

Diffusional and electrochemical investigation of combustion synthesized $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ titanate anode for rechargeable batteries

Anshuman Chaupatnaik and Prabeer Barpanda^{a)}

Faraday Materials Laboratory, Materials Research Centre, Indian Institute of Science, Bangalore 560012, India

(Received 1 June 2018; accepted 29 June 2018)

Energy-savvy auto-combustion synthesis was used to form the porous $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ titanate anode. It registered the lowest calcination temperature (800 °C) along with the shortest calcination duration (2 h). Rietveld analysis confirmed the purity of the orthorhombic (s.g. *Cmca*) product phase. The bond valence site energy analysis indicated a 1D ionic conduction along *c* axis with low activation energy and 2D pathways along (010) with high activation energy. AC conductivity analysis revealed a bulk conductivity of 2.41×10^{-4} S/cm (at 300 °C) with a moderate activation energy barrier (0.68 eV). From cyclic voltammetry, the Li^+ diffusion coefficient was calculated to be 10^{-11} – 10^{-12} cm^2/s . The as-synthesized $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ reversibly intercalated $\sim 1.3 \text{ Li}^+$ involving a 1.42 V $\text{Ti}^{4+}/\text{Ti}^{3+}$ redox activity delivering capacity ~ 100 mA h/g with good cyclability over 100 cycles. Furthermore, $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ was found to reversibly intercalate $\sim 0.89 \text{ Na}^+$. With suitable diffusional and electrochemical performance, $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ form a safe titanate anode for secondary batteries.



Prabeer Barpanda

Prabeer Barpanda is an Assistant Professor in the Materials Research Center at the Indian Institute of Science (IISc), Bangalore. He completed his B.Engg. from the National Institute of Technology Rourkela (NITR-India, 2002), M. Phil. from the University of Cambridge (U.K., 2004), and Ph.D. from Rutgers University, 2009. He pursued postdoctoral work under Prof. J.M. Tarascon (Universite de Picardie Jules Verne, France, 2009–2010) and with Prof. A. Yamada (The University of Tokyo, Japan, 2011–2013) with a JSPS fellowship. Prabeer's research revolves around synthesis, structural, and electrochemical study of novel materials for secondary Li-ion/ Na-ion batteries and supercapacitors. He has received several awards including the Ross Coffin Purdy Award (The American Ceramic Society), the ISE Prize for Applied Electrochemistry (International Society of Electrochemistry), the Energy Technology Division Young Investigator Award (The Electrochemical Society), and INSA Medal for Young Scientists (Indian National Science Academy). He directs the Faraday Materials Laboratory (FaMaL) at IISc. (<http://www.prabeer.in>)

I. INTRODUCTION

In the energy-hungry 21st century, sustainable energy 'generation' by renewable sources and efficient 'storage' for (mobile) distribution form two key technological sectors. Efficient energy storage can be realized by various electrochemical energy storage devices; batteries being the leader with their high gravimetric energy/power density and robust cyclability. The saga of batteries became popular with the commercialization of rechargeable Li-ion batteries by SONY[®] (Tokyo, Japan) (circa 1991) based on the intercalation reaction involving Li_xCoO_2 cathode and graphite anode.¹ Almost 40 years after the discovery of intercalation mechanism,² the internal design remains unaltered with various companies catering to the multibillion dollar battery market. Development of robust batteries

is a multiprong task, where anode (–ve electrode) plays an important role for safe operation.

In a sense, the successful commercialization of batteries can be rooted to the use of graphite anode versus a plethora of intercalation cathode materials. Graphite converts to LiC_6 via a staging intercalation process (at 0.2 V) delivering capacity over 372 mA h/g. However, graphite suffers from issues like irreversible Li loss owing to the formation of solid electrolyte interphase (SEI) and short-circuit related safety risks from low voltage dendrite formation at higher current or during over-discharge/over-lithiation. To overcome these issues, various Ti-based anode materials have been introduced.^{3,4} While spinel $\text{Li}_4\text{Ti}_5\text{O}_{12}$ has been commercialized,⁵ numerous titanate materials are widely being investigated. One such class of titanate anode family is $\text{MLi}_2\text{Ti}_6\text{O}_{14}$ ($\text{M} = 2\text{Na}, \text{Sr}, \text{Ba}, \text{Pb}$).^{6–10} Structurally, $\text{MLi}_2\text{Ti}_6\text{O}_{14}$ titanates have an orthorhombic (s.g. *Cmca*) framework built from layers of edge and corner

^{a)}Address all correspondence to this author.
e-mail: prabeer@iisc.ac.in
DOI: 10.1557/jmr.2018.250

connected TiO_6 octahedra along (100) with lithium atoms occupying vacancies within the TiO_6 framework.¹¹

In 1989, $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ was found by serendipity as a highly pure Li^+ conductive phase (4×10^{-3} S/cm at 300 °C, $E_a = 0.36$ eV) in the 20% Li_2O –73% TiO_2 –7% BaO ternary system.¹² Its crystal structure was reported in 2005 by Koseva et al.¹¹ $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ is capable of delivering high energy density with its high theoretical capacity (approximately 242.8 mA h/g) and a safe operating voltage ~ 1.4 V (versus Li). Following the initial reports by Belharouak and Amine,^{6,7} Shu group has systematically examined the $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ system by process/morphology optimization, doping, and conductive coating.^{13–17} They all involve aggressive heat treatment steps involving high calcination temperature (900–1100 °C), prolonged annealing (12–24 h), and expensive precursors. It makes the synthesis cumbersome that calls for alternate energy-miser synthesis methods.

Pursuing $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ titanate system, here we report a rapid solution combustion synthesis involving the lowest calcination temperature (approximately 800 °C) along with the shortest calcination duration of 2 h. We have investigated the Li^+ conductivity and migration pathways in $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ titanate by synergizing experimental ionic conductivity measurement with computational bond valence site energy (BVSE) calculations. It offers feasible Li^+ migration pathways suitable for battery anode application. The combustion synthesized barium lithium titanate delivers reversible capacity over 100 mA h/g in Li half-cell architecture. In addition, we have observed partial Na^+ (de)intercalation in $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ for the first time. With its open structure, one-dimensional diffusion pathways with moderate energy barrier, and intermediate voltage safe operation, combustion-made $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ forms a robust anode for secondary batteries.

II. MATERIALS AND METHODS

A. Combustion synthesis

The $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ target product was prepared via a two-step solution combustion method using low-cost metal nitrates as the oxidizer and glycine as fuel. Titanyl nitrate [$\text{TiO}(\text{NO}_3)_2$] was prepared in-house using acid hydrolysis.¹⁸ Under ice-cold condition and constant stirring, 3 mL (6 moles) of titanium isopropoxide ($\text{C}_{12}\text{H}_{28}\text{O}_4\text{Ti}$, Sigma, St. Louis, Missouri, 97%) was added to 9 mL of isopropyl alcohol (Merck & Co., Kenilworth, New Jersey, 99.7%). 3 mL of 1:1 v/v diluted HNO_3 (Merck, 69%) was added dropwise to form a clear titanyl nitrate solution. After sonication for 20 min, stoichiometric amounts of $\text{Ba}(\text{NO}_3)_2$ (Sigma, >99%), LiNO_3 (Sigma, 99%), and glycine ($\text{C}_2\text{H}_5\text{NO}_2$, Merck, 99.7%) were added to the titanyl nitrate solution. Upon heating this precursor solution at 140 °C, a thick white mixture was formed after evaporation of excess water. It

was transferred to a hot plate maintained at 500 °C. It triggered the exothermic combustion reaction forming an amorphous intermediate complex. It was mildly ground and was calcined at 800 °C for 2 h (in air) to obtain the final titanate product. The type of fuel, stoichiometry of the lithium precursor, and calcination temperatures were optimized after extensive trials.

