# EFFECTS OF CLAY FRACTION AND TEMPERATURE ON THE H<sub>2</sub>O SELF-DIFFUSIVITY IN HECTORITE GEL: A PULSED-FIELD-GRADIENT SPIN-ECHO NUCLEAR MAGNETIC RESONANCE STUDY

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**Abstract**—Self-diffusion coefficients of H<sub>2</sub>O molecules in Na-rich hectorite gel were measured by <sup>1</sup>H nuclear magnetic resonance (NMR). Spin-echo pulse sequences with magnetic field gradient pulses for the translational diffusion measurement were applied to the hectorite gel at the Larmor frequency of 20 MHz. Effects of clay fraction (0–51.2 wt. %) and temperature (20.0–60.3°C) were studied. The results show: (1) Phenomenologically, the self-diffusion coefficient, D, of <sup>1</sup>H<sub>2</sub>O in the clay gel is expressed by the normalized diffusivity,  $D/D_0 = \exp(-0.0257w)$ , where  $D_0$  is the water self-diffusivity in bulk water at temperature and w is the weight fraction of the hectorite (wt. %). (2) The activation energy of H<sub>2</sub>O diffusivity in the hectorite gel is nearly equal to that in bulk water. Hence, the normalized diffusivity,  $D/D_0$ , obeys a temperature-independent curve. (3) The exponential dependence of  $D/D_0$  on w for w < 30 wt. % is explained by a random-walk model, in which free or unbound H<sub>2</sub>O molecules migrate in the geometrically complex and tortuous pore structure of randomly scattered clay-mineral grains. **Key Words**—Complexity of Pore Structure, Hectorite, H<sub>2</sub>O, NMR, Self-Diffusion.

#### INTRODUCTION

Diffusion is a dominant mechanism of ground-water migration through less permeable clay barriers with small Péclet values. Thus, measurements of the coefficients of diffusion of H<sub>2</sub>O in clay are important in applied clay science, particularly for nuclear waste disposal (e.g., Madsen, 1998). Many studies exist on H<sub>2</sub>O mobility or diffusivity in clays (e.g., Mokady and Low, 1968; Low, 1976, 1979; Cebula et al., 1981; Fripiat et al., 1984; Tuck et al., 1985; Miyahara et al., 1991; Sato et al., 1992; Chang et al., 1995, 1998; Yu and Neretnieks, 1997; Ichikawa et al., 1999). One of the most important results of these studies is that H2O diffusivity in clay depends on the water fraction. For example, Cebula et al. (1981) and Chang et al. (1995, 1998) argued that diffusivity increases with increasing water fraction for relatively dry (<30 wt. % H<sub>2</sub>O) clay. However, an extensive study on the effects of clay or water fractions on H<sub>2</sub>O diffusivity has not been made for a clay gel of >50 wt. % H<sub>2</sub>O, which is more relevant to nuclear waste disposal because clay below the ground-water level contains significant amounts of water. In the present study, systematic experiments on H<sub>2</sub>O diffusion were performed for hectorite (a common clay mineral) gel of >48.8 wt. % H<sub>2</sub>O at five sample temperatures.

The self-diffusion coefficients of water molecules ( ${}^{1}\text{H}_{2}\text{O}$ ) in a Na-rich hectorite gel were measured using spin-echo  ${}^{1}\text{H}$  nuclear magnetic resonance (NMR). The pulsed-field-gradient (PFG) proton NMR technique is appropriate to obtain high-precision data on the translational diffusivity of H<sub>2</sub>O in clay (Fripiat *et al.*, 1984; Nakashima *et al.*, 1999). This technique was applied in the present study (1) to examine the effects of the

clay weight fraction of the gel on the self-diffusion coefficients of  ${}^{1}H_{2}O$  molecules and (2) to evaluate the temperature-dependence of self-diffusivity. The obtained diffusion data were analyzed by a random-walk model of unbound H<sub>2</sub>O molecules in porous media.

