

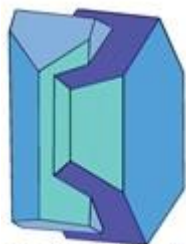
# The crystal structure of pezzottaite and the crystal chemistry of the beryl-pezzottaite series

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## Abstract

Crystal structures along the join beryl-pezzottaite have been refined and their compositions determined by electron-microprobe analysis. All crystals show sharp uniform diffraction spots but are microscale mixtures of more than one structure. Three distinct phases were identified with different diffraction characteristics: (1) hexagonal ( $P6/mcc$ ) Cs-rich beryl; (2) hexagonal-rhombohedral ( $R\bar{3}c$ ) twinned pezzottaite; (3) incommensurate phases with cell dimensions resembling those of beryl with a doubled  $c$ -dimension and  $l$  indices deviating from integer values by  $\pm 0.05$ – $0.10$ . Beryl ( $P6/mcc$ ) structures refined to  $R_1$  indices from 2.36 to 2.91% and pezzottaite structures refined to  $R_1$  indices from 3.31 to 5.83%. In pezzottaite, the Cs1 and Cs2 sites are each occupied by Cs<sup>+</sup>, Rb<sup>+</sup> and (H<sub>2</sub>O) with Cs<sup>+</sup> showing a preference for Cs1; and the Na1 and Na2 sites are occupied by Na<sup>+</sup> and Ca<sup>2+</sup>. Na<sup>+</sup> bonds to one (H<sub>2</sub>O) group and (H<sub>2</sub>O) bonds to one Na<sup>+</sup>. The ordering of (Cs<sup>+</sup> + Rb<sup>+</sup>) and (Na<sup>+</sup> + Ca<sup>2+</sup>) in pezzottaite is driven by the incident bond-valence requirements of the anions coordinating the (LiO<sub>4</sub>) tetrahedron. The valence-sum rule is maintained through the (Cs<sup>+</sup> + Rb<sup>+</sup>) + Li<sup>+</sup> → □ + Be<sup>2+</sup> variation in beryl by cooperative relaxation of bonds at the Si and Be tetrahedra, and in pezzottaite by cooperative relaxation of bonds at the Si, Al and Li tetrahedra. The valence-sum rule mandates that Na<sup>+</sup> must bond to one channel (type-II) (H<sub>2</sub>O) group which, when combined with the constraint of electroneutrality, requires that compositions along the beryl-pezzottaite join must lie below the line (Cs<sup>+</sup> + Rb<sup>+</sup>) + 2(Na<sup>+</sup> + Ca<sup>2+</sup>) = 1 – 2Ca<sup>2+</sup> apfu. The occurrence of an incommensurate phase at intermediate compositions is due to the interaction of the species in adjacent columns of the  $P6/mcc$  beryl structure.

**Keywords:** Pezzottaite, beryl, crystal structure, electron-microprobe analysis.

## Introduction

Pezzottaite is a Cs-rich mineral, ideal formula  $\text{Cs}(\text{Be}_2\text{Li})\text{Al}_2\text{Si}_6\text{O}_{18}$ , that was discovered about 20 years ago (Hawthorne *et al.*, 2004) at the Sakavalana pegmatite 25 km south of the village of Mandosonoro, SW of the town of Antsirabe, 140 km SW of Ambatofinandrahana, central Madagascar. Interest in this mineral was enhanced by it being a significant gemstone (Laurs *et al.*, 2003; Simmons *et al.*, 2003; Warin and Jacques, 2003; Peretti *et al.*, 2004) with prices up to US\$10,000 per carat. The crystal structure proved to be an ordered superstructure of beryl, ideally  $\text{Be}_3\text{Al}_2\text{Si}_6\text{O}_{18}$ . For many years, there has been interest in the incorporation of  $\text{Cs}^+$  and/or  $\text{Li}^+$  into the beryl structure (Belov, 1958; Beus, 1960; Evans and Mrose, 1966; Bakakin *et al.*, 1969; Černý and Hawthorne, 1976; Hawthorne and Černý, 1977; Aurisicchio *et al.*, 1988; Sherriff *et al.*, 1991; Abduriyim *et al.*, 2003; Andersson, 2006) and some discussion about how much  $\text{Cs}^+$  can substitute into the structure of beryl. Nevertheless, the discovery of pezzottaite came as a surprise as the occurrence of such an ordered superstructure was completely unexpected. Here, I report on the crystal structures of a series of samples of Cs-bearing beryl and pezzottaite and examine the detailed crystal-chemistry of the beryl-pezzottaite series. Crystallographic sites are indicated by italicized symbols (e.g. *Be*, *Si*), atoms and ions are indicated by Roman symbols (e.g. *Be*,  $\text{Be}^{2+}$ ); polyhedra are labelled by the central site (e.g. *Be* tetrahedron), or  $^{\text{Be}}\text{Li}^+$  where the *Be* tetrahedron is occupied by  $\text{Li}^+$ . When discussing the refinement of site occupancies, atoms are written as neutral as neutral scattering factors were used in the refinements.

## Previous work

There is some confusion in the literature, sometimes within individual papers, concerning the occupancy of the various sites in the beryl structure. Table 1 lists the Wyckoff positions, point symmetries and general coordinates of sites in the beryl and pezzottaite structures.

