



Impact dynamics of compound drops of fluids with density contrast

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The dynamics of compound drops impacting on a flat substrate is numerically investigated using a ternary-fluid diffuse-interface method, with the aim of assessing the effect of a density difference between the inner and outer droplets (denoted by λ) on the evolution of the interfaces. With the help of numerical simulations, we find that, at the intermediate stage of drop impact, the inner droplet exhibits a self-similar deformation at $\lambda = 1$ and relatively high Weber number, and experiences more or less a uniform acceleration for various λ . In particular, the acceleration magnitude at $\lambda \neq 1$ can be correlated with the acceleration at $\lambda = 1$ and the Atwood number. When the inner droplet is denser than the outer one, a lamella occurs at the spreading front of the inner droplet. We present a scaling analysis of the thickness of the lamella, and the resultant theoretical prediction is in good agreement with numerical results. At the maximal spreading of the compound drop, a bulging structure is formed around the symmetry axis due to the presence of the inner droplet, thereby effectively reducing the liquid supply to the spreading front and leading to a decrease of maximal spreading ratio β_{max} as compared with a pure drop. We proposed a corrected Weber number We_{λ}^* by taking account of the combined effects of λ , volume fraction of the inner droplet, Weber number and morphology of the compound drop. Integrating We_1^* with the universal model of β_{max} for impacting pure drops, we successfully build up a new model for predicting the maximal spreading ratio of impacting compound drops with various λ .

Key words: drops, contact lines

1. Introduction

Impact of compound drops on a solid substrate can be widely seen in industrial processes, such as ink-jet printing (Derby 2010; Wijshoff 2018; Lohse 2022), tissue construction (Murphy & Atala 2014; Hendriks *et al.* 2015) and microcapsule collection in pharmacy

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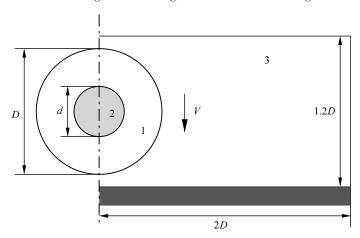


Figure 1. A sketch of a compound drop impacting onto a horizontal substrate at a vertical velocity V. The diameters of the outer and inner droplets of the compound drop are D and d, respectively. The simulations are performed in cylindrical coordinates (r, z), with z = 0 being the substrate.

(Delcea, Mohwald & Skirtach 2011; De Cock et al. 2010; Liu et al. 2018a). In these industrial processes, the compound drops consist of an outer (or shell) droplet and one/multiple inner (or core) droplets, and the inner droplets are encapsulated by the outer one. To optimize the processes requires us to gain insights into the impact dynamics of compound drops, especially the deformation of the inner droplet and the spreading of the whole compound drop at various impact conditions. Similar to impacting pure drops (Yarin 2006; Josserand & Thoroddsen 2016), the dynamics of impacting compound drops is affected by impact velocity V, surface tension γ , drop size D, wettability of the solid wall and the material properties of the liquid. For compound drops, the differences in fluid properties between the inner and outer droplets, e.g. the volume ratio (α) , surface tension ratio (η) , viscosity ratio and density ratio (λ) of the inner droplet to the outer one, are also expected to influence the flow features of drop impact. Therefore, the impact dynamics of compound drops is much more complicated than that of pure drops. A schematic diagram of compound drops impacting onto a substrate is shown in figure 1. Two dimensionless parameters are usually used to describe the impact dynamics of compound drops, i.e. the Weber number $We (= \rho_1 V^2 D/\sigma_{13})$ and the Reynolds number $Re (= \rho_1 V D/\mu_1)$, where ρ_1 and μ_1 are the density and viscosity of the shell liquid, respectively, and σ_{13} denotes the surface tension coefficient between the shell fluid and surrounding air.

The presence of inner droplets gives rise to fascinating flow phenomena during the impact processes. Gulyaev & Solonenko (2013) observed the occurrence of a counter-jet rising vertically along the centre line of the drop in the experimental investigation of hollow glycerin drops impacting onto a solid surface. Liu & Tran (2018) revealed in experiments that the change of the volumetric oil ratio in compound drops consisting of water and silicone oil might lead to the transition from spreading to splashing. Moreover, they also reported the emergence of two spreading lamellae, which significantly affect the overall spreading behaviour. Later, they further investigated the splashing dynamics of impacting compound drops (Liu & Tran 2019). Blanken *et al.* (2020) experimentally found that, for an impacting compound drop consisting of core water droplet and oil shell, the core water droplet could rebound from the surface below a threshold impact velocity; they attributed this phenomenon to the lubrication from the oil shell that prevents the contact between the water core and the substrate. Zhang, Li & Thoroddsen (2020) reported

the occurrence of fine radial jets near the substrate in the impact of a compound drop containing a number of emulsion droplets. The formation of these radial jets results from the local focusing of the outer liquid, which is forced into the narrowing wedge under each internal droplet.

Numerical simulations have also been used to investigate the impact dynamics of compound drops. Tasoglu et al. (2010) studied the deformation and spreading of compound drops at relatively low We (\sim 0.5–10) and Re (\sim 15–45) using a front-tracking method, to model the printing of droplet-encapsulated biological cells. Liu et al. (2018b) investigated the maximal spreading ratio of impacting compound drops with equal density (i.e. $\lambda = 1$) at moderate Reynolds and Weber numbers (Re = 1000 and $10 \le We \le 800$), with a focus on the effect of α and η . Based on the morphology of the compound drop at maximal spreading, they identified two flow regimes, i.e. jammed spreading (at small α) and joint rim formation (at relatively large α), which differ in that the inner droplet does not participate in the rim formation of the compound drop in the former while it does in the latter. A universal rescaling of impacting compound drops was then proposed with a corrected Weber number that takes α , η and the flow regime into account. Wei & Thoraval (2021) simulated the impact dynamics of an air-in-liquid compound drop with various α . They observed that the addition of a bubble in the drop decreases its maximal spreading, and attributed this to the decrease of the kinetic energy of the drop and the formation of a vertical jet at its centre. A recent review on impacting compound drops can be found in Blanken et al. (2021).

Despite of this research on compound drops impacting onto a flat substrate, the density effect on the interaction between the inner and outer interfaces of the compound drops remains unclear. Also, it is important in practice to understand how the density difference between the inner and outer droplets affects the deformation and motion of the inner droplet, and the overall spreading behaviour of whole compound drops.

In this paper, we numerically investigate the dynamics of compound drops impacting onto a flat substrate, aiming to evaluate the effect of λ on the evolution of the interfaces. For this purpose, we perform axisymmetric simulations using a ternary-fluid diffuse-interface method, in the parameter space of We = 50-500, $\lambda = 0.001-4$, $\alpha = 0.027-0.216$ and Re = 1000. We examine the temporal evolution of the inner and outer interfaces, and assess the interaction between the inner and outer droplets at different stages of drop impact. Based on the numerical results, we characterize the motion and deformation of the inner droplet at various λ , and establish a new universal model for the maximal spreading ratio of impacting compound drops.