B. Physical characterization

Powder X-ray diffraction patterns of pristine and electrochemically cycled samples were acquired with a PANalytical Empyrean X-ray diffractometer (PANalytical, Malvern, UK) equipped with a Cu K_α source ($\lambda_1 = 1.54$ Å, operating at 40 kV/30 mA). Typical patterns were collected in the 2θ range of 10–90° (step size = 0.026°/s). Rietveld refinement was performed using GSAS program using EXPGUI graphical user interface.^{19–21} The surface morphology was examined with an FEI Quanta 200 scanning electron microscope (FEI, Hillsboro, Oregon) having a tungsten source operating at 20–25 kV. The structure and morphology were further analyzed with an FEI Technai F 30 STwin transmission electron microscope operating at 200 kV. For TEM, the powder sample was dispersed in ethanol and was deposited on a holey carbon–copper grid. Brunauer–Emmett–Teller (BET) surface area analysis using surface adsorption of N_2 (at 77 K) was performed with a Belsorp Max unit (MicrotracBEL Corp., Krefeld, Germany). Raman spectra were collected with a HORIBA JobinYvon LabRAM HR spectrometer (Horiba Ltd., Kyoto, Japan) using a 532 nm laser source.

C. AC conductivity measurement

The ionic conductivity as a function of temperature was measured using AC impedance spectroscopy. The combustion synthesized titanate powder was pressed into pellet ($\Phi = 15$ mm) by applying 55 kN uniaxial pressure. This pellet was densified by sintering at 800 °C for 12 h and its relative density ($\rho_{\text{exp}}/\rho_{\text{true}}$) was determined by the Archimedes principle. Silver paste was coated on both sides serving as an electronic conductor while blocking the ionic exchange. AC impedance analysis was performed with an Agilent 4194 A HP impedance analyzer (Agilent Technologies, Santa Clara, California) in the frequency range of 40 Hz–100 MHz in the temperature range of 200–300 °C. The impedance spectra were analyzed using ZView impedance data analyzer software.

D. Computational methods

Lithium-ion occupancy in vacant sites in $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ and corresponding migration barrier values were calculated based on the BVSE method.^{22–24} $E_{\text{BVSE}}(\text{Li})$ identifies regions of low BVSE that connect to form migration pathways for mobile lithium ions. As demonstrated by Adam et al., the mismatch $|\Delta V|$ of bond

valence $s_{\text{Li-X}} = \exp [(R_{0,\text{Li-X}} - R_{\text{Li-X}})/b_{\text{Li-X}}]$ can be favourably scaled down to absolute energies by rewriting bond valence into a Morse-type interaction potential between the reference cation Li⁺ and anion X.

$$E_{\text{BVSE}}(\text{Li}) = \sum_x D \left[\sum_{i=1}^N \left(\left(\frac{s_{\text{Li-X}}}{s_{\text{min, Li-X}}} \right)^2 - 2 \frac{s_{\text{Li-X}}}{s_{\text{min, Li-X}}} \right) \right] + E_{\text{repulsion}} \quad (1)$$

The required parameters were taken from the *softBV* database.²⁴ The structure model was constructed with the refinement of atomic coordinates obtained from the experiment. Grids covering this structure model with a resolution of (0.1) Å³ was used while calculating $E_{\text{BVSE}}(\text{Li})$.

E. Electrochemical characterization

For battery testing, the working electrode was prepared by making a slurry of active material, polyvinylidene fluoride binder, and Super P carbon black (80:10:10 w/w) in minimal amount of *N*-methyl-2-pyrrolidone (Sigma, >99%) solvent. This slurry was uniformly coated on copper current collector ($\Phi = 12$ mm) and was dried in vacuum to remove the NMP solvent. The typical active material loading was ~ 3 mg/cm². For battery testing, CR2032-type coin cells were assembled inside an Ar-filled glove box (MBraun LabStar GmbH, Garching, Germany) to avoid any moisture contamination. Coated disks and Li metal foils (Sigma) were used as the working and counter electrodes, respectively, separated by two sheets of Whatman GF/C glass fiber separator soaked with 100 μL of 1 M LiPF₆ dissolved in 1:1:3 v/v % of ethylene carbonate/propylene carbonate/dimethyl carbonate (EC/PC/DMC) acting as the electrolyte. Sodium half cells were assembled in a similar fashion by using Na metal foil as the counter electrode and 1 M NaPF₆ dissolved in 1:1 v/v % of ethylene carbonate/diethylene carbonate (EC:DEC) acting as the electrolyte. These coin cells were subjected to galvanostatic cycling at different rates ($C/20 \sim 3C$) in the potential window of 0.5–2 V (at 25 °C) with VMP3 or BCS-805/810 (Bio-Logic SAS, Seyssinet-Pariset, France) battery cyler. The capacity and C rate values were calculated keeping in mind the theoretical capacity of BaLi₂Ti₆O₁₄ (242.8 mA h/g) based on six electron/lithium transfer.

F. Ex-situ characterization

Ex-situ electrochemical and Raman analyses were performed by using Swagelok type Teflon-aluminum cells. Swagelok cells were stopped at different states of charge/potentials in the 1st cycle (1.3 V, 0.5 V, 1.5 V, and 2 V). Complete phase formation at the stopping

potentials was ensured by keeping the cell at a constant voltage until current decayed to half ($C/20$). Postcycling, the Swagelok cells were opened inside the glove box, and the electrodes were washed with propylene carbonate solvent and were vacuum dried for 12 h for further analysis.

III. RESULTS AND DISCUSSION

A. Structure and morphology

For combustion synthesis of BaLi₂Ti₆O₁₄ titanate, several trials were made to optimize the amount of lithium precursor, fuel, pre-calcination temperature, and final calcination temperature. To compensate for possible lithium volatilisation at high temperature, a slightly excess amount (0–5%) of lithium precursor can be used. Varying the Li precursor content, the final BaLi₂Ti₆O₁₄ product was formed along with impurities like Li₄Ti₇O₁₆, BaTiO₃, and TiO₂ (Supplementary Material, Fig. S1). Using a pre-calcination temperature of 500 °C and final annealing at 800 °C, the phase pure titanate product was obtained. Despite several attempts, we were unable to get pure titanate phase by combustion synthesis employing alternate fuels such as ascorbic acid, citric acid, stearic acid, sucrose, and urea. The exothermicity of the combustion reaction can be altered by varying the oxidant to fuel ratio. In the current work, stoichiometric amounts of Ba/Li/Ti precursors (as oxidants) and glycine (as fuel) were used involving the final annealing at 800 °C for 2 h.

Rietveld refinement confirmed the phase purity of combustion synthesized BaLi₂Ti₆O₁₄ ($\chi^2 = 3.82\%$, R factor = 6.69%) (Fig. 1). When compared to solid-state synthesis involving 950 °C calcination for 12 h, solution

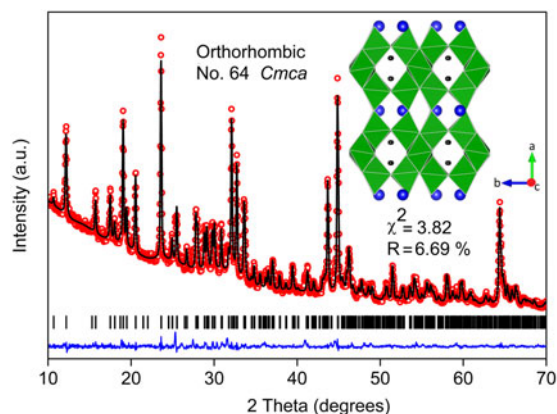


FIG. 1. Rietveld refinement of XRD (Cu K_α) pattern of BaLi₂Ti₆O₁₄ formed by solution combustion synthesis. The experimental data points (red hollow dots), calculated pattern (black line), their difference (blue line), and Bragg reflections of the orthorhombic *Cmca* phase (black bars) are shown. The inset shows the crystal structure along *c* axis of the refined cell having partly filled Li tunnels surrounded by rutile tunnels transversely reinforced by TiO₆ pairs (green). (Ba = blue balls, TiO₆ octahedra = distorted green squares, and Li = black balls).