### *Li<sup>+</sup> and Cs<sup>+</sup> in the beryl structure*

The details of the incorporation of  $\text{Li}^+$  into the beryl structure have been contentious since the early work of Belov (1958) and Beus (1960). Belov (1958) and Bakakin and Belov (1962) proposed that  $\text{Li}^+$  replaces  $\text{Be}^{2+}$  directly in the structure *via* the substitution  $^{\text{Be}}\text{Li}^+ \rightarrow ^{\text{Be}}\text{Be}^{2+}$  with alkalis entering the channel site(s) to maintain electroneutrality. Beus (1960) proposed that  $\text{Li}^+$  enters beryl *via* the coupled substitution  $^{\text{Al}}\text{Li}^+ + ^{\text{Be}}\text{Al}^{3+} \rightarrow ^{\text{Al}}\text{Al}^{3+} + ^{\text{Be}}\text{Be}^{2+}$  with alkalis entering the channel site(s) to maintain electroneutrality. On the basis of preliminary structure-refinement results, Evans and Mrose (1966) supported the mechanism of Beus (1960) whereas Bakakin *et al.*

*al.* (1969) reported structural results on a (Cs,Li)-rich beryl which supported the mechanism of Belov (1958). Hawthorne and Černý (1977) refined the crystal structure of a beryl with  $\text{Cs}^+ + \text{Rb}^+ = 0.14$ ,  $\text{Na}^+ = 0.31$  and  $\text{H}_2\text{O} = 0.66$  apfu (atoms per formula unit) and found that  $\text{Cs}^+$  occupies the  $2a$  site at  $0\ 0\ \frac{1}{4}$ ,  $\text{Na}^+$  occupies the  $2b$  site at  $0\ 0\ 0$ , and  $(\text{H}_2\text{O})$  occupies the  $2a$  site. In this beryl, the  $\langle \text{Be}-\text{O} \rangle$  distance is significantly larger than that in synthetic  $\text{Be}_3\text{Al}_2\text{Si}_6\text{O}_{18}$ , whereas the  $\langle \text{Al}-\text{O} \rangle$  distance is the same as that in synthetic  $\text{Be}_3\text{Al}_2\text{Si}_6\text{O}_{18}$ , compatible with the model of Belov (1958) and not with the model of Beus (1960). Brown and Mills (1986) and Aurisicchio *et al.* (1988) reported similar results. Sherriff *et al.* (1991) examined four beryls of different  $\text{Cs}^+$  and  $\text{Li}^+$  contents, showing that the  $\langle \text{Be}-\text{O} \rangle$  distance increases linearly with increasing  $\text{Li}^+$  content in beryl, and that  $^7\text{Li}$  MAS NMR spectra show the presence of two signals that they attributed to  $\text{Li}^+$  at the *Be* site and  $\text{Li}^+$  at a channel site adjacent to the *Be* site. Andersson (2006) also found two sites by EPR for  $\text{Li}^+$  in the beryl structure, one associated with the framework and another within the channel. Structure-refinement studies have not located any  $\text{Li}^+$  site in the channel, but this may be due to the low occupancy of such a site. Andersson (2006) also proposed that  $\text{Li}^+$  does not replace  $\text{Be}^{2+}$  at the *Be* site but is located in a tetrahedron to one side of the (locally empty) *Be* tetrahedron. However, this mechanism does not account for the expansion of the *Be* tetrahedron with increasing  $^{14}\text{Li}$  in the structure (Hawthorne and Černý, 1977; Sherriff *et al.*, 1991) and does not provide a mechanism for satisfying the valence-sum rule at every  $\text{O}^{2-}$  anion locally coordinating an empty *Be* site.

#### *Li<sup>+</sup> and Cs<sup>+</sup> in the pezzottaite structure*

In the formal description of pezzottaite (Hawthorne *et al.*, 2004; page 377), it was stated that “In beryl, Cs is incorporated into the channel at the  $2a$  position...Cs occupies the analogous position in the pezzottaite structure, complete details of which will be presented in a future publication.” The structure of the intergrowths described here delayed publication of the structure details of pezzottaite. Meanwhile, several descriptions of the structure have appeared: Gi *et al.* (2008); Yakubovich *et al.* (2009); Gatta *et al.* (2012). The structure is rhombohedral  $R\bar{3}c$ , the bond topology is the same as that of (Cs,Na,Li)-bearing beryl;  $\text{Cs}^+$  occupies the  $6a$  and  $12c$  sites,  $\text{Na}^+$  occupies the  $6b$  and  $12c$  sites, and  $\text{Be}^{2+}$  and  $\text{Li}^+$  alternately dominate at two distinct tetrahedrally coordinated sites, although some disorder is proposed by Yakubovich *et al.* (2009) and Gatta *et al.* (2012). Ende *et al.* (2021) refined the structure at different temperatures and pressures, showed that there is a transition from  $R\bar{3}c$  to  $R3c$  at  $\sim 4$  GPa, and noted the occurrence of diffuse scattering that they suggest is due to ordering of the channel constituents along **c**.

### *(H<sub>2</sub>O) in beryl and pezzottaite*

Quantitative chemical analysis of structural (H<sub>2</sub>O) is not practical because of the ubiquitous presence of fluid inclusions in these minerals, and our knowledge of structural (H<sub>2</sub>O) has come from an enormous amount of vibrational spectroscopy for beryl and some for pezzottaite.

In an extensive study of the polarized infrared spectra of both natural and synthetic beryl, Wood and Nassau (1968) showed that there are two types of (H<sub>2</sub>O) groups in beryl: Type-I and Type-II. According to Wood and Nassau (1968, page 777): “The Type I molecule is oriented in the channels with its C<sub>2</sub> symmetry axis perpendicular to the crystal C<sub>6</sub>-axis, while the Type II molecule is rotated 90° by the action of a nearby alkali ion on the molecular electric dipole”. A major amount of spectroscopic work on beryl has basically confirmed their suggestions while adding much quantitative information about the spectroscopic details. One expects the situation in pezzottaite to be similar, and in the formal description of this mineral (Hawthorne *et al.*, 2004), an infrared spectrum showed the presence in the principal OH-stretching region of type-II (H<sub>2</sub>O) bands at 3595 and 3547 cm<sup>-1</sup> and an H–O–H bending mode at 1636 cm<sup>-1</sup> (see also Gatta *et al.*, 2012). Lambruschi *et al.* (2014) and Ende *et al.* (2021) obtained similar results by Raman spectroscopy.

### **Samples**

Samples were obtained from our initial work on the description of pezzottaite as a distinct mineral species (Hawthorne *et al.*, 2004). At the same time, Hänni and Krzemnicki (2003) reported Cs-rich morganite from the Dara-i-Pech pegmatite field, Chapa Dara District, Konar Province, and the Deva Mine, Paroon pegmatite field, Vama District, Nuristan Province, Afghanistan. Samples of this material were generously supplied by the well-known mineral dealer Herb Obodda. Fourteen samples were characterized here by a combination single-crystal X-ray diffraction and electron microprobe analysis.