2. Problem statement and methodology

2.1. Problem statement

We consider here the axisymmetric impact of a compound drop onto a rigid smooth substrate, as shown in figure 1. The compound drop consists of two concentric droplets, with diameters denoted by d (for the inner droplet) and D (for the outer droplet), respectively. The density and viscosity of the fluids are defined as ρ_i and μ_i , where the subscript i denotes the respective fluid (i = 1, 2 or 3). The surface tension coefficient between fluid i and j is represented by σ_{ij} . We assume that the compound drop is made of liquids of low viscosity. For convenience of study, the following parameters are fixed: Re = 1000, $\rho_3/\rho_1 = 0.001$, $\mu_2/\mu_1 = 1$, $\mu_3/\mu_1 = 0.025$ and the ratio of the inner and outer interfacial tension coefficient $\sigma_{12} = \sigma_{13}$. Then, we restrict our study to the variation of We (or surface tension coefficients), density ratio $\lambda = \rho_2/\rho_1$ and volume ratio

 $\alpha=(d/D)^3$, with a focus on the effect of the density and size of the inner droplet on the dynamics of impacting compound drops. To avoid very strong coupling between the inner and outer interfaces from the very beginning of drop impact, we only consider relatively small α , ranging from 0.027 to 0.216. Such a numerical set-up is relevant to real physical conditions. For example, if water is taken as the shell fluid, Re=1000 corresponds to a millimetre-sized drop with impact velocity of O(1) m s⁻¹. Accordingly, the gravity effect is negligibly small compared with the acceleration encountered in the drop impact $(\sim V^2/D)$; for example, the Froude number $Fr=V^2/gD$ is of the order of 10^2 , where g is the gravitational acceleration. Unless stated otherwise, the diameter of the compound droplet D is chosen as the unit length, the time is made dimensionless by the scale D/V and the time t=0 refers to the moment when the compound drop comes into contact with the substrate.

In the present study, the core droplet hardly comes into contact with the solid surface during the spreading of the compound drop, primarily owing to the lubrication effect of the liquid film under it (Blanken *et al.* 2020). It should also be noted that there is no splashing of the shell droplet in the range of parameters considered. Therefore, the wetting dynamics is mainly determined by the contact angle θ_{13} , i.e. the angle at which the interface between fluids 1 and 3 intersects with the substrate. In particular, we consider a superhydrophobic substrate with a fixed $\theta_{13} (= 150^{\circ})$, while θ_{12} and θ_{23} are set to 150° and 90°, respectively. Given σ_{12} , σ_{13} , θ_{12} , θ_{13} and θ_{23} , the surface tension coefficient σ_{23} can be uniquely determined (Zhang *et al.* 2016), specifically, here, $\sigma_{23} = 2\sigma_{13}$.

A ternary-fluid diffuse-interface model is used to simulate the impact dynamics of compound drops (Zhang et al. 2016). The same method has been used previously to investigate the maximal spreading of impacting compound drops with $\lambda=1$ (Liu et al. 2018b), i.e. the shell and core liquids have the same density. In the method, a cylindrical coordinate system (r, z) is adopted to simulate the flow dynamics in a computational domain of $2D \times 1.2D$ on a uniform Cartesian mesh. A no-slip condition and the geometric moving contact line model are imposed at the substrate (z=0), a symmetry condition at r=0 and a far-field boundary condition at the right and upper boundaries. Initially, the compound drop is located above the substrate with a distance of 0.1D, and then descends with velocity of V, while the surrounding air is assumed to be stationary.

2.2. Convergence study

We simulate the impact dynamics of a compound drop at We=500, $\alpha=0.064$ and $\lambda=0.1$, to check the convergence of the numerical results. Figure 2 shows snapshots of the compound drop at the dimensionless time t=0.5 on successively refined meshes, where the mesh sizes are $\Delta x=0.004$, 0.002 and 0.001. It is clear that the numerical results converge with the mesh refinement, in terms of the drop shape. The numerical results with $\Delta x=0.002$ are nearly overlapping with those on the finest mesh $\Delta x=0.001$. We also examine the convergence of the maximal spreading ratio β_{max} , which is the diameter ratio of the wetted area at the maximal spreading to the initial compound drop. Table 1 shows the variation of β_{max} for the different meshes, where the difference decreases with mesh refinement. In particular, the relative error ϵ between the meshes $\Delta x=0.002$ and 0.001 becomes rather small ($\epsilon=0.24\%$). Therefore, a Cartesian mesh with mesh size of $\Delta x=0.002$ is used in the following studies.

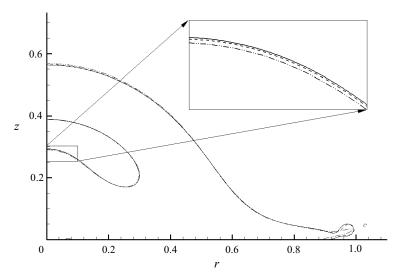


Figure 2. Convergence study with respect to the drop shape at the dimensionless time t=0.5 with We=500, $\alpha=0.064$ and $\lambda=0.1$. Different curves denote the numerical results with different mesh resolutions: $\Delta x=0.004$ (dash-dot-dotted), 0.002 (dashed) and 0.001 (solid). The inset shows a zoomed-in view of the interface near the bottom of the inner droplet.

Mesh size (Δx)	β_{max}	ϵ
0.004	3.1220	1.04 %
0.002	3.1471	0.24 %
0.001	3.1548	

Table 1. Convergence study on successive refined meshes.

3. Results and discussion

3.1. Impact dynamics of compound drops

Figure 3 shows the snapshots of impacting compound drops with a fixed volume fraction $(\alpha=0.064)$ and Weber number (We=500), but different density ratios $(\lambda=0.1,\ 1$ and 4), where the results of a pure drop $(\alpha=0)$ are included for a comparison of the dynamic process. The dynamics of the impacting compound drops is shown in the three supplementary movies available at https://doi.org/10.1017/jfm.2023.388. At the early stage of drop impact $(t \le 0.5)$, the outer interfaces of all the impacting compound drops have a close resemblance to that of the pure drop. There is little interaction between the inner and outer interfaces at this stage, primarily because the distance between the two interfaces remains relatively large. By contrast, the effect of different λ can be clearly seen in the movement of the inner droplets: the larger λ is, the lower the location the inner droplet reaches. In addition, the inner droplet with $\lambda=0.1$ has a concave bottom at t=0.25, while those with $\lambda \ge 1$ have a convex one. At this stage, the inner and outer interfaces of the impacting compound drops appear to evolve independently.