TABLE I. Crystallographic parameters determined by the Rietveld refinement of high-resolution XRD data ($\lambda = 1.5418 \text{ \AA}$) of BaLi₂Ti₆O₁₄ at 25 °C. (U_{iso} = equivalent isotropic displacement parameters) (BVS = bond valence sum).

Formula [molecular weight, g/mol]		BaLi ₂ Ti ₆ O ₁₄ [662.6]						
Crystal system		Orthorhombic						
Space group		<i>Cmca</i> (#64)						
Unit cell parameter (Å)		$a = 16.565, b = 11.266, c = 11.584, Z = 8$						
Unit cell volume (Å ³)		2161.769						
Theoretical density (g/cm ³) ^a		4.072						
Reliability factors & goodness of fit values		$R_p = 4.3\%, \text{RF} = 6.69\%, \chi^2 = 3.824\%$						
Global instability index (GII) ^b		0.147259						
Atom	Site	<i>x</i>	<i>y</i>	<i>z</i>	Occupancy	U_{iso}	BVS	
Li	16g	0.1890	0.2442	0.1215	1	0.0156	0.97	
Ba	8f	0.0000	0.3539	0.1192	1	0.0076	2.11	
Ti(1)	8e	0.2500	0.4975	0.2500	1	0.0060	4.55	
Ti(2)	8d	0.2395	0.5000	0.0000	1	0.0056	3.99	
Ti(3)	16g	0.1118	0.1290	0.3596	1	0.0059	3.89	
Ti(4)	16g	0.1095	0.3847	0.3867	1	0.0057	3.88	
O(1)	16g	0.2412	0.3883	0.3742	1	0.0061	-2.08	
O(2)	16g	0.1385	0.4972	0.2572	1	0.0068	-2.07	
O(3)	16g	0.2322	0.1143	0.3705	1	0.0059	-2.17	
O(4)	8d	0.1284	0.0000	0.5000	1	0.0074	-1.96	
O(5)	8d	0.1312	0.0000	0.0000	1	0.0075	-2.03	
O(6)	16g	0.1218	0.2531	0.2645	1	0.0072	-1.91	
O(7)	8f	0.0000	0.1057	0.3824	1	0.0083	-2.00	
O(8)	16g	0.1123	0.2481	0.4817	1	0.0070	-1.92	
O(9)	8f	0.0000	0.4058	0.3705	1	0.0089	-1.86	

^aThe high calculated theoretical density (4.09 g/cm³) in BaLi₂Ti₆O₁₄ can favor high tap density energy density.

^bGII is the root mean square bond valence mismatch of the bond valence sums.

combustion synthesis yielded the desired titanate with the lowest reported calcination temperature (800 °C) and calcination duration (2 h). This titanate stabilizes into an orthorhombic crystal structure (symmetry: *Cmca*) with lattice parameters $a = 16.565(2) \text{ \AA}$, $b = 11.265(5) \text{ \AA}$, and $c = 11.584(0) \text{ \AA}$ similar to earlier reports.^{6,13} The atomic coordinates and bond valence sums of all atoms gave a GII value of 0.147(2) in agreement with the value of 0.102(8) found for single crystal literature data. It validates the stability of the chemical environment of the refined structural model for further study. Table I lists the crystallographic parameters, atomic coordinates, and bond valence sum values obtained from Rietveld refinement.

The three-dimensional framework of BaLi₂Ti₆O₁₄ is built from layers TiO₆ octahedra having tunnels partly filled with Li ions. One set of TiO₆ octahedra containing Ti(1) and Ti(2) share opposite edges of their equatorial plane to form a rutile-like chain along *c* direction. Another similar set of TiO₆ octahedra reinforce these rutile chains by alternately sharing adjacent edges along *b* and *c* axis. It forms corner-sharing blocks of 3 edge-sharing TiO₆ octahedra (along *a* direction) having zig-zag tunnels partially filled with Li ions. Barium atoms occupy 11 coordinated 8f sites between the layers. Despite high unit cell volume, mean Ba–O bond distance (2.87 Å) in

our case was similar to the value (2.889 Å) obtained from the single crystal study,¹¹ both of which were significantly lower than the sum of the ionic radii (2.97 Å). This stems from the residual compressive strain, which was further validated by a high bond valence value of Ba (2.11) (Table I).

The short annealing time led to less aggressive grain growth so as to form small primary particles in the size range of 150–300 nm (Fig. 2). They agglomerated to form secondary micrometric (<5 μm) particles. Characteristic to combustion reaction involving gaseous by-products, porous morphology was developed that can be beneficial for electrolyte wetting and efficient Li⁺ diffusion (with shorter diffusion length) during battery cycling. The BET specific surface area was found to be ~8 m²/g (Supplementary Material, Fig. S2). HRTEM images [Fig. 2(f)] show ($\bar{1}\bar{1}\bar{1}$) plane with a dislocation-free interplanar spacing of 7.1725 Å. The corresponding selected area diffraction pattern [SAED, Fig. 2(h)] confirmed phase purity with distinct points indexed to [$\bar{1}\bar{1}\bar{1}$] zone axis. Figure 2(g) shows (311) and (112) planes with an interplanar spacing of 4.54 Å and 4.94 Å, respectively. Due to their small difference, several edge dislocations can be seen. Elemental mapping [Fig. 2(j)] showed a uniform distribution of constituent Ba, Ti, and O elements in BaLi₂Ti₆O₁₄ titanate.