#### EXPERIMENTAL METHODS

Hectorite is a trioctahedral smectite. The ideal formula of Na-rich hectorite is  $(Mg_{3,\nu}Li_{\nu})Si_4O_{10}(OH)_2$  $Na_v \cdot nH_2O$  (y = 0.2-0.6). The negative charge of the silicate layer is derived from the substitution of Li+ for Mg2+ in the octahedral sheet. The Na-rich hectorite sample used is a synthetic powder produced by Kunimine Industries Co., Ltd (Tokyo, Japan). The chemical composition (wt. %) is: SiO<sub>2</sub>, 49.92; Al<sub>2</sub>O<sub>3</sub>, 0.04; MgO, 24.3; Li<sub>2</sub>O, 0.99; CaO, 0.12; Na<sub>2</sub>O, 5.59; SO<sub>3</sub>, 0.97; and H<sub>2</sub>O, 18.03 (total 99.96). This Mn- and Fefree synthetic sample is essential to the high-precision NMR experiments because paramagnetic impurities shorten relaxation times of protons. The weight loss of the powder sample was 8.5 wt. % at 110°C. The average grain diameter of the hectorite in suspension (0.2 wt. % clay) was found to be 0.054  $\mu$ m by the laser-Doppler method.

By adding deionized water to the powder sample, 20 clay-gel samples (ranging from 1.83 to 51.2 wt. % clay) were prepared. The self-diffusion coefficient in bulk water (deionized water) was also measured at 25, 35, and 45°C to determine the accuracy of the NMR data. Relaxation times ( $T_i$ , spin-lattice relaxation time, and  $T_2$ , spin-spin relaxation time) for protons associated with H<sub>2</sub>O of the 20 gel samples and deionized water were measured at 39.7°C (Figure 1; Table 1). The bulk densities of the 21 samples at 22°C were

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(Table 1).



Figure 1. Relaxation times of protons in hectorite gel at 20 MHz and 39.7°C versus clay fraction, w (data from Table 1).  $T_1$  and  $T_2$  were measured by the inversion recovery method and spin-echo method, respectively. The 90°–180° pulse separation was 0.5 ms for the spin-echo method. The solid lines were approximated.

obtained by weighing each sample of known volume

suring the decrease in the NMR-signal intensity with

increasing magnetic field gradients (Stejskal and Tan-

ner, 1965). The pulsed-field-gradient (PFG) spin-echo

Self-diffusion coefficients were calculated by mea-



Figure 2. A diffusion-weighted spin-echo pulse sequence used in the present study. A spin-echo NMR signal is generated from a sequence consisting of 90° and 180° radio-frequency (rf) pulses and the intensity is modulated by two fieldgradient pulses. A 90° pulse refers to a pulse which rotates the magnetization vector of protons by 90°. TE is the echo time. This sequence is repeated at a period of TR. FID is a free induction decay signal which was not measured in the present study.

pulse sequence used is shown in Figure 2. The NMR spin-echo signal intensity, *I*, is given by:

$$I = I_0 \exp(-bD) \tag{1}$$

where

$$b = (\gamma G \delta)^2 (\Delta - \delta/3). \tag{2}$$

The quantity  $I_0$  is the signal intensity without magnetic field gradients,  $\gamma$  is the gyromagnetic ratio of a proton (2.675 × 10<sup>8</sup> rad/Ts), G is the strength of the gradient pulses,  $\delta$  is the duration of the field gradient pulses,  $\Delta$ 

Table 1. Results of the NMR experiments of hectorite gel ( $\Delta = 14$  ms). The water fraction (wt. %) is 100 - w and includes pre-existing H<sub>2</sub>O (weight loss of 8.5 wt. % at 110°C) of the clay powder.