Following collection of the X-ray intensity data, electron-microprobe analysis showed that all individual crystals are reasonably chemically homogeneous at the micron scale. However, the structure refinement revealed that these small crystal volumes are structurally complex: all rhombohedral crystals are twinned (~1 to 41% twin fraction), and also contain variable amounts of a hexagonal phase.

### **Single-crystal selection and data acquisition**

Crystal fragments were mounted in epoxy, polished and first examined by electron-microprobe

analysis for their Cs<sup>+</sup> and Na<sup>+</sup> content and spatial homogeneity. Complex chemical zoning at various scales is prevalent throughout the material examined. Small reasonably homogeneous regions (of different Cs<sup>+</sup> and Na<sup>+</sup> contents) were then identified and removed for single-crystal diffraction study. The crystal fragments were ground to spheres (or ellipsoids) and fixed to tapered glass fibers prior to collection of X-ray intensity data, and later set in epoxy and polished for quantitative chemical characterization by electron-microprobe analysis.

### Single-crystal X-ray diffraction

Single crystals (~150 μm in size, Table 2) were mounted on a Bruker four-circle diffractometer equipped with a 4K CCD detector at a crystal-to-detector distance of 5 cm. In excess of a hemisphere of intensity data was collected to 60°2θ using a frame width of 0.2° and an exposure time per frame of 20 s. Additional scans were used to increase data redundancy to improve X-ray absorption correction for the non-spherical crystals. Careful examination of the raw-data frames 'on-screen' showed simple sharp uniform diffraction spots for all crystals. However, correct indexing and subsequent integration of the intensity data was not straightforward. Three different types of diffraction patterns were encountered (Table 2):

- (1) hexagonal ( $P6/mcc$ ) [Cs-rich beryl: 5 samples: P3, P8, P10, P11, P14]: All reflections fit a  $P$  hexagonal cell with  $a \approx 9.22$  and  $c \approx 9.26$  Å.
- (2) hexagonal-rhombohedral ( $R\bar{3}c$ ) [pezzottaite: 7 samples: P1, P2, P4, P5, P6, P7, P12]: All reflections fit a hexagonal  $R$  cell with  $a \approx 15.93$  and  $c \approx 27.83$  Å. This rhombohedral cell has a volume nine times greater than that of the hexagonal  $P$  cell, giving rise to reflections with  $hkl$  indices  $1/3$  and  $2/3$  relative to the hexagonal  $P$  cell. Careful inspection of the data showed that all rhombohedral crystals have reflections that violate the general rhombohedral lattice restriction. So how can one be sure that the basic structure is rhombohedral? Two crystals, P2 and P7, have reasonably prominent superlattice reflections (relative to the small hexagonal beryl cell) and contain very minor (<1%) twin components; thus the entire diffraction patterns are consistent with a large  $R(\text{obv})$  cell. Integrating the data on the  $R(\text{obv})$  cell (ignoring the twin fraction) gave the following merge results for the data: Sample, number of reflections, number of unique reflections,  $R(\text{merge})$  in  $R\bar{3}c$ : P2, 19381, 2002, 1.9%; P7, 15520, 2002, 1.9%; these results confirm  $R\bar{3}c$  as the symmetry of the structure. Some reflections are present (with  $l \neq 3n$ ) that violate the obverse condition ( $-h+k+l = 3n$ ) and other reflections are present that violate the reverse condition ( $h-k+l = 3n$ ). This observation is consistent with twinning by reticular merohedry through the introduction of a 2-fold twin axis along [001] (Herbst-Irmer and Sheldrick, 1998).
- (3) Incommensurate (trigonal-hexagonal) [beryl-like: 2 samples: P9, P13]: All reflections fit a  $P$  cell with  $a \approx 9.22$  and  $c \approx 18.52$  Å. Relative to the hexagonal  $P$  cell (1) above, there are

additional reflections that support an approximate doubling of the **c**-axis; however, these additional spots are not quite commensurate and their *l*-indices deviate from ideal integer values by  $\pm 0.05$ – $0.10$ . Attempts to refine these structures were not successful.

#### *Processing of the X-ray intensity data*

Due to the complex nature of the diffraction patterns, processing of the X-ray intensity data was quite complicated. For each crystal, numerous raw-frame sequences were carefully inspected on the computer screen with optimized signal:noise settings, such that additional diffraction spots (*i.e.* not fitting the smaller hexagonal *P* cell) could be identified visually. After all sets of data had been examined visually, it was apparent that reflections supporting the large rhombohedral *R* cell [ $a \approx 15.97$ ,  $c \approx 27.83$  Å] are quite variable in their expression from one crystal to the next. For crystals that show evidence of either the smaller hexagonal *P* cell or the larger rhombohedral *R* cell, these data sets were integrated initially on the large rhombohedral cell using a primitive lattice constraint (data for the apparent hexagonal crystals were forcibly re-indexed by applying the transformation  $1\ 2\ 0 / 2\ -1\ 0 / 0\ 0\ 3$ ). After integration, all reflections with  $l = 3n$  were removed, and the remaining reflections were carefully examined; observed reflections with  $l \neq 3n$  establishes the presence of some component of the rhombohedral superstructure within the crystal. For those crystals having observed reflections with  $l \neq 3n$ , the relative ratio of reflections violating the obverse or reverse settings served to establish the dominant twin-component in the absence of any possible hexagonal *P* component (*i.e.* mutual overlap occurs on layers where  $l = 3n$ ).

Standard (final) integration (with SAINT) was then done on the simple hexagonal *P* datasets, followed by processing with SADABS and final merging of identical reflections in XPREP to produce a normal HKLF 4 file for structure refinement. For the rhombohedral crystals, the dominant twin-component was first set as the primary obverse component (the transformation reverse  $\rightarrow$  obverse *via*  $1\ 1\ 0 / -1\ 0\ 0 / 0\ 0\ 1$  was used if necessary), and the secondary component was then defined by the twin law  $[-1\ 0\ 0 / 0\ -1\ 0 / 0\ 0\ 1]$ ; the two orientation matrices were used in the twin-integration procedure. Absorption corrections and merging of data were then done with the TWINABS program, and an HKLF 5 data file [that distinguishes the data of the primary component ( $l \neq 3n$ ) from the data overlapping with the twin component ( $l = 3n$ )] was written for refinement of the twinned structure.