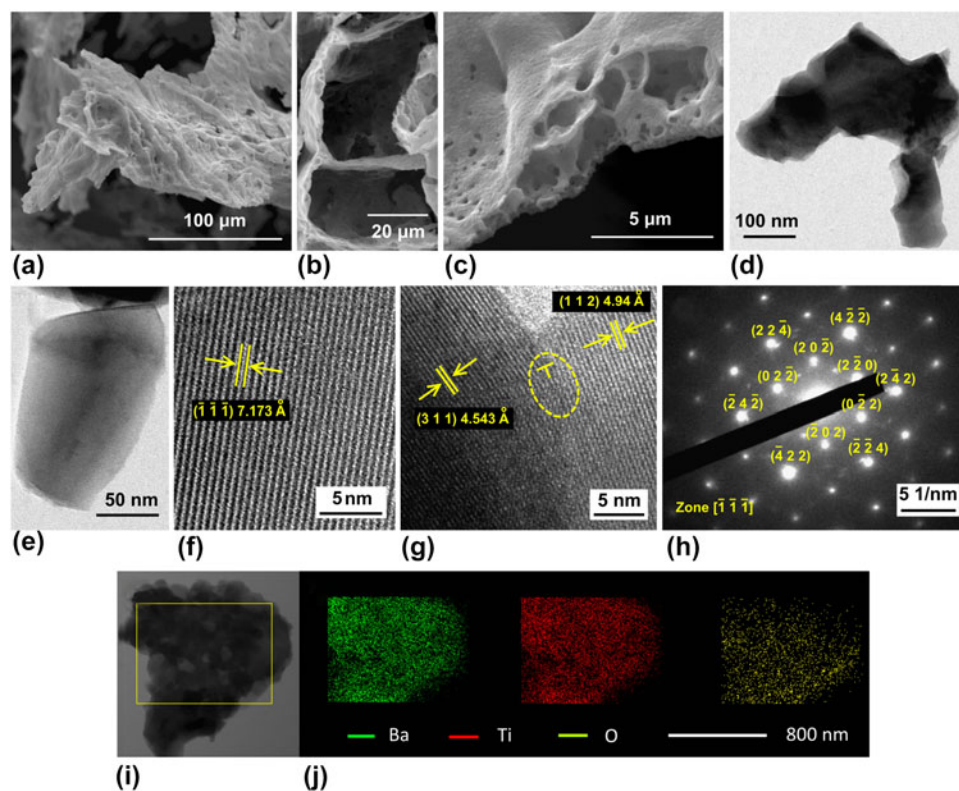


FIG. 2. (a–c) SEM images of as-prepared $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ showing porous morphology. (d and e) TEM images indicating nanometric particle size. (f and g) High resolution TEM images showing fringes indexed to atomic plane and dislocations showing extra half plane at the interface between two planes. (h) SAED pattern indexed to the orthorhombic $Cmca$ crystal structure. (i and j) Bright field STEM images and elemental mapping showing homogenous distribution of barium, titanium, and oxygen.

B. BVSE analysis

During lithiation, $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ reduces one (or more) Ti from Ti^{4+} to Ti^{3+} while intercalating $x\text{Li}^+$ to form $\text{BaLi}_{2+x}\text{Ti}_6\text{O}_{14}$. It involves diffusion of Li^+ ions that is controlled by the crystal structure and surrounding potential. As Li^+ ions intercalate at $x = 0$ in $\text{BaLi}_{2+x}\text{Ti}_6\text{O}_{14}$ proceeding through partially delithiated structures ($0 < x < 6$), the chemical environment around Li^+ gets gradually modified and determines its iterative distribution and movement. The key is to build an accurate lowest energy chemical environment from experimentally reliable and a hence relevant local structure consisting of refined atomic positions. Environment modeling can be done using several ways such as computationally expensive ab initio methods. Similar results can be obtained by using simpler BVSE calculations.^{22–24} BVSE method, working on force field of the chemical environment, intuitively identifies interstitial or vacancy sites of the lowest BVSE of lithium ($E_{\text{BVSE}} \text{Li}^+$), stitching them by intersite hopping barrier energies into one or multidimensional threads of lithium ion migration pathways. Based on blocking due to defects/impurity or change of barrier energies with composition x , different pathways can activate. For consistency, migration pathways found by

computationally expensive ab initio methods have been found to match those by the bond valence approach in suites of electrode materials.

In the pristine delithiated state ($x = 0$), tunnels directed along c axis host 16 Li^+ ions (2 per formula unit as $Z = 8$) completely occupying single 16 g empty tetrahedral sites, along with two interstitial sites i2 and i3. These tunnels are created by TiO_6 rutile chains interconnected alternately above and below by sets of edge-sharing TiO_6 blocks (Fig. 1, inset). Inside the tunnels, along with i2 and i3 sites, Li1 sites form a one-dimensional (1D) zigzag migration pathway Li1-i2-Li1-i3 that interconnect to neighboring 1D channels by Li1-i4-Li1 2D paths forming a two-dimensional (2D) network spread in the ac or (010) plane [Fig. 3(a) showing isosurface as pathways along with position of the environmentally most perturbing ion]. The 2D nets are linked in the bc plane (100) by Li1-i3-i3-Li1 three dimensional (3D) paths [Fig. 3(b)]. For a clearer understanding, complete Li^+ ion migration pathways overlapping with the crystal structure is illustrated in Fig. 3(c).

From the energy plot in Fig. 3(d), it can be seen that i2 and i3 interstitials have dissimilar site energies unlike the case of $\text{SrLi}_2\text{Ti}_6\text{O}_{14}$.⁹ Despite the compressive strain of

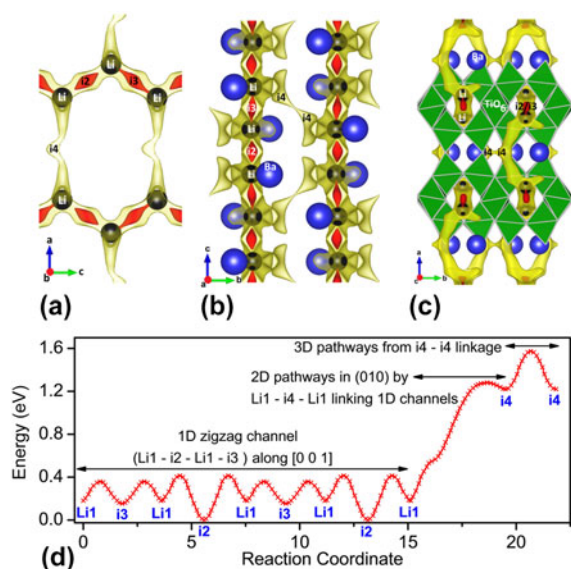


FIG. 3. BVSE model showing lithium ion migration pathways in $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$. The pathways shown are two isosurfaces (red and yellow) (a) (010) plane having one dimensional and two dimensional paths involving i_2 , i_3 , and i_4 interstitials in half of the unit cell (to avoid overlap), (b) (100) plane having three dimensional pathways through i_4 and (c) (001) plane showing 1D path running along the lithium filled tunnel, rutile chain (one labelled TiO_6), and (d) energy landscape showing migration barriers across different interstitials connected 1D, 2D, and 3D paths. The barrier for i_3 access by $\text{Li}1$ is smaller than i_2 , hence as the energy corresponding to the isosurface in red is enough for i_3 access but just exceeds the i_2 barrier, i_2 is not connected to lithium while i_3 is. All illustrations have been presented using VESTA.²⁵

the M (M = Sr/Ba) atom in $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ (bond valence of Ba = 2.11) that is absent in $\text{SrLi}_2\text{Ti}_6\text{O}_{14}$ (bond valence of Sr = 1.75), the larger ionic size of Ba significantly increases the b and c lattice parameters in comparison to a . Ba is closer towards the i_2 site while being far and opposite from i_3 . This smaller Ba- i_2 distance [Fig. 3(a)] increases the i_2 energy significantly from i_3 . Hence the 2D links are difficult to operate in the case of Ba with only one interstitial as compared to two interstitials in Sr. Concomitant to the case of Sr, with BVSE ignoring the mobile Li-Li repulsions, though interstitials i_2 and i_3 exist at energies much lower than $\text{Li}1$, stay unfilled because of $\text{Li}1$ stabilization in i_1 by reduced repulsion among mobile Li^+ ions. (The nomenclature is i_x if the site is unfilled and Li_x if the site is filled by Li).

The migration pathways calculated for $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ have low barriers of 0.414 eV for 1D links with higher barriers of 1.281 and 1.574 eV for the 2D and 3D links [Fig. 3(d)]. Hence, most likely it is a one-dimensional ionic conductor, rarely activating the 2D and 3D pathways in cases when 1D pathways are blocked. It is in contrast to isostructural $\text{SrLi}_2\text{Ti}_6\text{O}_{14}$ which is at discretion to freely use 1D, 2D, and 3D pathways with barrier energies lower than 0.69 eV making it a 3D ion

conductor. Following the energy landscape, a maximum of four Li^+ will insert sequentially in i_3 , i_2 , i_4 , and i_5 sites, each of which can hold one lithium. This is if progressive lithium insertion does not drastically energize the chemical environment. Otherwise, based on the lowest energy at that composition, Li^+ ions will dynamically rearrange altering the energy landscape. Overall, $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ was found to be a one-dimensional Li^+ conductor. The ionic conductivity was further analyzed by experimental ac conductivity measurement as described below.