| w<br>(wt. %) | Density<br>22°C<br>(g/mL) | T <sub>1</sub><br>39.7°C<br>(ms) | $\begin{array}{c} T_2 \\ 39.7^{\circ}C \\ (ms) \end{array}$ | D<br>20.0°C | D<br>30.1°C | D<br>39.7°C<br>(10 <sup>-9</sup> m²/s) · · · · · | D<br>50.3°С | Д<br>60.3°С | E<br>(kJ/mol) |
|--------------|---------------------------|----------------------------------|---|-------------|-------------|--|-------------|-------------|---------------|
| 0.00         | 1.0                       | 3750                             | 2594  | 1.96        | 2.55        | 3.22   | 4.05        | 4.86        | 18.1          |
| 1.83         | 1.0                       | 2718                             | 861   | 1.86        | 2.43        | 3.09   | 3.86        | 4.66        | 18.2          |
| 2.74         | 1.0                       | 2541                             | 682   | 1.82        | 2.37        | 3.00   | 3.74        | 4.53        | 18.1          |
| 3.66         | 1.0                       | 2345                             | 541   | 1.78        | 2.30        | 2.93   | 3.65        | 4.42        | 18.2          |
| 4.57         | 1.0                       | 2180                             | 477   | 1.73        | 2.26        | 2.86   | 3.59        | 4.32        | 18.2          |
| 5.48         | 1.0                       | 2019                             | 420   | 1.69        | 2.19        | 2.79   | 3.48        | 4.23        | 18.3          |
| 7.24         | 1.1                       | 1770                             | 308   | 1.60        | 2.09        | 2.63   | 3.30        | 4.00        | 18.3          |
| 9.08         | 1.1                       | 1586                             | 268   | 1.54        | 2.00        | 2.55   | 3.18        | 3.85        | 18.2          |
| 11.0         | 1.1                       | 1413                             | 217   | 1.46        | 1.89        | 2.41   | 3.00        | 3.63        | 18.2          |
| 13.5         | 1.1                       | 1200                             | 173   | 1.36        | 1.77        | 2.26   | 2.80        | 3.41        | 18.2          |
| 16.4         | 1.2                       | 1015                             | 146   | 1.258       | 1.63        | 2.08   | 2.59        | 3.14        | 18.3          |
| 19.1         | 1.2                       | 909                              | 120   | 1.17        | 1.53        | 1.94   | 2.43        | 2.95        | 18.4          |
| 21.8         | 1.2                       | 815                              | 103   | 1.11        | 1.44        | 1.84   | 2.29        | 2.79        | 18.4          |
| 25.4         | 1.2                       | 674                              | 86.7  | 1.02        | 1.34        | 1.69   | 2.11        | 2.58        | 18.5          |
| 29.2         | 1.2                       | 587                              | 68.6  | 0.943       | 1.24        | 1.56   | 1.97        | 2.40        | 18.6          |
| 32.8         | 1.3                       | 491                              | 58.9  | 0.869       | 1.13        | 1.44   | 1.82        | 2.21        | 18.7          |
| 36.5         | 1.4                       | 415                              | 50.7  | 0.779       | 1.01        | 1.28   | 1.62        | 1.97        | 18.5          |
| 40.0         | 1.4                       | 353                              | 41.6  | 0.698       | 0.894       | 1.14   | 1.43        | 1.73        | 18.3          |
| 43.4         | 1.4                       | 314                              | 37.3  | 0.683       | 0.878       | 1.10   | 1.39        | 1.69        | 18.3          |
| 47.4         | 1.5                       | 281                              | 32.2  | 0.600       | 0.729       | 0.956  | 1.18        | 1.44        | 18.0          |
| 51.2         | 1.6                       | 240                              | 27.1  | 0.537       | 0.667       | 0.859  | 1.05        | 1.30        | 18.0          |



Figure 3. Example of spin-echo NMR signals for w = 29.2 wt. % at 39.7°C. The field-gradient intensity is indicated. The echo height at TE = 28 ms obeys Equation (1).

is the interval between two gradient pulses (characteristic diffusion time of  $H_2O$  molecules), and D is the self-diffusion coefficient of  $H_2O$  (e.g., Johnson, 1996).

PFG NMR measurements were performed with an NMS120 proton spectrometer (Bruker, Karlsruhe, Germany) at the resonant frequency of 20 MHz. Each sample (volume  $\sim 1 \text{ cm}^3$ ) was placed in a separate glass tube (outside diameter, 10 mm). A probehead PH20/10VTS with gradient coils was used to produce magnetic field gradients of  $\leq 2.1$  T/m. The pulse parameters were as follows:  $\delta = 0.7$  ms, the echo time  $TE = 28 \text{ ms}, \Delta = 14 \text{ ms}, \text{ the } 90^{\circ} \text{ pulse length was } 2.8$ µs, and the number of stacking of echo signals was 16. The repetition time of the pulse sequence, TR, was taken to be  $TR = 5T_i$ . About ten values of G (from 0 to 2.1 T/m) were used for a specific clay fraction and temperature to measure the dependence of I on b. As a result, D was calculated from a regression analysis of the data sets  $(I/I_0, b)$  using Equation (1). The experiments were performed at atmospheric pressure and no pressure vessel (e.g., Figure 1 of Miyahara et al., 1991) was used. Five temperatures (20.0, 30.1, 39.7, 50.3, and 60.3°C) were chosen to calculate the activation energy for the diffusion process.