At the intermediate stage of drop impact (e.g. $0.5 < t \le 1$), the downward motion of the compound drop pushes the inner droplet further towards the substrate; at the same time, the distance between the inner and outer interfaces is gradually shortened. As a result, the

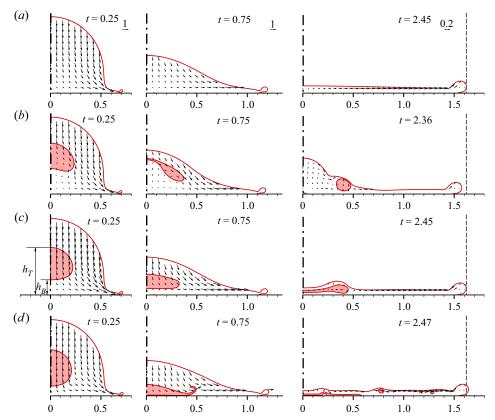


Figure 3. Snapshots of an impacting pure drop at We = 500 (a) and impacting compound drops at $\alpha = 0.064$, We = 500 and various density ratios λ : 0.1 (b), 1 (c) and 4 (d). The columns from left to right correspond to the results at the time t = 0.25, 0.75 and t_{max} , where t_{max} denotes the moment when the drop reaches its maximal spreading. In each column, the reference velocity vectors are the same and are shown at the upper-right corner in (a). The numbers above the arrows indicate the values of the reference vector.

effect of λ becomes noticeable in this stage: an upward liquid counter-jet is induced at the bottom of the light inner droplet ($\lambda=0.1$), thereby hindering the descending of the outer interface near the symmetry axis to some degree (see the second image of figure 3b). By contrast, the dense inner droplet ($\lambda=4$) apparently impacts onto the substrate (with no formation of contact lines), and spreads over a thin film of fluid 1, with its front rolling up (see the second image of figure 3d). At the intermediate stage, the deformation of the inner droplet starts to affect the evolution of the outer interface.

At the late stage of drop impact, e.g. at the moment of maximal spreading t_{max} , the maximal spreading ratio of the compound drop, β_{max} , depends on the value of λ . For the case with $\lambda=0.1$, the inner droplet is penetrated by the induced liquid counter-jet, and evolves into a donut-like shape; subsequently, a recirculation zone occurs at the centre of the compound drop. As a result, the supply of fluid 1 is restricted from the central region to the front of spreading, thereby making its β_{max} smaller than the pure drop. By contrast, such an effect of flow restriction is much weaker in the case with $\lambda=1$. Therefore, the compound drop with $\lambda=1$ has almost the same β_{max} as the pure drop. For the case with large $\lambda(=4)$, the liquid film beneath the inner droplet breaks up and forms a ring on the substrate, while the rolling-up part of the inner droplet pinches off and expands

radially outwards. The dense inner droplet provides extra momentum to the spreading of the compound drop, which is responsible for the larger β_{max} than that of the pure drop.

It is clear from the observation of numerical results above that the density contrast of the compound drop plays an important role in the evolution of the inner droplet, which in turn affects the maximal spreading ratio of the whole compound drop. In the following, we will further investigate the dynamic behaviours of the inner interface with different λ (in § 3.2), and quantitatively assess the effect of the density contrast on the maximal spreading ratio (in § 3.3).

3.2. Evolution of the inner interface

3.2.1. Uniform acceleration and self-similar interface evolution at $\lambda = 1$

In this section, we study the motion of the inner droplet at the early stage of drop impact and interface evolution at the intermediate stage for compound drops with equal density $(\lambda = 1)$. The interface of an impacting drop can be represented by the vertical component of its position vector z = h(r, t). To examine the motion of the inner droplet, we track the vertical positions of its centroid (denoted by h_C), as well as the top and bottom of the inner droplet at the symmetry axis (denoted by h_T and h_B , respectively; see the first image in figure 3c). The temporal evolutions of h_T , h_B and h_C are shown in figure 4 for an impacting compound drop at We = 500, $\alpha = 0.064$, $\lambda = 1$ and various $\alpha = 0.027$, 0.064 and 0.125). We find that the inner droplet experiences a uniform acceleration a at the early stage, in the sense that h_C can be approximated by

$$h(0,t) = h(0,0) - t + \frac{1}{2}a_0t^2, \tag{3.1}$$

where h(0,0) is the initial position and $a_0 = aD/V^2$ denotes the dimensionless acceleration. Moreover, the trajectories of h_C are the same for three different α (so as to give a constant $a_{0,C} = 1.5$ for $0 \le t \le 0.4$ by data fitting), which suggests that the motion of the inner droplet does not depend on α at the early stage of drop impact.

Interestingly, the time variations of h_T and h_B in figure 4(a-c) follow a manner very similar to h_C , and can also be described by (3.1). For example, in the case of $\alpha = 0.064$, we can obtain $h_T|_{t=0} = 0.7$ and $h_B|_{t=0} = 0.3$ from the initial set-up, and the acceleration at the top of the inner droplet $a_{0,T} = 0.83$ and that at the bottom $a_{0,B} = 3.5$ by data fitting; here, the duration of acceleration depends on the vertical location, and $0 \le t \le 0.5$ at the top and $0 \le t \le 0.2$ at the bottom of the inner droplet. That is, the acceleration at the bottom of the inner droplet is much higher than its top, which accounts for its gradual flattening with time. The difference between $a_{0,T}$ and $a_{0,B}$ is found to increase with α , e.g. $a_{0,B} = 4.8$ and $a_{0,T} = 0.75$ for $\alpha = 0.125$ while $a_{0,B} = 2.8$ and $a_{0,T} = 0.95$ for $\alpha = 0.027$. Such an acceleration process is not contradictory with zero acceleration at the drop apex at the early stage of impact of pure drops (Eggers *et al.* 2010). Figure 4(*d*) shows the trajectories of drop apex of the impacting compound drops for $\alpha = 0.027$, 0.064 and 0.125. We can see that all the trajectories generally overlap and, moreover, have nearly zero acceleration until $t \approx 0.2$, at which time the pressure gradient arising from drop impact starts to affect the drop apex; see e.g. figure 5.

The motion of the inner droplet is closely related to the pressure distribution inside the compound drop. Figure 5 shows the pressure contours at the early stage of drop impact (from t = 0.05 to 0.30), with $\lambda = 1$, We = 500 and $\alpha = 0.064$. Firstly, once the drop comes into contact with the substrate, we can see that a high pressure zone is instantaneously established in the vicinity of the impact region, and the inner droplet is immediately surrounded by vertical pressure gradients. After this, the high pressure zone

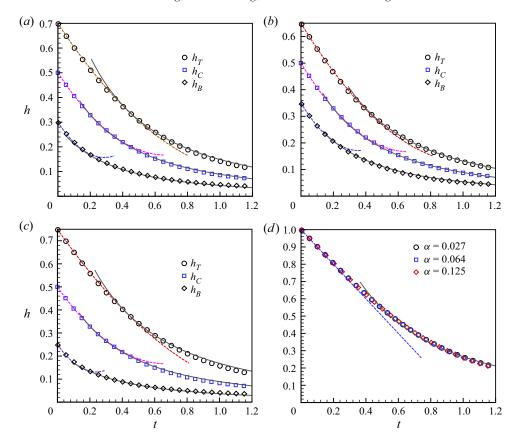


Figure 4. Motion of the inner droplet in terms of time variation of h_C , h_T and h_B , with We = 500, $\lambda = 1$ and various α : (a) $\alpha = 0.064$, (b) $\alpha = 0.027$ and (c) $\alpha = 0.125$. The dashed lines represent the prediction of (3.1), and the solid lines correspond to the prediction of (3.5). (d) Evolution of the apex of the compound droplets, where the dashed line represents the prediction of (3.1) with zero acceleration.