C. AC (ionic) conductivity

Unlike graphitic anode where Li^+ ions intercalate along with electrons without reducing anything, ionic conductivity is important in anodes involving transition metal ions. Ionic conductivity is more important than electronic conductivity as diffusion governs/limits the rate of (de)lithiation during battery cycling. Ionic conductivity was measured using $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ pellets having 94.24% (3.83 g/cm^3) of theoretical density (4.069 g/cm^3). Figure 4(a) shows the high temperature complex Nyquist plots from 200 to 300 °C at intervals of 10° C taken to understand the process involved during ionic conduction and correlate it with that obtained from the earlier BVSE analysis. For temperatures up to 250 °C, depressed semicircles were observed. A tail at the low-frequency end suddenly appeared in Nyquist plots above 250 °C indicating fast ion mobility which gets blocked as ionic charges accumulate at the sample-electrode interface. All depressed semicircles diminished at higher temperatures indicating an increase in conductivity.

The observed values were fitted to an equivalent circuit consisting of a pair of parallel Debye-like resistor-constant phase element (representing impedance contribution from grain and grain boundary) and a constant phase element (representing the impedance contribution from the electrode-grain interface) connected in series. Though semicircles of impedance spectra seem as a single depressed semicircle, two overlapping semicircles from grain contribution at higher frequency and grain boundary contribution at lower frequency regions exist, which can be resolved slightly more clearly at higher temperatures. This difficulty in resolution indicates overlapping time constants for grain and grain boundary relaxation. The bulk resistance R was calculated from a parallel combination of resistance values of grain (R_g) and grain boundary (R_{gb}) obtained after fitting. Bulk conductivity (σ) in S/cm was calculated using $\sigma = 1/\rho = l/(R \times A)$, where l is the thickness of the pellet and A is the disc area of the pellet in cm. The grain, grain boundary, and bulk conductivity at 300 °C were $2.16 \times 10^{-4} \text{ S/cm}$, $2.44 \times 10^{-5} \text{ S/cm}$, and $2.41 \times 10^{-4} \text{ S/cm}$, respectively. The activation energy for ion movement was calculated from

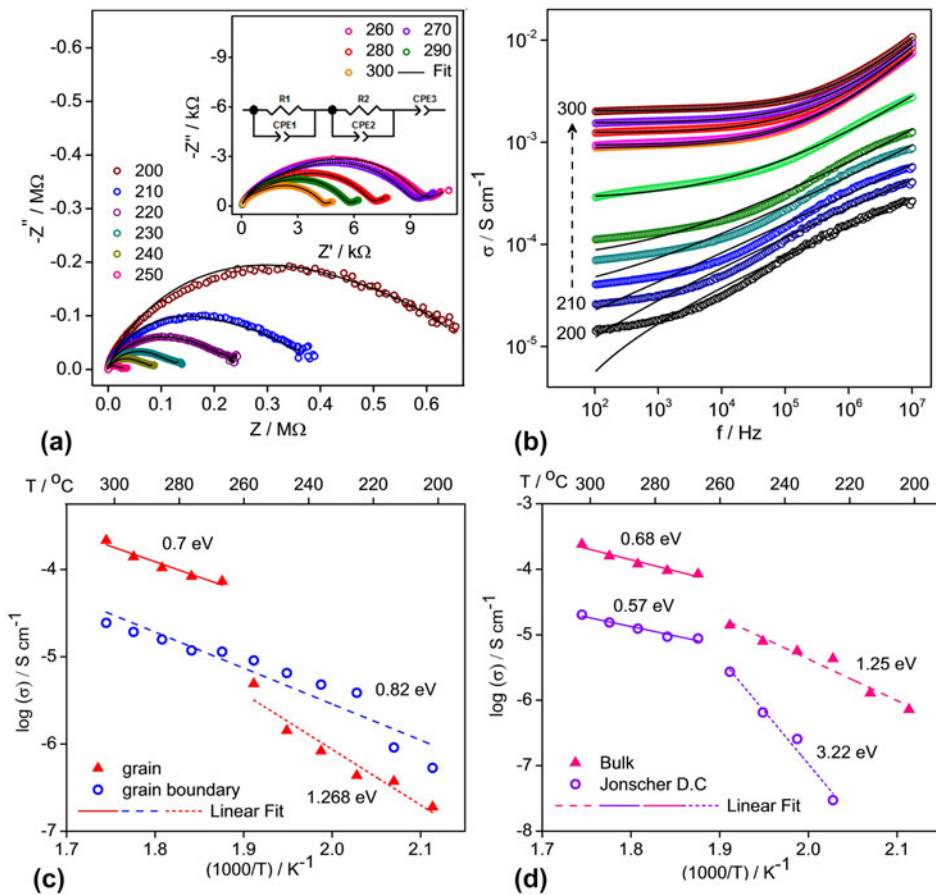


FIG. 4. Electrical measurements of AC conductivity. (a) Complex impedance plots for BaLi₂Ti₆O₁₄ recorded in the frequency range of 40 Hz–110 MHz at high temperatures and the corresponding fit, using ZView, as per the equivalent circuit in the inset. (b) AC conductivity versus frequency and fit based on Jonscher’s power law. The individual resolved and combined bulk resistance values from fits in (a) and Jonscher’s dc conductivity values from fits in (b) have been used to calculate the activation energy in graphs (c) and (d).

Arrhenius relation of the temperature dependence of dc conductivity:

$$\sigma = A_0 \exp\left(-\frac{E_a}{kT}\right) \quad (2)$$

where A_0 is the pre-exponential factor, E_a is the activation energy in eV, k is the Boltzman’s constant in eV/K, and T is the temperature in K.

The individual grain and grain boundary conductivity values (in S/cm) at different temperatures obtained after fitting the impedance spectra have been plotted versus $1000/T$ [Fig. 4(c)]. The grain conductivity shows a large jump above 250 °C with a corresponding change in slope while the grain boundary conductivity follows a single trend. Two temperature regions of grain and entire temperature region of grain boundary conductivity were fitted. Grain boundary activation energy of 0.82 eV was obtained. Grain activation energy corresponding to 0.7 and 1.268 eV for high and low temperature regions was found. It indicates the occurrence of an internal switch in

ionic conduction mechanism within the grain from 2D to 1D, increasing ion mobility, possibly from clearing away of defects in the 1D pathways at a higher temperature. It is justified from an excellent agreement of the activation energy obtained from BVSE where calculated values for the 1D path (0.414 eV) match the high-temperature values (0.7 eV), while values for the 2D path (1.281 eV) match the low-temperature values (1.268 eV) of grain conductivity.

Figure 4(b) shows the variation of ac conductivity with frequency at 10 °C intervals from 200 to 300 °C. AC conductivity increases with an increase in temperature indicating higher mobility, while at temperatures above 240 °C, it varies with frequency as per Jonscher’s universal dielectric response depicting localized ionic motion.²⁶

$$\sigma(\omega) = \sigma_{dc} + A\omega^n \quad (3)$$

where σ_{dc} is the low frequency or dc conductivity, A is the preexponential temperature-dependent factor, and n is the degree of interaction between mobile ions. Solid

black lines in Fig. 4(b) show the fitting of experimental data to Jonscher's law at each temperature from which the magnitudes of n and σ_{dc} are obtained. Plotted versus $1000/T$ [Fig. 4(d)], the Jonscher's dc conductivity σ_{dc} shows a sharp change in slope at 250 °C. The activation energies of Jonscher's dc and bulk conductivity are 0.57 and 0.68 eV at high temperature and 3.22 and 1.25 eV at low temperature. Except for the low temperature value of Jonscher's dc conductivity, the change of activation energy signals a change in ion conduction mechanism from 2D to 1D as discussed earlier.