Because the silicate layer of each clay grain is impermeable, diffusing H<sub>2</sub>O molecules are forced to go around the obstacles (clay grains) in the porous gel. Thus, the random-walk trajectory of the molecules is probably restricted by these obstacles, which is termed a 'restricted diffusion regime'. The condition of the regime is  $\Delta \gg d^2/6D$  where d is the average pore diameter of the clay gel (e.g., Callaghan, 1991). The physical meaning is that characteristic diffusion time of H<sub>2</sub>O ( $\Delta$ ) is much larger than the time required for migrating H<sub>2</sub>O to travel a pore of d in size (d<sup>2</sup>/6D). In



Figure 4. NMR-signal intensities versus the b factor at  $39.7^{\circ}$ C for eight samples. Each clay fraction is indicated. Data points are fitted to Equation (1) by a *least-squares* method. Note that higher D yields a higher slope.

terms of the diffusivity, this regime is characterized by  $\Delta$ -independence of *D*. Thus, large- $\Delta$  experiments ( $\Delta = 140 \text{ ms}$ ) were also performed for some samples to confirm that the measured H<sub>2</sub>O diffusivity was under the restricted diffusion regime.

### **RESULTS AND DISCUSSION**

A qualitative discussion on D is possible using proton relaxation data. Figure 1 shows that  $T_1$  and  $T_2$  decrease as the clay fraction increases. The mechanism for the spin relaxation in porous media is the collision of diffusing H<sub>2</sub>O molecules at the surface of solids. The small (or large)  $T_1$  and  $T_2$  imply the high (or low) collision-frequency. The high (or low) collision-frequency is related to the dense (or sparse) packing structure of the clay grains in which H<sub>2</sub>O molecules diffuse by a random walk. The dense (or sparse) packing yields the low (or high) values of D because the clay grains are obstacles for the migrating H<sub>2</sub>O molecules. Thus Figure 1 predicts that H<sub>2</sub>O self-diffusivity decreases with increasing clay fraction. This qualitative prediction is quantitatively verified by the PFG NMR experiments of the present study.

Examples of time domain spin-echo signals (Figure 3) and *b*-dependent echo intensities (Figure 4) are shown for selected clay samples. The slope of each regression line in Figure 4 gives the self-diffusion coefficient of  $H_2O$ , *D*. These regression lines gave high precision in the calculated diffusion-coefficient values. The accuracy of the PFG NMR experiments can be



Figure 5. Schematic microstructure of hectorite gel. The trajectory (arrow) of the random walk is geometrically restricted by the packing of hectorite grains. An example of the random covering of clay by circles is shown for a single grain. As wincreases, the water-filled pore space may shrink into the interlayer space filled with several monolayers of H<sub>2</sub>O between clay platelets.

discussed by using the diffusion coefficient for bulk water (Holz and Weingärtner, 1991). Mills (1973) produced very reliable values for diffusion in bulk water,  $D = 2.299 \times 10^{-9}$  m<sup>2</sup>/s at 25.0°C, 2.919  $\times 10^{-9}$  m<sup>2</sup>/s at 35.0°C, and 3.575  $\times 10^{-9}$  m<sup>2</sup>/s at 45.0°C. The selfdiffusivity of the bulk water sample,  $D_0$ , measured here was  $2.25 \times 10^{-9}$  m<sup>2</sup>/s at 25.0°C,  $2.89 \times 10^{-9}$  m<sup>2</sup>/ s at 35.0°C, and  $3.58 \times 10^{-9}$  m<sup>2</sup>/s at 45.0°C. These values agree well with the data of Mills (1973), suggesting that the experiments reported here were performed reliably. These bulk-water experiments suggest that the accuracy of the PFG NMR experiments is near  $10^{-11}$  m<sup>2</sup>/s.