expands with the increase of the wetted area on the substrate, while the magnitude of the highest pressure gradually decreases with time. In principle, at the early stage of drop impact, the process of an impacting compound drop with high impact speed and equal density and viscosity (i.e. $\lambda = 1$, $\mu_2 = \mu_1$, $We \gg 1$ and $Re \gg 1$), is similar to that of an impacting pure drop, owing to the dominance of drop inertia over the surface tension of the inner droplet. Consequently, the interface of the inner drop can be viewed as a flow tracer, until the effect of its surface tension cannot be neglected anymore (e.g. when the curvatures at the sides of the flattened inner droplet become high). This explains why the trajectories of h_C and the drop apex are independent of α . Secondly, the flow inside the compound drop is decelerated vertically by the pressure gradients, and is then redirected near the substrate to the spreading (see also figure 3). We note that the pressure gradient varies with the vertical position. More precisely, the closer the position relative to the substrate, the stronger the pressure gradient and, therefore, the larger the acceleration of the flow. In addition, because the maximum pressure decreases with time, the pressure distribution around the inner droplet does not significantly change with the droplet descending, leading to the more or less uniform acceleration of the inner droplet. Thirdly, as the drop apex is away from the substrate, it is hardly affected by the pressure gradient at the very beginning of drop impact.

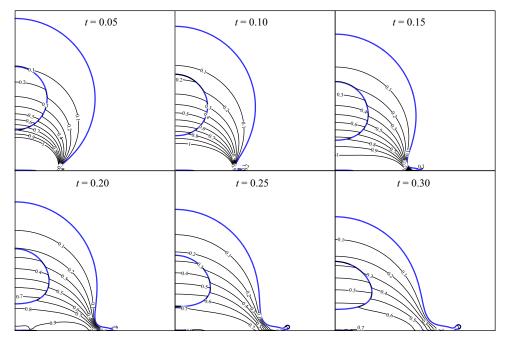


Figure 5. Time variation of pressure contours (black thin lines) of an impacting compound drop (blue thick lines) with We = 500, $\alpha = 0.064$ and $\lambda = 1.0$ at times t = 0.05, 0.10, 0.15, 0.20, 0.25, 0.30.

In the intermediate stage, the flow inside the drop is no more driven by the high pressure induced by the impact, and can be approximated by an axisymmetric stagnation point flow (Eggers *et al.* 2010). As a result, the shape evolution of an impacting pure drop would enter a self-similar inertial regime thereafter (Eggers *et al.* 2010; Lagubeau *et al.* 2012; Gordillo, Sun & Cheng 2018; Mitchell *et al.* 2019). Because the inner droplet is enclosed by the outer liquid of the compound drop, the self-similar evolution of the inner interface is supposed to start at the same time as the establishment of the stagnation point flow inside the impacting compound drop.

If the flow in the compound drop evolves into stagnation point flow, it can be expressed in the axisymmetric framework by

$$v_r = \frac{r}{\tau}$$
 and $v_z = -\frac{2z}{\tau}$, (3.2*a*,*b*)

where τ denotes the time of the stagnation point flow, v_r and v_z are the radial and vertical velocity components, respectively. The subsequent interface evolution follows $Dh/D\tau = 0$, or

$$\frac{\partial h}{\partial \tau} + v_r \frac{\partial h}{\partial r} = v_z. \tag{3.3}$$

Equation (3.3) has the similarity solution

$$h(r,\tau) = \frac{1}{\tau^2} H\left(\frac{r}{\tau}\right),\tag{3.4}$$

which is valid for any function H (Eggers *et al.* 2010). In other words, if the deformed interface has a scale of l in the z direction, (3.4) suggests that its scale in the r direction should be of the order of $l^{-1/2}$.

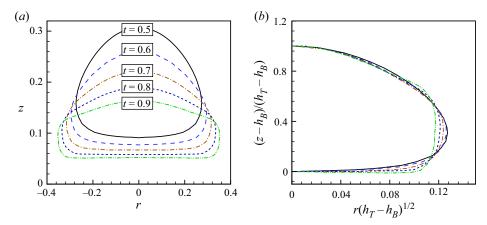


Figure 6. (a) The superimposed shapes of the inner droplet at different times at We = 500, $\lambda = 1$ and $\alpha = 0.064$. (b) Illustration of self-similar evolution of the inner droplet, in which the droplet shapes are rescaled by the self-similar length scales.

Eggers *et al.* (2010) reported that the stagnation point flow might start from $t \approx 0.5$ for an impacting pure drop. We check whether this is also true for the impacting compound drop by examining the time variation of h_T and h_B . Note that τ is related to the physical time t by $\tau = t + t_0$, in which t_0 is a case-dependent constant. To determine t_0 in a specific flow problem, we need to take account of the condition of v_z in (3.2*a,b*). From the numerical results at t = 0.5, we get $h_T = 0.307$ and $v_z = -0.52$ at the top of the inner interface, which suggests $t_0 = 0.680$. In addition, we can also obtain $h_B = 0.092$ and $v_z = -0.16$ at the bottom of the inner interface at t = 0.5, which gives $t_0 = 0.644$. Because the two t_0 only have a difference of 5% in magnitude, it implies that the flow in the compound drop at t = 0.5 is very close to stagnation point flow.

Suppose that the flow enters the regime of stagnation point flow at $\tau = \tau_0$, it is easy to obtain from (3.4) that the subsequent time variation of h_T (and h_B) should obey

$$\frac{h(0,\tau)}{h(0,\tau_0)} = \left(\frac{\tau_0}{\tau}\right)^2. \tag{3.5}$$

We plot in figure 4 the prediction of h_C , h_T and h_B by (3.5), with $\tau_0 = 0.5 + t_0$ and $t_0 = 0.662$ (i.e. the averaged value of the two t_0). We can see that the theoretical prediction agrees well with the numerical results for $t \in [0.5, 1]$. Furthermore, it is also interesting to see in figure 4(a) that the self-similar solution of h_C can be extended to as early as t = 0.24, while it is t = 0.16 for h_B and t = 0.44 for h_T . This observation suggests that the lower part of flow enters the self-similar inertial regime at an earlier time.

Figure 6(a) shows the snapshots of the inner interface in the stagnation point flow at We = 500, $\lambda = 1$ and $\alpha = 0.064$ (specifically from time t = 0.5 to 0.9, with a time interval of 0.1). To check whether the interface evolution is self-similar, we firstly choose $l = h_T - h_B$ as the characteristic length of the deformed inner droplet in the z direction. If the inner interface undergoes self-similar evolution, it would have $1/\sqrt{h_T - h_B}$ as its characteristic length in the r direction. Then, we rescale the corresponding droplet shapes by the self-similar scales, i.e. $(r\sqrt{h_T - h_B}, (z - h_B)/(h_T - h_B))$, and the results are shown in figure 6(b). We can see that the inner interface at different times appears to overlap in the self-similar coordinate, except the region near its spreading front. The deviation from the self-similar solution at the spreading front is reasonably expected at the late times (t = 0.8 and 0.9). Because the local curvature progressively increases with time (also see

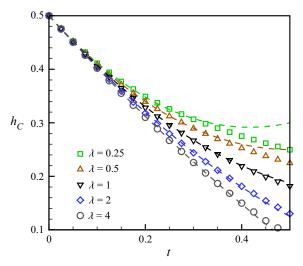


Figure 7. Evolution of h_C at We = 500, $\alpha = 0.064$ and various λ . The dashed lines correspond to the prediction of (3.1) using the acceleration a_{λ} calculated by (3.7).