D. Electrochemical performance

The diffusion behavior in BaLi₂Ti₆O₁₄ was further analyzed by cyclic voltammetry (CV). Figure 5(a) shows potentiostatic cyclic voltammograms at scan rates ranging from 0.1 to 1 mV/s. Pristine BaLi₂Ti₆O₁₄ reduces while intercalating Li⁺ at 1.37–1.29 V (R1) and 1.16–1.11 V (R2) and oxidizes while deintercalating Li⁺ at 1.17–1.28 V (O1) and 1.48–1.55 V (O2). O1 can be resolved to two peaks which merge at higher scan rates. Figure 5(b) shows the variation of current for four redox peaks (R1, R2, O1, and O2) with square root of the scan rate in (V/s)^{0.5}. Linearly fit with zero intercepts R1, R2, O1, and

O2 gave slopes of -0.076 , -0.028 , 0.030 , and 0.109 , respectively. These slopes were used to calculate the diffusion coefficient as per Randal Sevchik equation.²⁷

$$i_p = 2.69 \times 10^5 \times n^{1.5} A D^{0.5} C v^{0.5} \quad (4)$$

where the i_p , n , A , D , C , and v represent the peak current in A, number of electrons utilized in the peak, electrode area of 2.324 cm², diffusion coefficient in cm²/s, the concentration of the diffusing ion for each peak in mol/cm³, and scan rate in V/s. C is the concentration of lithium ion in a unit cell of BaLi₂Ti₆O₁₄. For 1 Li⁺ ion in a unit cell, C is the ratio of moles of Li to the volume of the unit cell (2164.17 Å³) calculated from refinement, i.e., 0.006137 mol/cm³. C can then be written as

$$C = 0.006137(\# \text{ of Li}^+) \text{ mol/cm}^3 \quad (5)$$

All Li⁺ ions in the unit cell are considered. This includes pre-existing two lithium ions in BaLi₂Ti₆O₁₄ in addition to n lithiums exchanged corresponding to n electrons during the redox process. The reason why the two pre-existing structural lithiums are included is because the BVSE analysis confirmed their mobility as

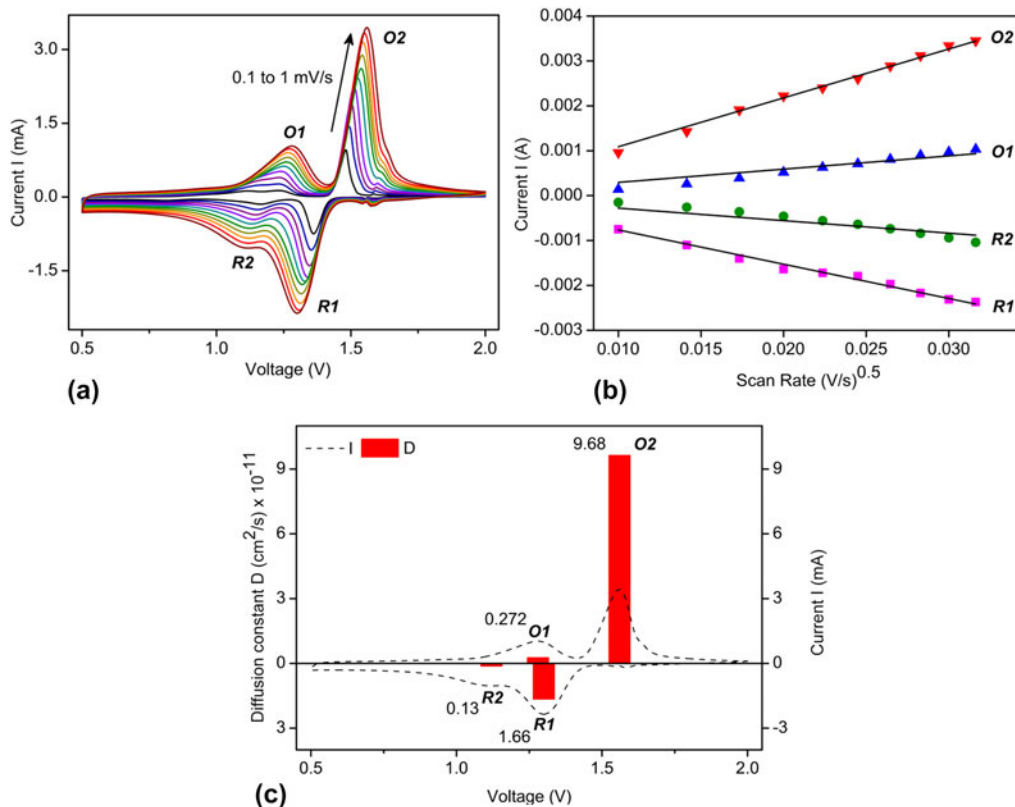


FIG. 5. (a) CV of BaLi₂Ti₆O₁₄ versus lithium half-cell cycled at current rates from 0.1 to 1 mV/s. Four distinct redox peaks were observed named as R1, R2, O1, and O2 in the sequence of their appearance. (b) Linear fit of the four peak currents to square root of the scan rate. (c) Schematic of calculated diffusion coefficient from slope obtained from fits in (b).

they were part of 1D migration pathways having a low energy barrier of 0.414 eV. The number of electrons, n , at each peak depends on the number of Li^+ ions exchanged during that peak. n for R1 and O2 is assumed to be 1.28 based on the intake of around 52 mA h/g observed in 1st charge at 1.41 V in $4a/4b/8c$ sites as discussed later. Similarly, n for R2 and O1 is assumed to be 1.24 based on 50 mA h/g charge capacity stored in the slopes other than during and after the plateau in the 1st charge. Thus, the cumulative numbers of lithium ions present in the unit cell in R1, R2, O1, and O2 are 3.38 (2 + 1.28), 4.62 (2 + 1.28 + 1.24), 3.38 (4.62 - 1.24), and 2 (3.38 - 1.28). Although the O1 and R2 peaks are smaller than the sharp peaks, the area under the curve remains the same confirming equal charge exchange (close to 1.3 lithiums). Based on the above discussions, the diffusion coefficients of lithium ions at R1, R2, O1, and O2 are compared in Fig. 5(c). It is highest for the O2 peak as it has the least number of lithiums (2) amongst all redox peaks.

Diffusion coefficient values in the range of 10^{-11} to 10^{-12} cm^2/s [Fig. 5(c)] were obtained for combustion prepared $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$. The ionic diffusivity can be enhanced by four standard ways: (i) changing crystallinity, (ii) doping, (iii) conductive coating, and (iv) particle downsizing. Combustion synthesis delivers carbon-coated small particles, which is favorable to obtain high diffusion coefficient. Following the diffusion analyses, the electrochemical performance was measured in standard Li- and Na-half-cell architectures.

The galvanostatic voltage–capacity profiles of combustion-made $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ are shown in Fig. 6 cycled (i) at $C/10$ rate between a narrow potential window (1–2 V) and (ii) at $C/20$ rate between a wider potential window (0.5–2 V). In the former case, out of 120 mA h/g stored in the first cycle, 16 mA h/g was lost to the parasitic reaction, 62.6 mA h/g (1.55 Li^+) was stored in the $4a/4b/8c$ sites at 1.41 V (inset) while 41 mA h/g (1 Li^+) was stored in the vacant 8f sites. In the

subsequent cycles, out of 87 mA h/g (2.12 Li^+) extracted during the first charge, 53 mA h/g (1.3 Li^+) could be extracted at 1.41 V [the inset of Fig. 6(a)] from the partly lithium filled $4a/4b/8c$ sites. Excellent capacity retention was recorded for over 120 cycles.