The restricted diffusion regime is characterized by the  $\Delta$ -independence of *D*. Thus, comparison of the diffusivity obtained by small- and large- $\Delta$  experiments was performed to determine that the measured H<sub>2</sub>O diffusivity was under the regime. For example, measured *D* values at 39.7°C for  $\Delta = 14$  ms were 2.86, 2.63, and 2.41 × 10<sup>-9</sup> m<sup>2</sup>/s for w = 4.57, 7.24, and 11.0 wt. %, respectively (Table 1). The values for  $\Delta$ = 140 ms were 2.84, 2.67, and 2.39 × 10<sup>-9</sup> m<sup>2</sup>/s, respectively. They agree well with each other to within error, which suggests that the present NMR experiments are under the fully restricted diffusion regime.

In the restricted diffusion regime, the translational diffusivity is controlled by the complex and tortuous

structure of porous media as shown in Figure 5 (e.g., Latour et al., 1993). The migration distance (rootmean-square displacement) of random walkers in three-dimensional space is  $(6D\Delta)^{1/2}$  (e.g., Hollewand and Gladden, 1995). Because  $D = 0.5-5 \times 10^{-9} \text{ m}^2/\text{s}$ (Table 1) and  $\Delta = 14$  ms,  $(6D\Delta)^{1/2}$  is equal to 6-20 µm. This characteristic diffusion length in NMR experiments is several orders of magnitude longer than that in molecular-dynamic simulations and neutronscattering experiments. The measured diffusivity in the regime is a result of a random walk traveling a long distance compared to the pore size, d (e.g., Callaghan, 1991). Therefore, the average pore size of the gel structure of hectorite is  $\ll 6-20 \ \mu m$ . This may be a unique aspect of clay gel when compared with other gels, for example, polyacrylate (Zeng and Stejskal, 1996), agarose (Pavesi and Balzarini, 1996), and polyacrylamide (Pavesi and Rigamonti, 1995) for which d of a few tens of microns was found. As for the hectorite samples used here, the average grain diameter is  $0.054 \mu m$ . Probably the clay-gel pore size is also small (i.e., submicron) because the gel structure is constructed by the packing of the fine grains. Actually, Monma et al. (1997) reported pore diameters of  $<1 \mu m$  for w = 2 wt. % hectorite gel as produced by Kunimine Industries using Cryo-SEM (low vacuum scanning electron microscopy for water-rich samples). These results are consistent with the NMR data suggesting that  $d \ll 6-20 \ \mu\text{m}$ . Thus, for example, if  $d = 0.5 \ \mu\text{m}$  and  $(6D\Delta)^{1/2} = 10 \ \mu m$ , then the measured diffusivity by PFG NMR is the diffusivity of H<sub>2</sub>O molecules migrating by  $\sim 10/0.5 = 20$  pores.

The H<sub>2</sub>O self-diffusion coefficients, D, in the hectorite gel as a function of clay weight fraction, w, at various temperatures are shown in Figure 6 and Table 1. At all temperatures examined, D decreases with an increase in w. All D values in the clay are smaller than those in bulk water. At a high w, D is small because the H<sub>2</sub>O mobility is strongly restricted by densely packed clay-mineral grains (Figure 5). As w decreases, the density of obstacles (clay grains) for the random walk decreases, and thus H<sub>2</sub>O mobility increases. For a sample dominated by H<sub>2</sub>O, the H<sub>2</sub>O molecules diffuse as if they were in bulk water, and D approaches the diffusivity of bulk water.

A simple phenomenological equation relating w to D is proposed in the present study:

$$D/D_0 = \exp(-\alpha w) \tag{3}$$

where  $D_0$  is the diffusivity for bulk water at temperature,  $\alpha$  is a dimensionless constant, and w is a clay weight fraction (in wt. %). Equation (3) satisfies  $D = D_0$  at w = 0 wt. %. The fitting of Equation (3) to the data is shown in Figures 6 and 7 and each calculated  $\alpha$  value is listed in Table 2. Table 2 shows that  $\alpha$  is nearly independent of the sample temperature. As a result, a single temperature-independent master curve,



Figure 6. Self-diffusion coefficients of  $H_2O$  in hectorite gel, *D*, as a function of clay fraction, *w*, of the gel at various temperatures. Data are from Table 1. Data points are fitted to Equation (3) by a *least-squares* method. Temperatures in °C.