For one of the incommensurate crystals (P9), attempts to integrate the data and refine the structure on the  $a \approx 9.22$ ,  $c \approx 18.52$  Å cell gave poor results that are not presented here. As a comparative index for all the crystals refined here, all the hexagonal and rhombohedral



crystals and one of the incommensurate crystals were processed in a standard manner on the small hexagonal  $P$  cell, ignoring any superlattice reflections; all refinements gave  $R_1$  values between 2.3 and 2.7%, suggesting that all crystals studied are of similar high quality.

#### *Space-group assignment for the hexagonal $P$ and rhombohedral crystals*

Crystals with the smaller hexagonal  $P$  unit-cell have Laue merging results and systematically absent reflections consistent with the space group  $P6/mcc$ . In order to correctly assign a space group to the rhombohedral crystals, data that is unaffected by twinning and the possible presence of a hexagonal component was treated in the following manner. Special subsets of data were generated in the following way: the data were integrated using the orientation matrix of the dominant twin-component; data were then processed using SADABS; reflections affected by twinning or possible overlap with a hexagonal  $P$  contribution (*i.e.* reflections with  $l = 3n$ ) were removed. The remaining reflections are in accord with Laue-group symmetry  $\bar{3}m1$  and the presence of a  $c$ -glide plane, suggesting that the correct space group is  $R\bar{3}c$  for the rhombohedral crystals. Note that the final twin refinements (HKLF 5 data from TWINABS) for the rhombohedral crystals commonly list several reflections  $h, k, l$  (with  $l = 3n$ ) that significantly violate ( $F_o^2 > 5-10 \sigma$ ) the  $c$ -glide reflection condition. However, if the twinning is ignored (HKLF 4 data from SADABS), the refinements list no such  $c$ -glide violations above  $5\sigma$ , suggesting that the apparent violations result from twin integration and TWINABS data-processing.

#### *Refinement of the simple hexagonal structure*

The structure of each sample was refined in the space group  $P6/mcc$  using  $F^2$  in the SHELXTL PLUS (PC version) software package with neutral scattering factors. Full occupancy was assumed for all sites except those occupying the channel. According to previous crystal-structure refinements of Li-bearing beryl (Hawthorne and Černý, 1977; Aurisicchio *et al.*, 1988; Sherriff *et al.*, 1991), the  $Be$  site is occupied by  $Be$  and  $Li$ . However, attempts to refine the relative amounts of  $Be$  and  $Li$  were not always successful; this is not surprising as complete replacement of  $Be^{2+}$  by  $Li^+$  as indicated by the chemical analyses will affect the total scattering from the crystal by  $\ll 0.3\%$ . Thus,  $Be$  site-occupancies were assigned from the analyzed chemical formulae. The structures converged to  $R_1$  indices of 2.36 to 2.91%; details of the data collection and structure refinement are listed in Table 3. Final atom coordinates and anisotropic-displacement parameters are given in Table 4, selected interatomic distances and angles are given in Table 5, refined site-populations are given in Table 6, and Table 7 shows a bond-valence table for beryl P10 calculated with the parameters of Gagné and Hawthorne



(2015).

#### *Refinement of the rhombohedral structure*

The intensity data (HKLF 5 format from TWINABS) for the rhombohedral crystals consist of reflections merged with Laue symmetry  $\bar{3}m1$ , that is with  $l \neq 3n$ , belonging only to the dominant obverse domain (batch 1), and with  $l = 3n$ , belonging to both the dominant domain and the subordinate twin-domain (batch 2). Refinement of this data gave  $R_1$  values from 3.3 to 6.0%, and in all cases, the worst-fit reflections are those with  $l = 3n$  for which  $|F_o| > |F_c|$ . The twin fraction (*i.e.* the BASF value) ranges from 0.159 to 0.524 for the seven rhombohedral crystals, indicating that in all cases, a significant twin component is present. If the correct intensity contributions for both domains were simply related by the BASF value from the refinement, then one would expect an even distribution of  $|F_o|$  and  $|F_c|$  values for the worst-fit reflections, but this is not the case. Normally, obverse-reverse twins are refined in this manner, without reflections that belong only to the minor component as they are weaker and unlikely to improve the model (Herbst-Irmer and Sheldrick 1998). For comparison, new HKLF 5 data files were generated (using TWINABS) that contained the *full* reflection set, *i.e.* all reflections with  $l \neq 3n$  were present in either batch 1 or batch 2, in addition to the overlapped reflections with  $l = 3n$  (batch 2). As expected, refinements from these *full* datasets did indeed result in higher  $R_1$  values (4.5 to 9.7%); however, the BASF values in all cases refined to significantly lower values than for the previous set of refinements. The new BASF values ranged from 0.009 to 0.415 and indicate that the twinned fractions vary from <1 to 41% for the seven rhombohedral crystals. For two of the rhombohedral crystals (P2, P7), there was no on-screen evidence for the presence of a twin component, and the initial test for the relative ratio of obverse:reverse components (see section above on *Processing of X-ray intensity data*) indicated less than 1% twin component. The refined BASF values derived using both individual-component contributions on  $l \neq 3n$  layers result in more realistic contributions from the minor twin-component for crystals P2 and P7 (and presumably also for the other twinned rhombohedral crystals). Furthermore, it seems that, in the absence of the twin-component data on  $l \neq 3n$  layers, the twin fraction is significantly overestimated for these seven rhombohedral crystals as a result of an unaccounted additional hexagonal component that only overlaps with the  $l = 3n$  reflections of the rhombohedral structure.

