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Authors will receive only first proofs for correction; charges will be made for excessive alteration to these.

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