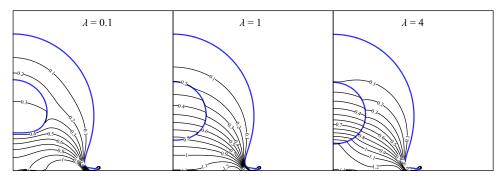


Figure 8. Pressure contours (lines with numbers) of impacting compound drops (thick lines) with We = 500, $\alpha = 0.064$ and various $\lambda = 0.1, 1.0, 4.0$ at time t = 0.15.

figure 6a), the effect of surface tension on the drop shape cannot be neglected at the late times.

3.2.2. Density effect on the motion of inner droplet

In order to assess the effect of density ratio on the dynamics of the inner droplet, we plot the time evolution of h_C at We = 500, $\alpha = 0.064$ and various $\lambda (= 0.25, 0.5, 1, 2, 4)$ in figure 7. We can see that, the lower the density of the inner droplet, the higher the position of h_C . This indicates that the inner droplets encounter different accelerations, of which the magnitude increases monotonically with λ . The density difference also affect the pressure distribution inside the compound drop. Figure 8 shows the pressure contours of impacting compound drops at the early stage (more precisely, t = 0.15) with We = 500, $\alpha = 0.064$ and various $\lambda (= 0.1, 1.0, 4.0)$. We can see that the maximum pressure increases with λ , because initial momentum of the inner droplet also increases with λ and a denser droplet is harder to stop. Similar to the cases with $\lambda = 1$ in § 3.2.1, a uniform acceleration process is expected for the inner droplet with $\lambda \neq 1$ at the early stage of drop impact. If so, the trajectory of the inner droplet can also be described by (3.1), by replacing a_0 by a λ -dependent acceleration a_{λ} .

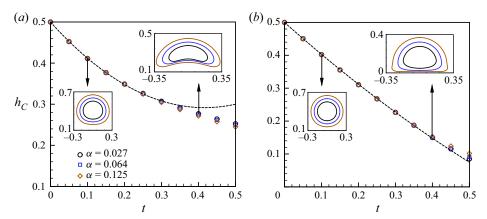


Figure 9. Evolution of the vertical position of the centroid of the inner droplet (h_C) at We = 500 and various $\alpha = 0.027$, 0.064 and 0.125). In particular, $\lambda = 0.25$ in (a), and $\lambda = 4$ in (b). The dashed line corresponds to the prediction of (3.1), with a_{λ} calculated by (3.7). The inset shows the superimposed interfaces of the inner droplets with different α .

Because for small α the inner and outer interfaces of the impacting compound drops evolve independently at the early stage of impact, the motion of the inner droplet can be modelled as a droplet subject to an impulsive acceleration a_0 of the surrounding fluid in an open space. Without loss of generality, we use the Atwood number $A = (\rho_1 - \rho_2)/(\rho_1 + \rho_2) = (1 - \lambda)/(1 + \lambda)$ to represent the effect of λ on the acceleration a_{λ} . A linear approximation of a_{λ} as a function of A can be obtained by Taylor expansion around A = 0 (or equivalently $\lambda = 1$),

$$a_{\lambda} = a_0 + \frac{\partial a_{\lambda}}{\partial A} A + O(A^2). \tag{3.6}$$

At the early stage of drop impact, the buoyancy force and the effect of added mass play a major role in the acceleration process (and both are a linear function of density), while the viscous force exerted by the surrounding fluid can be neglected. It is reasonable to assume that the quadratic term on the right-hand side of (3.6) is negligibly small.

To determine the value of $(1/a_0)(\partial a_\lambda/\partial A)$, we check a_λ/a_0 under two extreme conditions, i.e. A=-1 and 1 (corresponding to $\lambda\to\infty$ and $\lambda\to0$, respectively). When $A\to-1$, it is straightforward to have $a_\lambda/a_0\to0$. The case of $A\to1$ corresponds to a gas bubble immersed in an accelerated dense liquid. We assume that the bubble is more or less spherical, so that the added mass can be approximated by $\frac{1}{2}\rho_1\Omega$, where Ω denotes the volume of the bubble. Taking the added mass and the buoyancy force $(\approx \rho_1\Omega a_0)$ into account, we can get $a_\lambda/a_0\to2$ for $A\to1$. It is noteworthy that we obtain $(1/a_0)(\partial a_\lambda/\partial A)\approx1$ from either $A\to-1$ or $A\to1$. This fact is further confirmation that the acceleration of the inner droplet at the early stage of drop impact theoretically follows

$$a_{\lambda} = a_0(1+A). \tag{3.7}$$

Equation (3.7) can be verified by comparing the prediction of h_C by (3.1) against the numerical results. Figure 9 shows the evolution of h_C at We = 500 and various $\alpha = 0.027$, 0.064 and 0.125) and $\lambda = 0.25$ and 4), along with the prediction of (3.1), in which $a_{0,C} = 1.5$ obtained from numerical results at $\lambda = 1$ is used to calculate a_{λ} by (3.7). It is interesting to see that the trajectories of h_C for the three different α are virtually overlapped at the early stage of impact, specifically $t \leq 0.25$ for $\lambda = 0.25$ and $t \leq 0.35$ for

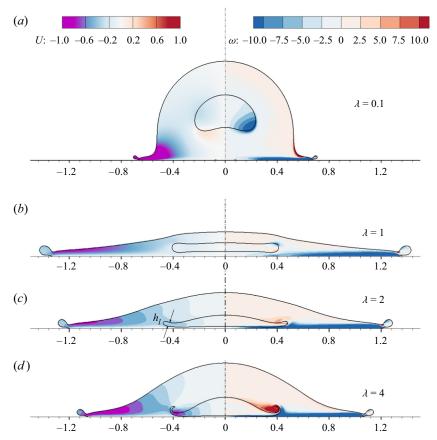


Figure 10. Snapshots of impacting compound droplets with $\alpha = 0.064$, We = 500 and various λ . In particular, (a) $\lambda = 0.1$, t = 0.25, (b) $\lambda = 1$, t = 1.25, (c) $\lambda = 2$, t = 0.9, (d) $\lambda = 4$, t = 0.6. The horizontal velocity contour (left) and vorticity (right) are shown.

 $\lambda = 4$. That is, the time variation of h_C is not sensitive to α for relatively small α . Also, the predictions are in good agreement with the numerical results in the respective range of time, as expected.