It is not feasible to refine the simple hexagonal and twinned rhombohedral structures simultaneously, and one must accept the results of refinement of the twinned rhombohedral structure without accounting for the presence of a simple hexagonal component. Details of the

data collection and structure refinement for the twinned rhombohedral structures are listed in Table 8. Attempts to refine the amounts of Be and Li at both the *Be* and *Li* sites were not successful (as expected). The *Be* site was assigned initially as completely occupied by Be and the *Li* site as occupied by the amounts of Li from the chemical formulae plus the Be in excess of 2 apfu, and these occupancies were fixed in the refinement. Local stereochemistry will be a more reliable way to assign Be,Li site-occupancies *a posteriori* than direct refinement that will rely on differences of <<0.3% in the total scattering of the crystal.

Atom coordinates and displacement parameters are given in Table 9, selected interatomic distances and angles in Table 10, and refined site-populations are listed in Table 11. A bond-valence table for pezzottaite P6 is given in Table 12. All Crystallographic Information Files (CIFs) for the refined structures have been deposited with the Principal Editor of *Mineralogical Magazine* and are available as Supplementary Material (see below).

### Electron-microprobe analysis

The single crystals used for collection of the X-ray-diffraction intensity data were subsequently set in epoxy, ground, polished and coated with carbon prior to being mounted in a Cameca SX100 electron microprobe. They were analysed in wavelength-dispersion mode with an accelerating voltage of 15 kV, a specimen current of 15 nA, and a beam diameter of 7  $\mu\text{m}$ . The following standards were used: TAP: Ca, diopside; Al, andradite; Na, albite; PET: Si, albite; K, orthoclase; LiF: Fe, fayalite, Cs, pollucite; Rb: Rb-leucite. The data were reduced and corrected by the PAP method of Pouchou and Pichoir (1985). Unit formulae were normalized on the basis of 18 anions with  $\text{Li}^+ = [\text{Na}^+ + \text{Cs}^+ + \text{K}^+ + \text{Rb}^+ + (\text{Ca}^{2+} \times 2)] - \text{Fe}^{2+}$  and  $\text{Be}^{2+} = 3 - [\text{Na}^+ + \text{Cs}^+ + \text{K}^+ + \text{Rb}^+ + (\text{Ca}^{2+} \times 2)] - \text{Fe}^{2+}$  apfu. Chemical compositions (mean of 10 determinations) and unit formulae are given in Table 13. Beryl P3 contains a small amount of Fe (Table 13) that substitutes for  $\text{Al}^{3+}$  at the *Al* site. Aurisicchio *et al.* (1988) note that the main ions substituting for  $\text{Al}^{3+}$  at the *Al* site are  $\text{Fe}^{2+}$  and  $\text{Mg}^{2+}$ , and hence the formula for P3 was calculated accordingly.  $\langle \text{Al}-\text{O} \rangle$  for P3 is 1.909 Å, whereas the  $\langle \langle \text{Al}-\text{O} \rangle \rangle$  distance for the other beryls is 1.903 Å; this difference of 0.006 Å is in accord with the weighted difference in ionic radii between  $\text{Al}^{3+}$  and  $\text{Fe}^{2+}$ :  $(0.78 - 0.535) \times 0.054 / 2 = 0.007$  Å.

### The beryl and pezzottaite structures

The beryl structure (Fig. 1) consists of a series of six-membered rings of ( $\text{SiO}_4$ ) tetrahedra that are linked into a framework by ( $\text{BeO}_4$ ) tetrahedra and ( $\text{AlO}_6$ ) octahedra (Fig. 1a). The beryl structure is very strongly compositionally layered (Fig. 1b) with layers of ( $\text{SiO}_4$ ) tetrahedra

interleaved with layers of ( $BeO_4$ ) tetrahedra and ( $AlO_6$ ) octahedra.  $Li^+$  substitutes for  $Be^{2+}$  in the ( $BeO_4$ ) tetrahedra (shown in blue in Fig. 1) and the interstitial species  $Na^+$ ,  $Cs^+$  and ( $H_2O$ ) occur in the channels formed by columns of [ $Si_6O_{18}$ ] rings extending along the **c**-axis (Fig. 1a).

Pezzottaite (Fig. 2) is a superstructure of the beryl structure, as suggested by the relation between the cell dimensions (Table 1, Figs. 1 and 2). There are prominent six-membered rings of ( $SiO_4$ ) tetrahedra arranged at the vertices of a simple hexagonal plane net. These rings are linked into a framework by ( $BeO_4$ ) and ( $LiO_4$ ) tetrahedra (Fig. 2), and  $Cs^+$  and  $Na^+$  are incorporated into the prominent channels that extend through the structure along the **c**-axis (Fig. 2a). As with beryl, the pezzottaite structure is very strongly compositionally layered (Fig. 2b) with layers of ( $SiO_4$ ) tetrahedra interleaved with layers of ( $BeO_4$ ) and ( $LiO_4$ ) tetrahedra and ( $AlO_6$ ) octahedra, with alkalis ( $Cs^+$ ,  $Na^+$ ) and ( $H_2O$ ) occurring in the channels. The structure differs from that of beryl (Gibbs *et al.*, 1968; Morosin, 1972; Aurisicchio *et al.*, 1988) and Li-bearing beryl (Bakakin *et al.*, 1969; Hawthorne and Černý, 1977; Sherriff *et al.*, 1991) by having two distinct tetrahedrally coordinated sites, here labeled *Be* (shown in blue in Fig. 2) and *Li* (shown in yellow in Fig. 2) that cross-link the [ $Si_6O_{18}$ ] units.

### Site populations

The assignment of site populations is far from straightforward in these two structures. I assigned scattering factors to the specific sites in each structure, indicating the scattering factors by the italicized labels of the sites. For the reasons discussed by Hawthorne *et al.* (1995), I will express the results of the site-scattering refinement (Tables 6 and 11) in a chemically independent form as effective epfu (electrons per formula unit) such that there is direct correspondence between the refined site-scattering values, site populations, the structural formula and the formula unit of the mineral.