Equation (3), was determined (Figure 7). Low (1979) found that some properties (*e.g.*, viscosity of interlayer H<sub>2</sub>O) of montmorillonite/water systems were given by exp[cw/(100 - w)] where c was a numerical constant. The fit of the empirical equation of Low (1979) was



| Temperature (°C) | α      |  |
|------------------|--------|--|
| 20.0             | 0.0257 |  |
| 30.1             | 0.0259 |  |
| 39.7             | 0.0256 |  |
| 50.3             | 0.0259 |  |
| 60.3             | 0.0253 |  |
| average          | 0.0257 |  |

applied to the data of Table 1, but the fit is very unsatisfactory.

An Arrhenius plot of the diffusion data (Table 1) is shown in Figure 8. Activation energy, E, is calculated from

$$D = A \exp\left(-\frac{E}{RT}\right) \tag{4}$$

where A is a constant, R is the gas constant, and T is the absolute temperature. The activation energy of bulk water (18.1 kJ/mol; Table 1) for 20.0–60.3°C is nearly equal to the result of Mills (1973) of 17.6 kJ/ mol for the temperature range of 15–45°C, which suggests that the NMR experiments were performed in a reliable manner. Whereas the weak non-Arrhenius behavior of bulk water and clay gel was observed for a broader temperature range (2–225°C, Krynicki *et al.*, 1979; 4–55°C, Fripiat *et al.*, 1984), the Arrhenius fitting to Equation (4) in Figure 8 appears reasonable



Figure 7. Normalized diffusivity,  $D/D_o$ , (data identical to Figure 6) versus clay fraction, w. Data points are fitted to Equation (3) by a *least-squares* method ( $\alpha = 0.0257$ ). Note that the normalized diffusivity is independent of temperature. Equation (5) for  $\beta = 7.3$  and  $\rho_b/\rho_w = 2.3$  is indicated by a broken curve. Temperatures in °C.



Figure 8. Arrhenius plot of D for various clay fractions. The data set is from Table 1. Data points are fitted to Equation (4) by a *least-squares* method.

also, probably because of the narrow temperature range of the present study. Table 1 indicates that the activation energy for each hectorite gel sample nearly equals the value for bulk water. The temperature-in-dependence of  $D/D_0$  in Equation (3) is a consequence of this *w*-independence of E.

There are two possible reasons for  $D/D_0$  of less than unity for clay gels; bound or less mobile H<sub>2</sub>O molecules may occur near negatively charged clay surfaces and/or the geometrical complexity of the pore structure of clay gel through which H<sub>2</sub>O molecules migrate by random walk. (1) In the NMR experiments, H<sub>2</sub>O molecules travel sufficiently long distances  $[(6D\Delta)^{1/2} = 6-$ 20 µm] to experience the complex pore structure of the gel (Figure 5). Thus the complexity is a possible reason for the low H<sub>2</sub>O-diffusivity in clay gel. (2) The activation energy, E, for clay is nearly equal to that for bulk water (Table 1). This suggests that H<sub>2</sub>O molecules in the gel are in the same chemical environment as in bulk water, so the effects of structurally ordered H<sub>2</sub>O molecules near the clay surface are probably negligible. (3) The contribution of the low mobility of the bound H<sub>2</sub>O is negligible for H<sub>2</sub>O-rich clay gels (e.g., Kemper et al., 1964; Low, 1976, 1979; McBride, 1994). For example, the average  $H_2O$  viscosity in montmorillonite gels of w < 50 wt. % is nearly equal to the viscosity of bulk water [Equation (38) of Low, 1979]. This result occurs because the population of bound H<sub>2</sub>O is small compared to that of free water for water-rich gel. The viscosity is directly related to the diffusivity by the Stokes-Einstein relation. Hence, the contribution of the bound H<sub>2</sub>O to the average diffusivity of H<sub>2</sub>O in clay gel is also negligible for w < 50 wt. %. On the basis of the above (1-3), H<sub>2</sub>O diffusion measured by the present PFG NMR experiments is predominantly controlled not by the bound H<sub>2</sub>O but by the geometrical complexity of the hectorite gel structure.