When cycled in the wide 1.5 V potential window (0.5–2 V), the first discharge of 176 mA h/g was observed [the inset of Fig. 6(b)], out of which the first 17 mA h/g (0.4 Li^+) was lost to the parasitic reaction, next 63 mA h/g (1.57 Li^+) was stored in vacant $4a/4b/8c$ sites of lithium tunnels at 1.41 V while remaining 96 mA h/g (2.38 Li^+) was stored collectively at (i) 2 different voltage regions in 8f sites and (ii) consumed to possible SEI formation. 111 mA h/g of capacity (2.75 Li^+) could be extracted in the first charge, out of which only 51.78 mA h/g (1.28 Li^+) could be removed at 1.43 V (low polarization of 0.02 V) from the partly filled $4a/4b/8c$ sites. 78% of total first charge capacity (87 mA h/g or 2.12 Li^+) could be retained or reversibly extracted in the 50th charge cycle [Fig. 6(b) inset]. These results indicated (a) the same 1.3 Li^+ can be extracted in the first plateau independent of potential window indicating reversibility in $4a/4b/8c$ sites remains unaffected and (b) reducing lower cut-off voltage significantly affects Li^+ reversibility/capacity retention whose origins could be gradual lithium loss to unstable SEI formation and/or trapping in the inherent weakly reversible 8f sites.

Following, the rate performance of combustion prepared $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ was assessed by varying the current rate from $C/10$ to $3C$. The corresponding capacity retention and voltage–capacity profiles are summarized in Fig. 7. Charge capacities of 96 mA h/g (2.38 Li^+), 80 mA h/g (1.98 Li^+), 71 mA h/g (1.76 Li^+), 64 mA h/g (1.58 Li^+), 58 mA h/g (1.44 Li^+), and 55 mA h/g (1.36 Li^+) were recorded at C rates of $C/10$, $C/5$, $C/2$, $1C$, $2C$, and $3C$, respectively. Charge capacity reverted back to 77 mA h/g (1.9 Li^+) upon decreasing the C rate to $C/5$.

Overall, the electrochemical performance of $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ prepared using rapid solution combustion

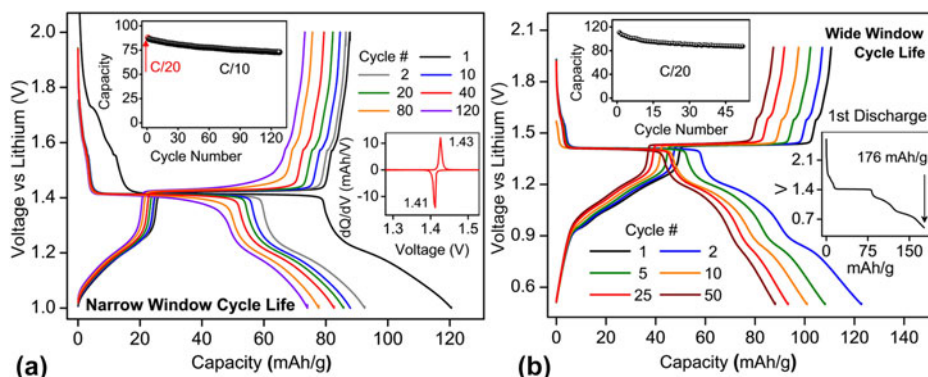


FIG. 6. Cycle life performance of $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ versus lithium (a) at $C/10$ rate for a narrow voltage window of 1–2 V and (b) at $C/20$ for a wider voltage window of 0.5–2 V. A $C/20$ slow formation cycle precedes both tests. The insets show capacity retention, dQ/dV versus V , and first cycle losses.

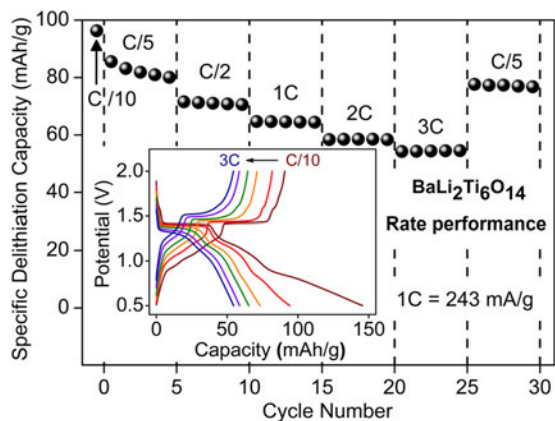


FIG. 7. Rate performance of $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ versus lithium at higher current rates up to 3C (726 mA/g). The inset shows voltage profile and their polarization at different C rates.

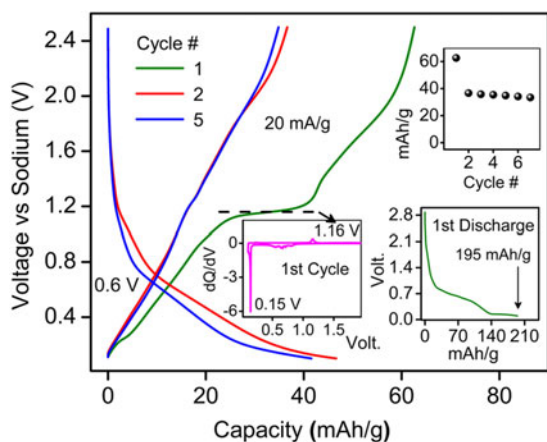


FIG. 8. Sodium activity in $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ at 20 mA/h/g in 1 M NaPF_6 in 1:1 EC:DEC in the voltage range of 0.1 and 2.5 V. The inset shows capacity retention, first cycle loss, and dQ/dV versus V.

synthesis was better than solid-state prepared $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ without ball milling. It could be due to the formation of smaller particles with porous morphology. In our case, the electrochemical performance can be further improved by ball milling, doping (that improves electronic conductivity), and process optimization (co-fuel/oxidant-fuel ratio) until it can fully utilize the 1D low energy pathways.

Following the efficient (de)lithiation, the presence of open channels inspired us to gauge possible (de)insertion of Na^+ ions into $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$. When cycled in a Na half-cell architecture, we observed reversible Na^+ insertion for the first time (Fig. 8). The first discharge capacity was 195 mA h/g (4.83 Na^+ insertion) with a plateau ~ 0.15 V. In the subsequent cycles, a reversible capacity of 36 mA h/g (0.89 Na^+) was observed with an average redox potential of 0.6 V. This preliminary result hints at the use of $\text{MLi}_2\text{Ti}_6\text{O}_{14}$ family of compounds for sodium-ion insertion with proper material optimization.

IV. CONCLUSIONS

Barium lithium titanate ($\text{BaLi}_2\text{Ti}_6\text{O}_{14}$) was prepared by solution combustion synthesis by employing the lowest reported calcination temperature (approximately 800 °C) and soaking duration (approximately 2 h). The purity of titanate product was confirmed by Rietveld and electron microscopy analyses. The Li^+ diffusivity was measured synergizing BVSE computation, impedance spectroscopy, and CV. BVSE analysis revealed lower activation energy barrier for 1D (0.414 eV) migration along *c* axis and higher activation energy barrier for 2D (1.281 eV) and 3D (1.574 eV) pathways. AC conductivity analysis showed a Jonscher's type of behavior with a bulk conductivity value of 2.41×10^{-4} S/cm (at 300 °C) with an activation energy barrier of 0.68 eV. CV calculated the diffusion coefficient in the range of 10^{-11} – 10^{-12} cm^2/s . With this feasible Li^+ migration, reversible Li^+ (de)intercalation was noticed in the combustion synthesized $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ titanate involving a 1.4 V $\text{Ti}^{4+}/\text{Ti}^{3+}$ redox activity along with decent rate kinetics and cycling stability. Furthermore, reversible Na^+ (de)intercalation (0.89 Na^+) was observed for the first time. Combustion synthesis is proposed as a rapid and scalable synthesis route to form a variety of titanate anodes for secondary batteries.