### $Na^+$ , $Cs^+$ , $Li^+$ and ( $H_2O$ ) in beryl

The behaviour of these species is reasonably well-understood in beryl. As discussed above,  $Na^+$  occupies the *2b* site at 0 0 0,  $Cs^+$  occupies the *2a* site at 0 0  $\frac{1}{4}$ , and ( $H_2O$ ) occupies the *2a* site.  $Na^+$  occurs in the plane of the closest ring of *Si* tetrahedra (Fig. 3a) and has 6 bonds of equal length to the bridging O1 atoms.  $Cs^+$  occurs halfway between two six-membered rings of *Si* tetrahedra (Fig. 3b) and has 12 bonds of equal length to the bridging O1 atoms of the two adjacent rings of *Si* tetrahedra (Figs. 3b,c), occupying a hexagonal antiprism.

$Na^+$  occurs at the channel *Na* site where it is coordinated by a planar hexagon of anions at a distance of 2.54 Å (Fig. 3c) which leads to an incident bond-valence of  $0.134 \times 6 = 0.804$  vu

(valence units) where the *Na* site is occupied by  $\text{Na}^+$ , insufficient to satisfy the valence-sum rule (Brown, 2016; Hawthorne, 2012, 2015) at  $\text{Na}^+$ . An  $(\text{H}_2\text{O})$  group at a locally adjacent *2a* site (at a distance of 2.25 Å) will contribute a bond valence of 0.267 vu to the bonded  $\text{Na}^+$ , and to satisfy the valence-sum rule, channel  $\text{Na}^+$  will have to bond to one  $(\text{H}_2\text{O})$  group at an adjacent *2a* site for a local incident bond-valence sum of 1.071 vu. Kolesnikov *et al.* (2018, 2019) showed that in beryl,  $(\text{H}_2\text{O})$  is particularly sensitive to very small differences in the size and local structure of the channel which can cause drastic changes in the confined  $(\text{H}_2\text{O})$  dynamics.

In beryl,  $(\text{H}_2\text{O})$  is commonly described as having two types of occurrence: (1) with the H–H vector of the  $(\text{H}_2\text{O})$  group parallel to the *c*-axis, and (2) with the H–H vector of the  $(\text{H}_2\text{O})$  group perpendicular to the *c*-axis. However, this is not exactly what Wood and Nassau (1968) stated (see above). They defined type-I and type-II  $(\text{H}_2\text{O})$  in terms of the orientation of their 2-fold rotation axis: perpendicular and parallel to the *c*-axis of the crystal. Fig. 4a shows type-II  $(\text{H}_2\text{O})$  bonded to a single  $\text{Na}^+$  ion and the 2-fold rotation axis of the  $(\text{H}_2\text{O})$  group parallel to the *c*-axis. Fig. 4b shows  $(\text{H}_2\text{O})$  bonded to two  $\text{Na}^+$  ions; the 2-fold rotation axis of the  $(\text{H}_2\text{O})$  group is perpendicular to the *c*-axis but the H–H vector is also perpendicular to the *c*-axis, although the arrangement shown in Fig. 4b does not conform well to the valence-sum rule (see above).

One aspect that needs to be considered is the coordination of  $(\text{H}_2\text{O})$ . Type-I  $(\text{H}_2\text{O})$  is coordinated by zero  $\text{Na}^+$  ions, and type-II  $(\text{H}_2\text{O})$  is coordinated by one  $\text{Na}^+$  ion. However, the  $\text{Na}-(\text{H}_2\text{O})$  bond-valence is  $\sim 0.267$  vu (see above) which would result in an incident bond-valence of  $0.267 \times 2 = 0.534$  vu at  $(\text{H}_2\text{O})$ . This is not possible as it would require very strong H...O hydrogen bonds to the anions coordinating  $\text{Si}^{4+}$  and suggests a frequency of absorption in the infrared or Raman spectra lower than that observed ( $3450 \text{ cm}^{-1}$ ) by Lambruschi *et al.* (2014). On balance, the evidence points to  $\text{Na}^+$  being incorporated into beryl as  $\text{Na}^+-(\text{H}_2\text{O})$  and not as  $\text{Na}^+-(\text{H}_2\text{O})_2$ .

$\text{Cs}^+$  occurs at the channel *Cs* site where it is coordinated by a hexagonal antiprism of anions at a distance of 3.43 Å (Figs. 3b,c) which leads to a local incident bond-valence of  $0.0633 \times 12 = 0.760$  vu where *Cs* is occupied by  $\text{Cs}^+$ . This seems somewhat low compared with the valence-sum rule but is well within the variation of 3.21–3.54 Å given by Gagné and Hawthorne (2016) for ninety  $(\text{CsO}_{12})$  polyhedra. The separation between the *2a* and *2b* sites along the channel in beryl is  $\sim 2.31$ – $2.32$  Å which places significant constraints on what species can occupy locally adjacent *2a* and *2b* sites. This issue was examined by Hawthorne and Černý (1977) who noted that neither  $\text{Cs}^+$  and  $\text{Na}^+$  nor  $\text{Cs}^+$  and  $(\text{H}_2\text{O})$  can occupy locally adjacent *2a* and *2b* sites. This conclusion is in accord with the observed ranges of  $^{121}\text{Cs}^+-\text{O}^{2-}$  and  $^{6}\text{Na}^+-\text{O}^{2-}$  distances in inorganic structures: 2.910–4.072 and 2.019–3.055 Å, respectively (Gagné and

Hawthorne, 2016). Hence Cs<sup>+</sup> and (H<sub>2</sub>O) cannot occupy locally adjacent 2*a* and 2*b* sites whereas Na<sup>+</sup> and (H<sub>2</sub>O) can occupy locally adjacent 2*a* and 2*b* sites (Hawthorne and Černý, 1977).