3.2.3. Density effect on the inner droplet deformation at the immediate stage

At the intermediate stage of drop impact, the deformation of the inner droplets with $\lambda < 1$ is very different from that with $\lambda > 1$ (cf. the middle column in figure 3). For $\lambda < 1$, the non-alignment of pressure and density gradients at the bottom of the inner droplet gives rise to the baroclinic effect and the subsequent generation of vorticity at the interface (cf. figure 10a). This phenomenon consequently enhances the ascending movement of the bottom of the inner droplet. At a later time, an upward counter-jet is induced by the vorticity, and breaks up the inner droplet (see the two right images in figure 3b). Such a counter-jet has been experimentally observed in a wide range of Re and Re after the impact of hollow drops, and it could be so strong as to penetrate the whole compound drop, especially with large impact velocity and Re (Gulyaev & Solonenko 2013). When the inner droplet with Re 1 is approaching the substrate, its deformation is characterized by the formation and subsequent evolution of a lamella at the spreading front. Figure 10 shows the snapshots of impacting drops at Re 0.064, Re 500 and various density contrasts

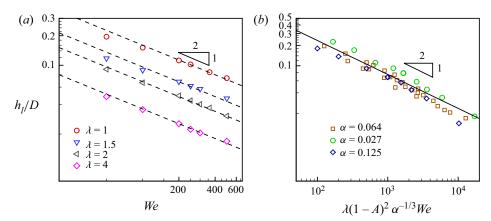


Figure 11. (a) Variation of lamella thickness of the inner droplet (h_l/D) as a function of We at $\alpha = 0.064$ on a log-log scale. (b) The lamella thickness as a function of $\lambda(1-A)^2\alpha^{-1/3}We$ on a log-log scale, in which We ranges from 50 to 500, λ from 1 to 4 and α from 0.027 to 0.125.

 $(\lambda = 1, 2 \text{ and } 4)$. We notice that, with the increase of λ , the lamella becomes thinner and thinner, probably accompanied by curling up.

Figure 11(a) shows the lamella thickness of the inner droplet (h_l) as a function of We for $\lambda = 1, 1.5, 2$ and 4. Here, h_l is defined as the mean thickness of the lamella (over a distance of 0.03 starting from the lamella front), which is measured at the moment when the velocity of the inner droplet centroid approaches zero. Despite of the differences between the results at various λ , the dimensionless lamella thickness h_l/D is seen to have a scaling of $We^{-1/2}$ for the cases with the same λ . This observation is very similar to the deformation of a pure drop after impacting onto a substrate, for which Clanet et al. (2004) experimentally found that the dimensionless lamella thickness follows $h_l/D \sim We^{-1/2}$. Moreover, they attributed this to the balance between the surface tension and the vertical deceleration of the drop ($\sim V^2/D$). The balance gives rise to an effective capillary length $(\sim \sqrt{\sigma D/(\rho V^2)} = DWe^{-1/2})$, which is nothing but the scale of the lamella thickness. The idea of Clanet et al. (2004) is adopted here to analyse the lamella thickness of the inner droplet. At the early stage of drop impact, the inner droplet experiences more or less uniform acceleration $a_0(1+A)V^2/D$, as indicated in (3.7). When the inner droplet is approaching the substrate (at $t \approx 0.5$), its vertical velocity approximately reduces to $U_i = V(1-A)/2$. Then, after a time scale of d/U_i , the vertical momentum of the inner droplet is supposed to completely transform to its horizontal spreading. In other words, the inner droplet encounters an acceleration of scale U_i^2/d in the process of momentum transformation. Therefore, from the balance between surface tension and drop acceleration as in Clanet et al. (2004), the dimensionless lamella thickness of the inner droplet with $\lambda > 1$ should follow

$$\frac{h_l}{D} \sim [\lambda (1-A)^2 \alpha^{-1/3} We]^{-1/2}.$$
 (3.8)

Figure 11(b) shows h_l vs $\lambda(1-A)^2\alpha^{-1/3}We$ on a log-log scale with different λ and α . The results roughly collapse onto a straight line, which corresponds to the theoretical predictions in (3.8).

The rolling up of the lamella of the inner droplet is caused by a mechanism that is the same as that of the ejected sheet in the impact of a pure drop (Riboux & Gordillo 2014). This is a combined effect of the lubrication force exerted by the surrounding fluid near

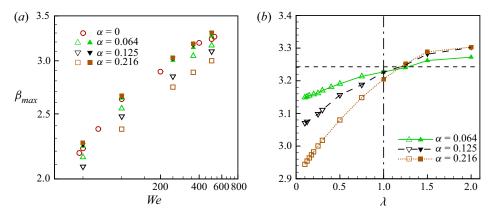


Figure 12. (a) Maximal spreading ratio β_{max} vs We with two fixed λ ; specifically, $\lambda = 0.25$ (hollow symbols) and 2 (filled symbols). Various values of α are considered, including $\alpha = 0.064$ (\triangle), 0.125 (∇) and 0.216 (\square). (b) Maximal spreading ratio β_{max} at We = 500 as a function of λ with different α . The horizontal dashed line denotes the value for the pure drop ($\alpha = 0$).

the lamella front, and the suction force due to the Bernoulli pressure acting on top of the spreading lamella. Obviously, the mechanism becomes more significant for a thinner lamella.

3.3. The maximal spreading ratio of compound drops

At the late stage of spreading of impacting compound drops, the interaction between the inner and outer interfaces becomes more intensive (see e.g. the last column of figure 3), and the presence of the inner droplet can affect the maximal spreading of the whole compound drop. Liu *et al.* (2018*b*) identified two flow regimes, i.e. jammed spreading (at small α) and joint rim formation (at large α). In particular, in the regime of jammed spreading, which is closely related to the present study, the contribution of the initial kinetic energy of the inner droplet to the spreading of the whole drop was found to decrease linearly with α . In this section, we focus on the effect of the density variation of the inner droplet (represented by λ) on the maximal spreading ratio β_{max} .

Figure 12(a) shows the variation of β_{max} as a function of We for different values of α ($0 \le \alpha \le 0.216$) and λ (= 0.25 and 2). We can see that at low λ (= 0.25), β_{max} monotonically decreases with α for all Weber numbers; comparatively, β_{max} is less sensitive to the change of α at relatively high λ (= 2). More results are shown in figure 12(b), in terms of β_{max} vs λ . We can see that β_{max} generally increases with λ for the same α and We.

To interpret these observations, we present the snapshots of the impacting compound drops at maximal spreading at different relatively small λ (= 0.1 and 0.5) in figure 13 and relatively large λ (= 1.5) in figure 14. For the compound drops, the drop shape at the maximal spreading is characterized by the upward bulging of the drop at its centre. The bulging arises from the floating inner droplet, which could be flattened (cf. λ > 1 in figure 14) or reshaped into a 'donut' (cf. λ = 0.1 in figure 13). The size of the bulging structure can be approximately measured by its height at the symmetry axis H and the radius of the spreading front of the inner droplet R_b (see the first row in figure 13c).