ACKNOWLEDGMENTS

AC thanks the Ministry of Human Resource Development (MHRD, Govt. of India) for financial assistance. PB acknowledges the Department of Atomic Energy (DAE, Govt of India) for a DAE-BRNS Young Scientists Research Award (YSRA). The authors thank Professor Stefan Adams for his scientific help with BVSE analysis. The current work was financially supported by the Indian National Science Academy (INSA/CMR/PBB/0021).

REFERENCES

1. J.B. Goodenough and K. Park: The Li-ion rechargeable battery : A perspective. *J. Am. Chem. Soc.* **135**, 1167 (2013).
2. M.S. Whittingham: Electrical energy storage and intercalation chemistry. *Science* **192**, 1126–1127 (1976).
3. Z. Chen, I. Belharouak, Y.K. Sun, and K. Amine: Titanium-based anode materials for safe lithium-ion batteries. *Adv. Funct. Mater.* **23**, 959 (2013).
4. G.N. Zhu, Y.G. Wang, and Y.Y. Xia: Ti-based compounds as anode materials for Li-ion batteries. *Energy Environ. Sci.* **5**, 6652 (2012).
5. T. Ohzuku, A. Ueda, and N. Yamamoto: Zero-strain insertion material of $\text{Li Li}_{1/3}\text{Ti}_{5/3}\text{O}_4$ for rechargeable lithium cells. *J. Electrochem. Soc.* **142**, 1431 (1995).
6. D. Dambournet, I. Belharouak, and K. Amine: $\text{MLi}_2\text{Ti}_6\text{O}_{14}$ (M = Sr, Ba, 2Na) lithium insertion titanate materials: A comparative study. *Inorg. Chem.* **49**, 2822 (2010).
7. I. Belharouak and K. Amine: $\text{Li}_2\text{MTi}_6\text{O}_{14}$ (M = Sr, Ba): New anodes for lithium-ion batteries. *Electrochem. Commun.* **5**, 435 (2003).

8. S. Ghosh, Y. Kee, S. Okada, and P. Barpanda: Energy-savvy solid-state and sonochemical synthesis of lithium sodium titanate as an anode active material for Li-ion batteries. *J. Power Sources* **296**, 276 (2015).
9. A. Dayamani, G.S. Shinde, A. Chaupatnaik, R.P. Rao, S. Adams, and P. Barpanda: Electrochemical and diffusional insights of combustion synthesized $\text{SrLi}_2\text{Ti}_6\text{O}_{14}$ negative insertion material for Li-ion batteries. *J. Power Sources* **385**, 122 (2018).
10. P. Li, S. Qian, H. Yu, L. Yan, X. Lin, K. Yang, N. Long, M. Shui, and J. Shu: $\text{PbLi}_2\text{Ti}_6\text{O}_{14}$: A novel high-rate long-life anode material for rechargeable lithium-ion batteries. *J. Power Sources* **330**, 45 (2016).
11. I. Koseva, J.P. Chaminade, P. Gravereau, S. Pechev, P. Peshev, and J. Etourneau: A new family of isostructural titanates, $\text{MLi}_2\text{Ti}_6\text{O}_{14}$ ($M = \text{Sr}, \text{Ba}, \text{Pb}$). *J. Alloys Compd.* **389**, 47 (2005).
12. W.J. Zheng, R. Okuyama, T. Esaka, and H. Iwahara: Ionic conduction in the sintered oxides of the system $\text{Li}_2\text{O}-\text{BaO}-\text{MO}_2$ ($M = \text{Ti}, \text{Sn}, \text{Zr}$). *Solid State Ionics* **35**, 235 (1989).
13. X. Lin, P. Li, L. Shao, M. Shui, D. Wang, N. Long, Y. Ren, and J. Shu: Lithium barium titanate: A stable lithium storage material for lithium-ion batteries. *J. Power Sources* **278**, 546 (2015).
14. H. Yu, M. Luo, H. Lan, L. Yan, S. Qian, W. Ye, M. Shui, N. Long, and J. Shu: Comparative study of $\text{Pb}_{1-x}\text{Ba}_x\text{Li}_2\text{Ti}_6\text{O}_{14}$ ($0 < x < 1$) as lithium storage materials for secondary batteries. *J. Power Sources* **357**, 179 (2017).
15. W. Tao, M-L. Xu, Y-R. Zhu, Q. Zhang, and T-F. Yi: Structure and electrochemical performance of $\text{BaLi}_{2-x}\text{Na}_2\text{Ti}_6\text{O}_{14}$ ($0 \leq x \leq 2$) as anode materials for lithium-ion battery. *Sci. China Mater.* **60**, 728 (2017).
16. X. Lin, S. Qian, H. Yu, L. Yan, P. Li, Y. Wu, N. Long, M. Shui, and J. Shu: Advanced $\text{BaLi}_2\text{Ti}_6\text{O}_{14}$ anode fabricated via lithium site substitution by magnesium. *ACS Sustainable Chem. Eng.* **4**, 4859 (2016).
17. H. Yu, L. Yan, S. Qian, P. Li, H. Lan, H. Zhu, N. Long, M. Shui, and J. Shu: Fabrication of $\text{Ba}_{0.95}\text{M}_{0.05}\text{Li}_2\text{Ti}_6\text{O}_{14}$ ($M = \text{Ag}, \text{Pb}, \text{Al}$) as high performance anode candidates for lithium secondary batteries. *Electrochim. Acta* **228**, 453 (2017).
18. S-L. Chung and C-M. Wang: Solution combustion synthesis of TiO_2 and its use for fabrication of photoelectrode for dye-sensitized solar cell. *J. Mater. Sci. Technol.* **28**, 713 (2012).
19. H.M. Rietveld: A profile refinement method for nuclear and magnetic structures. *J. Appl. Crystallogr.* **2**, 65 (1969).
20. A.C. Larson and R.B. Von Dreele: *General Structure Analysis System (GSAS)*; Report LAUR 86-748; Los Alamos National Laboratory, New Mexico, 2000.
21. B.H. Toby: EXPGUI, a graphical user interface for GSAS. *J. Appl. Crystallogr.* **34**, 210 (2001).
22. S. Adams and R.P. Rao: Transport pathways for mobile ions in disordered solids from the analysis of energy-scaled bond-valence mismatch landscapes. *Phys. Chem. Chem. Phys.* **11**, 3210 (2009).
23. S. Adams and R.P. Rao: High power lithium ion battery materials by computational design. *Phys. Status Solidi* **208**, 1746 (2011).
24. H. Chen and S. Adams: Bond softness sensitive bond-valence parameters for crystal structure plausibility tests. *IUCrJ* **4**, 614 (2017).
25. K. Momma and F. Izumi: VESTA: A three-dimensional visualization system for electronic and structural analysis. *J. Appl. Crystallogr.* **41**, 653 (2008).
26. A.K. Jonscher: Dielectric relaxation in solids. *J. Phys. D: Appl. Phys.* **32**, R57 (1999).
27. N. Ding, J. Xu, Y.X. Yao, G. Wegner, X. Fang, C.H. Chen, and I. Lieberwirth: Determination of the diffusion coefficient of lithium ions in nano-Si. *Solid State Ionics* **180**, 222 (2009).

Supplementary Material

To view supplementary material for this article, please visit <https://doi.org/10.1557/jmr.2018.250>.