Li<sup>+</sup> substitutes for Be<sup>2+</sup> at the *Be* site and there is a reasonably well-developed relation between the variation in the <*Be*–O> distance and the amount of Li<sup>+</sup> in the structure (Sherriff *et al.*, 1991). We may write the incorporation of Li<sup>+</sup> into the ideal beryl structure as follows: (Cs<sup>+</sup>,Na<sup>+</sup>) + Li<sup>+</sup> → □ + Be<sup>2+</sup> [we will look at the effect of (H<sub>2</sub>O) later]. This is a long-range description that specifies how overall electroneutrality in the structure is maintained. However, what about short-range issues; how is the valence-sum rule (Brown, 2016; Hawthorne, 2012, 2015) maintained where this incorporation occurs? Inspection of Table 5 shows that the ions at the *Be*, *Al*, *Cs* and *Na* sites are each coordinated by only one crystallographically distinct O<sup>2-</sup> ion whereas Si<sup>4+</sup> is coordinated by two crystallographically distinct O<sup>2-</sup> ions: O1 and O2. Inspection of Figs. 1a and 3 show that Cs<sup>+</sup> and Na<sup>+</sup> do not bond to anions that coordinate the *Be* site in beryl: Cs<sup>+</sup> and Na<sup>+</sup> bond only to O1 whereas Be<sup>2+</sup> (and Li<sup>+</sup>) bond only to O2 (Table 5). Where Li<sup>+</sup> is incorporated at the *Be* site, the bond valence incident at O2 from the ions at the *Be* site must decrease. This decrease in bond valence must be compensated by bond valence contributed to the structure by Cs<sup>+</sup> and Na<sup>+</sup> at the channel site. However, the ions at the channel site do not bond to the O2 anion and hence cannot contribute directly to O2; Cs<sup>+</sup> and Na<sup>+</sup> bond to O1 and the influence of their additional bond valence is transferred to O2 by cooperative change in bond lengths within the (SiO<sub>4</sub>) tetrahedron. This mechanism is shown in Fig. 5. Where Li<sup>+</sup> occupies the *Be* site, the bond valence of the <sup>Be</sup>Li<sup>+</sup>–O2 bond decreases (shown by yellow bonds in Fig. 5a). Bond valence from the incorporated Cs<sup>+</sup> and Na<sup>+</sup> is transferred to O1 to Si<sup>4+</sup> to O2 as indicated by the path of red-yellow-red bonds in Fig. 5a. The long-range consequences of this mechanism will be to shorten the two Si–O2 distances as Li<sup>+</sup> and (Cs<sup>+</sup>,Na<sup>+</sup>) increase. In turn, the mean of the two Si–O1 distances will increase in order to maintain the valence-sum rule at Si<sup>4+</sup>. Figs. 5b,c show that the variation in Si–O bond-lengths is in accord with this mechanism.

This mechanism is apparent in the bond-valence table for beryl (Table 7). Cations at *Cs* and *Na* bond to O1 and the Si–O1 bond-valences are correspondingly less than the Si–O2 bond-valence which compensates somewhat for the reduced *Be*–O2 bond-valence due to the presence of Li<sup>+</sup> at the *Be* site.

### Na<sup>+</sup>, Cs<sup>+</sup>, Li<sup>+</sup>, K<sup>+</sup> and (H<sub>2</sub>O) in pezzottaite

The pezzottaite structure is bond-topologically analogous to the beryl structure but differs in having a larger unit-cell and lower space-group symmetry, giving rise to a greater number of

crystallographically distinct sites and different point symmetries of those sites (Figs. 1, 2; Table 1).

#### *Occupancy of the Na1 and Na2 sites*

There are two crystallographically distinct Na sites, Na1 and Na2, and two crystallographically distinct Cs sites, Cs1 and Cs2, all of which occur in the channels bounded by [Si<sub>6</sub>O<sub>18</sub>] rings (Fig. 2a). The lower symmetry and larger unit cell of pezzottaite (relative to those of beryl) complicate the assignment of site populations, particularly as both the different Na sites and different Cs sites have different point symmetry (Table 1).

Fig. 6a shows the variation in the refined total scattering at the (Na1 + Na2) sites (red circles) as a function of the Na<sup>+</sup> content analyzed by EMPA and expressed in epfu. The data lie above the 1:1 line, indicating that another scattering species also occurs at the Na1 and/or Na2 sites. Crystals P1 and P2 depart from the 1:1 line far more than the other crystals and inspection of Table 13 shows that these two crystals contain significantly more Ca<sup>2+</sup> than the other crystals in the figure. In Fig. 6b, the refined scattering from the Na sites has been corrected for the presence of Ca<sup>2+</sup> at these sites and now accords with the 1:1 line, indicating that Ca<sup>2+</sup> also occupies one or more of the Na sites.

#### *Occupancy of the Cs1 and Cs2 sites*

Fig. 7a shows the variation in the refined total scattering at the (Cs1 + Cs2) sites (red circles) and at the Cs1 site (green circles) in pezzottaite as a function of the (Cs<sup>+</sup> + Rb<sup>+</sup>) content analyzed by EMPA and expressed in epfu. It is immediately apparent that the total scattering at the Cs1 + Cs2 sites exceeds that of the Cs<sup>+</sup> and Rb<sup>+</sup> from EMPA, and the scattering at Cs1 is less than that of the Cs<sup>+</sup> and Rb<sup>+</sup> from EMPA. Hence both Cs1 and Cs2 must be occupied by Cs<sup>+</sup>, and each site must also be occupied by another scattering species. Fig. 7b shows the effect of assigning type-II (H<sub>2</sub>O) to Cs1 and Cs2 and subtracting the amounts of scattering due to this (H<sub>2</sub>O) for Na bonding to one (H<sub>2</sub>O) (yellow circles). This brings the data significantly closer to the 1:1 line in Fig. 7b. Moreover, infrared and Raman spectroscopy (Hawthorne *et al.*, 2004; Gatta *et al.*, 2012; Lambruschi *et al.*, 2014) indicate the presence of both type-I and type-II (H<sub>2</sub>O) in pezzottaite, and hence we may attribute the displacement of the data from the 1:1 line in Fig. 7b to the presence of type-I (H<sub>2</sub>O) at the Cs1 and Cs2 sites. Thus, Cs1 and Cs2 are occupied by Cs<sup>+</sup>, type-I (H<sub>2</sub>O) and type-II (H<sub>2</sub>O) in pezzottaite.