For the cases with $\lambda < 1$, we can see that the lower the λ , the higher the H; in particular, the deformed inner droplet holds more liquid than that at $\lambda = 1$ (figure 13), due to the density effect on its motion (see details in § 3.2.2). This fact gives rise to a smaller

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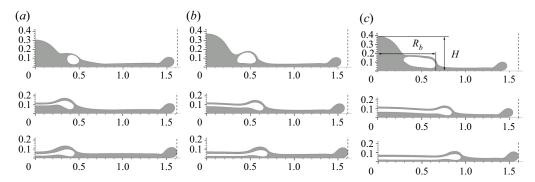


Figure 13. Snapshots of compound drops at the maximal spreading at We = 500 and various α and λ . Specifically, (a) $\alpha = 0.064$, (b) $\alpha = 0.125$ and (c) $\alpha = 0.216$; $\lambda = 0.1$ in the top row, $\lambda = 0.5$ in the middle row and $\lambda = 1.0$ in the bottom row. Here, H and H0 are the dimensionless height of the compound drop at the symmetry axis and the dimensionless radius of the inner droplet, respectively. For comparison, the maximal spreading diameters at H1 are marked by the dashed lines.

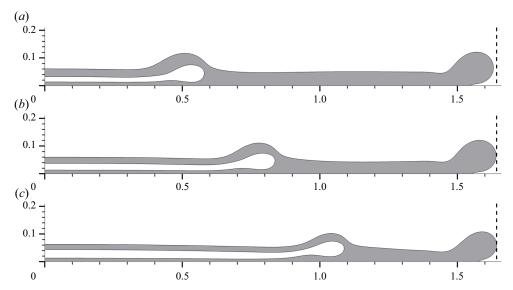


Figure 14. Snapshots of compound drops at the maximal spreading at fixed We (= 500) and λ (= 1.5) but different α : 0.064 (a), 0.125 (b) and 0.216 (c). The dashed line denotes the maximal spreading diameter for α = 0.216, i.e. the case in (c).

 β_{max} at $\lambda < 1$ than at $\lambda = 1$, because a larger bulging structure would reduce the liquid supply to the spreading front more significantly. Furthermore, the deformation of the inner droplet with $\lambda \le 1$ can be measured by the relative significance of droplet inertia to surface tension, i.e. $\rho_1 V^2 d/\sigma_{12} = \alpha^{1/3} We$. A larger α would lead to a more deformed inner droplet (or larger R_b ; see figure 13) at the same Weber number and subsequently a more noticeable bulging structure. Therefore, the change of the bulging structure for $\lambda < 1$ accounts for the monotonic decrease of β_{max} with α in figure 12. By contrast, for the cases with $\lambda > 1$, the flattened inner drop is generally located in the vicinity of the substrate at the maximal spreading, which is similar to that at $\lambda = 1$. Furthermore, H (≈ 0.06) is not sensitive to λ for small values of α (see figure 14).

To obtain the relation between β_{max} and λ for the impacting compound drops, we follow the modelling strategy of Liu *et al.* (2018*b*); that is, to propose a corrected Weber number We_{λ}^* by taking account of the density contrast, and use We_{λ}^* in the universal scaling for impacting pure drops. In order to do so, it is crucial to assess how much of the initial kinetic energy of compound drops would contribute to the spreading of the compound drop. The initial kinetic energy of a compound drop can be expressed by $\eta_i E_k$, where $E_k = \pi \rho_1 D^3 V^2 / 12$ corresponds to the initial kinetic energy of the compound drop at $\lambda = 1$, and

$$\eta_i = 1 + \alpha(\lambda - 1). \tag{3.9}$$

For the impacting compound drops with $\lambda = 1$ in the regime of jammed spreading, which occurs at small α , Liu *et al.* (2018*b*) found that the contribution of the kinetic energy of the inner droplet decreases linearly with α . In particular, given $\sigma_{12}/\sigma_{13} = 1$, their model of the corrected Weber number ((3.3) in their paper) can be simplified to

$$We^* = (1 - \alpha)We.$$
 (3.10)

We can see in figure 3 that the descending inner droplet with $\lambda > 1$ is more capable of draining away the fluid beneath it than that with $\lambda = 1$, thereby producing a similar but slightly lower bulging structure. Despite of the possible difference in topology of the inner droplet between $\lambda = 1$ and $\lambda > 1$, we assume that the effective contribution of the kinetic energy with $\lambda > 1$ can also be approximated by (3.10). Combining (3.10) with the correction of drop inertia by λ , i.e. (3.9), we can obtain the λ -corrected Weber number

$$We_{\lambda}^* = \eta_i We^* = (1 - \alpha + \alpha \lambda)(1 - \alpha)We, \quad \text{for } \lambda \ge 1.$$
 (3.11)

Wang *et al.* (2022) recently proposed a universal model to predict β_{max} for impacting pure drops in a wide range of Reynolds number ($10 \le Re \le 10\,000$), Weber number ($20 \le We \le 1000$) and substrate wettability ($30^{\circ} \le \theta \le 150^{\circ}$), which gives

$$\beta_{max}Re^{-1/5} = \frac{f(P)}{2 + f(P)},\tag{3.12}$$

where $f(P) = P^{1/4} + 10P^{1/2}$, and $P = WeRe^{-4/5}(1 - \cos \theta)^{-2}$. Substituting the corrected Weber number in (3.11) into (3.12), we can expect to obtain a universal model of β_{max} for impacting compound drops.

However, when using (3.11) for the cases with $\lambda < 1$, the numerical results are found to be scattered below the theoretical prediction; by contrast, these with $\lambda = 1$ are well predicted by the model; see figure 15(a). The particular bulging structure at $\lambda < 1$ is probably responsible for the deviation from the theoretical prediction. Because of the baroclinic effect at the bottom of the inner droplet and the induced counter-jet, the bulging structure at $\lambda < 1$ is noticeably bigger than that at $\lambda = 1$ (cf. figure 13). This should be taken into account in the estimate of We^{λ}_{λ} , e.g. by introducing a correction of η_b

$$We_{\lambda}^* = (1 - \alpha + \alpha \lambda)(1 - \alpha - \eta_b)We, \text{ for } \lambda \le 1.$$
 (3.13)

Clearly, the correction η_b is dependent on α and λ . It is straightforward to get $\eta_b \to 0$ when either $\lambda \to 1$ (compound drops with equal density) or $\alpha \to 0$ (pure drops). In such a way, the effect of the additional blocked liquid vanishes in case of either compound drops with $\lambda = 1$ or pure drops.

On the other hand, η_b should be proportional to the additional volume of liquid 1 held in the bulging structure at $\lambda < 1$ relative to $\lambda = 1$. Figure 16(a) shows the variation of the bulge size as a function of λ in terms of H and R_b for $\alpha = 0.064$, 0.125 and 0.216.