The measured diffusivity in Table 1 is explained by a random-walk model. An exact solution of random walk in porous media under the restricted diffusion regime was determined by Netz and Dorfmüller (1997):

$$\frac{D}{D_0} = e^{-x} + x^2 e^x \int_{2x}^{\infty} \frac{e^{-y}}{y} dy$$
 (5)

where

$$x = \frac{4\pi r^3}{3} \left( \frac{N}{L^3} \right). \tag{6}$$

The quantity r is the radius of a spherical random walker (~0.15 nm for H<sub>2</sub>O; Krynicki *et al.*, 1979), N is the number of obstacles, and L is the system size. In the model, spherical random walkers migrate in three-dimensional space where infinitesimal point obstacles (with density of  $N/L^3$ ) are randomly placed. Effects of the adsorption of walkers on the obstacles are

neglected, so the only factor decreasing D is the geometrical complexity of the porous media. The average grain diameter, 0.054 µm, is much smaller than the characteristic diffusion length of H<sub>2</sub>O molecules, 6-20 µm. Thus, despite the plane or two-dimensional shape of clay platelets, this three-dimensional model is relevant. Because clay minerals are not infinitesimal and have finite volume, N is taken to be the number of spheres required to cover all clay grains by the equal spheres of radius r (see Figure 5, this is a 'random covering problem' in mathematics). Therefore N = $3\beta\phi L^3/(400\pi r^3)$  where  $\phi$  is the volume fraction of hectorite (vol. %) and  $\beta$  is the covering density. The quantity  $\phi$  is related to w:  $\phi = 100 w / [100 \rho_h / \rho_w + (1 - \rho_h / \rho_w)]$  $(\rho_w)w$ ] where  $\rho_h$  is the density of hectorite and  $\rho_w$  is the density of water. A reasonable value of  $\rho_{\rm h}/\rho_{\rm w}$  is 2.3 (e.g., Anthony et al., 1995). The numerical constant,  $\beta$ , was calculated by computer simulation as: (number of randomly scattered small equal circles required to cover a large square)  $\times$  (area of each circle)/(area of the square). Thus,  $\beta$  was estimated at 5–9. The parameter,  $\beta$ , has statistical ambiguity because the random covering process is stochastic. If  $\rho_h/\rho_w$  is equal to 2.3, the fit of Equation (5) to the obtained data is the best fit for  $\beta = 7.3$  (Figure 7), which falls in the estimated range of 5-9. Figure 7 indicates that the fit is good, particularly for w of <30 wt. %. When w increases to approach the percolation threshold, the randomly scattered spheres of radius r occupy nearly all of the threedimensional space, which isolates the pores (Trinh et al., 2000). This is the reason for the sharp drop of Equation (5) for w > 30 wt. %. On the other hand, three-dimensionally connected percolation clusters of the pore space for random walk survive in the real clay-gel system, even for high w, because the claymineral packing is not random in dense gel, but packing occurs with a 'card-house' structure. This structure may be the possible reason for the underestimate of  $D/D_0$  by Equation (5) for w > 30 wt. %. Except for the underestimate, however, the fit of Equation (5) to the NMR data is good. Thus, unbound H<sub>2</sub>O molecules diffuse by avoiding randomly placed clay grains for w of <30 wt. %.

The random-media model by Netz and Dorfmüller (1997) was successfully applied to the hectorite gel of w < 30 wt. %. The gel is characterized by high porosity which allows the approximations that (1) the effects of bound H<sub>2</sub>O are negligible and (2) the solid distribution is spatially random. Thus, the model is also applicable to other expandable smectite gels with a high water-fraction. PFG NMR enables us to perform quick, precise, and non-destructive measurements of the H<sub>2</sub>O mobility. The NMR technique contributes to the study of probing the porous structure of water-rich smectite gel systems.

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