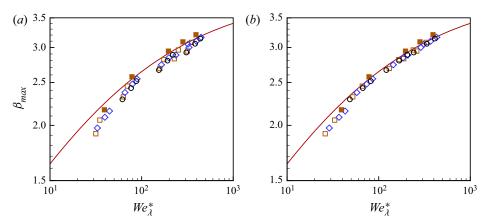


Figure 15. Value of β_{max} as a function of We_{λ}^{*} for the cases with $\lambda \leq 1$: (a) without the correction η_{b} , and (b) with the correction η_{b} . The numerical results consist of those with $\alpha = 0.216$ and various $\lambda = 0.1$, 0.5,

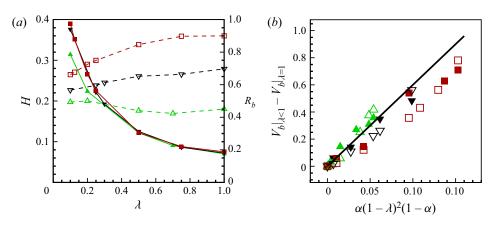


Figure 16. (a) Variation of H (filled symbols and solid lines) and R_b (dashed lines and empty symbols) as a function of λ at We = 500. (b) Variation of $V_b|_{\lambda < 1} - V_b|_{\lambda = 1}$ as a function of $\alpha(1 - \lambda)^2(1 - \alpha)$ at We = 50 (filled symbols) and 500 (empty symbols); the solid line denotes $V_b|_{\lambda < 1} - V_b|_{\lambda = 1} = 6\alpha(1 - \lambda)^2(1 - \alpha)$. The symbols represent numerical data at different α : 0.064 (\triangle), 0.125 (∇) and 0.216 (\square).

The plot indicates that H generally decreases with λ . Moreover, both H and R_b are not sensitive to α when $\lambda \geq 0.5$. For $\lambda < 0.5$, the increase of α leads to more significant changes of R_b with λ , approximately 10% at $\alpha = 0.064$ and 25% at $\alpha = 0.216$. In the present study, the volume of the bulging structure is approximated by $V_b = 6R_b^2H$. As shown in figure 16(b), $V_b|_{\lambda<1} - V_b|_{\lambda=1}$ is found to be roughly proportional to $\alpha(1-\lambda)^2(1-\alpha)$; in particular, the smaller the α , the better the proportionality. Therefore, η_b is expected to have a form

$$\eta_b \propto \alpha (1 - \lambda)^2 (1 - \alpha).$$
 (3.14)

The results with the η_b correction (by an approximation of η_b in (3.14) with a prefactor of 1) for $\lambda < 1$ are shown in figure 15(b). We can see that the numerical results gather around

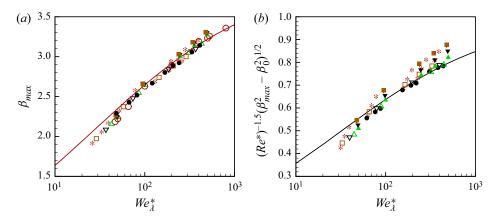


Figure 17. (a) Universal model of β_{max} of impacting drops using We_{λ}^* . The numerical results include symbols pure drops (\circ) and compound drops, and are represented by symbols. For the impacting compound drops, the cases consist of those with $\lambda = 0.25$ and various $\alpha = 0.064$ (Δ), 0.125 (∇) and 0.216 (\Box)), those with $\lambda = 2$ and various $\alpha = 0.064$ (Δ), 0.125 (∇) and 0.216 (\Box)), those with $\alpha = 0.216$ and λ ranging from 0.1 to 2 (*) and those with $\lambda = 0.001$ and α ranging from 0.064 to 0.216 (\bullet). The solid curve denotes the universal model (3.12) with We_{λ}^* as the variable. (b) Rescaled β_{max} as a function of We_{λ}^* defined in (3.11). The symbols represent the numerical results, which are the same as in (a); the solid curve denotes the theoretical prediction of Wei & Thoraval (2021), in which the modified Reynolds number $Re^* = 0.83(1 - \alpha^{2/3})Re$ and the fitting parameter $\beta_0 = 1.2$ were used.

the theoretical prediction now, and the maximal difference relative to the prediction of (3.13) also reduces from 13 % (without the correction) to 6 % (with the correction).

It is noteworthy that the corrections of the Weber number in (3.11) and (3.13) are only applicable to relatively small α (\leq 0.216 in the present study). We present all the numerical results in figure 17(a) with respect to β_{max} vs We_{λ}^* . All the results appear to collapse onto a single curve, which is in line with the prediction of (3.12). We find that this universal model for pure drops can well represent the results for compound drops by using We_{λ}^* , with a maximum relative difference of 6%. Based on the numerical simulations, Wei & Thoraval (2021) also proposed a model ((4) in their paper) for impacting hollow drops, i.e. $\lambda = 0.001$. Figure 17(b) shows the comparison of the prediction of Wei & Thoraval's model against our numerical results. Note that we use $We_{\lambda}^* = (1 - \alpha)(1 - \alpha + \alpha\lambda)We$ in their model instead of $We_{\lambda}^* = (1 - \alpha)^2We$ in the original paper, in order to take account of the density effect in drop inertia and get a better agreement. Because it was established based on results for hollow drops, it is not surprising that the model agrees excellently with our numerical results of hollow drops. However, the distribution of the other data is more scattered compared with the present model in figure 17(a).

4. Conclusion

We have numerically studied the dynamics of impacting compound drops at moderate Weber and Reynolds numbers using a ternary-fluid diffuse-interface method, with a focus on how the density ratio λ between the inner and outer droplets affects the evolution of the interfaces. We firstly examined the dynamic behaviour of the inner droplet at different stages of drop impact. At the early stage, the inner droplet experiences more or less a uniform acceleration, owing to the development of impact-induced pressure. The magnitude of the acceleration at $\lambda \neq 1$ (denoted by a_{λ}) was then correlated with the acceleration at $\lambda = 1$ (denoted by a_0) and the Atwood number (A), specifically by

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 $a_{\lambda} = a_0(1+A)$. At the intermediate stage, the shape evolution of the inner droplet at $\lambda = 1$ followed a self-similar trend, which is closely related to the occurrence of stagnation point flows inside the compound drop. For $\lambda > 1$, a lamella was found to form at the spreading front of the inner droplet, similar to the deformation of a pure drop after impacting onto a substrate. We theoretically analysed the thickness of the lamella h_l , and ended up with a scale of $h_l/D \sim (\lambda(1-A)^2\alpha^{-1/3}We)^{-1/2}$, which agrees with numerical results. Secondly, we investigated the effect of the density ratio on the maximal spreading of the compound drop. A bulging structure is generally observed at the centre of the compound drop due to the presence of the inner droplet, thereby effectively reducing the liquid supply to the spreading front and leading to a decrease of β_{max} as compared with a pure drop. In particular, the occurrence of a counter-jet at $\lambda < 1$ makes the bulging structure much larger than that at $\lambda \geq 1$. To obtain a universal expression of β_{max} for impacting compound drops, we analysed the effect of λ on the contribution of the initial kinetic energy to the drop spreading and the features of the bulging structure. Then, we proposed a corrected Weber number We_{λ}^* by taking account of the combined effects of λ , α , We and the morphology of the compound drop. Replacing We by We_{λ} in the universal model for impacting pure drops, we successfully obtained a good prediction of the maximal spreading ratio for compound drops with liquids of different densities.

In the present study, we considered a fixed $\theta_{13} = 150^{\circ}$. Similarly to the impact dynamics of pure drops (Wang *et al.* 2022), the substrate wettability (represented by θ_{13} here) is supposed to affect the maximal spreading of compound drops too. In addition, as the substrate is essentially superhydrophobic, the compound droplet would retract after the maximal spreading happens. The effect of wettability and the retraction dynamics is beyond the scope of the present study and would be the topic of our future research.

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