#### *Differences between the Cs1 and Cs2 sites and between the Na1 and Na2 sites*



Details of the coordinations of these sites are shown in Fig. 8. Cs1 and Cs2 are both [12]-coordinated but there are significant differences in the arrangements of next-next-nearest polyhedra. Inspection of Fig. 8a shows that the two [Si<sub>6</sub>O<sub>18</sub>] rings that surround the Cs1 site are linked by a single 12-membered ring of edge-sharing polyhedra that contains three (BeO<sub>4</sub>) tetrahedra, three (LiO<sub>4</sub>) tetrahedra and six Al octahedra that girdle the channel at the height of the Cs1 site. In contrast, the two [Si<sub>6</sub>O<sub>18</sub>] rings that surround the Cs2 site are linked by a single 12-membered ring of six (BeO<sub>4</sub>) tetrahedra and six Al octahedra. Fig. 8b shows the same arrangement as Fig. 8a except viewed in the opposite direction. Fig. 8c shows the next-next-nearest arrangements of polyhedra surrounding the Na1 and Na2 sites in which the single [Si<sub>6</sub>O<sub>18</sub>] ring that surrounds each of the Na sites is girdled by two 12-membered rings of edge-sharing polyhedra. The rings surrounding both the Na1 and Na2 sites consist of three (BeO<sub>4</sub>) tetrahedra, three (LiO<sub>4</sub>) tetrahedra and six Al octahedra (Fig. 8c). When viewed from the opposite direction as in Fig. 8d, the top ring girdling Na1 consists of three (BeO<sub>4</sub>) tetrahedra, three (LiO<sub>4</sub>) tetrahedra and six Al octahedra whereas the top ring girdling Na2 consists of six (BeO<sub>4</sub>) tetrahedra and six Al octahedra. Thus (1) the Cs1 and Na1 sites are locally associated with six (LiO<sub>4</sub>) tetrahedra; (2) the Na2 site is locally associated with three (LiO<sub>4</sub>) tetrahedra; and (3) the Cs2 site is not locally associated with any (LiO<sub>4</sub>) tetrahedra.

#### *Occupancies of the Be and Li sites*

It was not possible to reliably refine the Be<sup>2+</sup> and Li<sup>+</sup> occupancies at the Be and Li sites and it was necessary to make an initial assignment on little evidence. I will now examine the validity of these initial assignments. I will deal with site populations directly as apfu as these were not refined for the Be and Li sites but were assigned and fixed during structure refinement.

The variation in <Be–O> distance as a function of the assigned site-population at the Be site for both beryl (red circles) and pezzottaite (green circles) is shown in Fig. 9a. The lack of a (expected) linear relation indicates that the initial assigned site-populations are not correct. In particular, there is a wide dispersion of the <Be–O> distance in pezzottaite for which the site population was assigned as 2 Be<sup>2+</sup> apfu. Gagné and Hawthorne (2016) listed the grand <Be<sup>2+</sup>–O<sup>2–</sup>> distance in 161 tetrahedra in inorganic structures as 1.637 Å, close to the values of the three lowest data for pezzottaite in Fig. 9a. The pezzottaite crystals with the aberrantly large <Be–O> distances are P4 and P12 which are the only pezzottaite crystals identified in Table 2 as “weakly rhombohedral”. The data for beryl in Fig. 9a correspond to the curve of Sherriff *et al.* (1991), shown as the red line in Fig. 9b, which runs through the grand <Be–O> distance of Morosin (1972) and Gibbs *et al.* (1968) for Li-free beryl indicated by the pink square. It seems



reasonable to suggest that the weakly rhombohedral refinements of pezzottaite P4 and P12 have significant  $\text{Li}^+$  at their *Be* sites, and these amounts may be calculated as indicated by the dotted lines in Fig. 9b.

The variation in  $\langle \text{Li-O} \rangle$  distance as a function of the assigned site-population at the *Li* site for pezzottaite is shown in Fig. 10a. The data for four pezzottaite structures show a linear relation but crystals P4 and P12 deviate strongly from this relation. However, in Fig. 9b, some  $\text{Li}^+$  was reassigned to the *Be* site in P4 and P12, decreasing the amount of  $\text{Li}^+$  at the *Li* site in these crystals. This change in assigned  $\text{Li}^+$  at the *Li* site is shown in Fig. 10b where it is seen that this reassignment brings linearity to both relations in Figs. 9 and 10. Thus in compositions approximately halfway between beryl and pezzottaite, there is significant disorder of  $\text{Be}^{2+}$  and  $\text{Li}^+$  at the two distinct tetrahedrally coordinated *Be* and *Li* sites.

#### *Replacement of ${}^{\text{Li}}\text{Be}^{2+}$ by ${}^{\text{Li}}\text{Li}^+$ and the valence-sum rule*

The lower symmetry in pezzottaite when compared with beryl (Table 1) allows a slightly different style of structural adjustment to accommodate the replacement of  $\text{Be}^{2+}$  by  $\text{Li}^+$  in the *Li* tetrahedron and to conform with the valence-sum rule.

The mechanism is shown in Fig. 11: the yellow bonds  ${}^{\text{Li}}\text{Li-O5}$  and  ${}^{\text{Li}}\text{Li-O8}$  have lower bond-valences than where the *Li* site is occupied by  $\text{Be}^{2+}$ . In the channel,  $\text{Cs}^+$  at *Cs1* (Fig. 11a) and  $\text{Na}^+$  at *Na1* (Fig. 11b) bond to  $\text{O}^{2-}$  anions coordinating  $\text{Si}^{4+}$ . Thus in Fig. 11a, *Cs1-O3* bonds provide additional bond-valence to the *O3* anions, causing the *O3-Si1* bonds to weaken as required by the valence-sum rule at *O3* (indicated by the grey bonds), and in turn the valence-sum rule at *Si1* requires a stronger (red) bond to *O8* which compensates for the weaker bond (yellow) from  ${}^{\text{Li}}\text{Li}^+$  compared to where *Li* was occupied by  $\text{Be}^{2+}$ . However, the lower symmetry of pezzottaite compared to that of beryl also allows  $\text{Al}^{3+}$  at *A1* and *A2* to participate in the bond-valence-transfer mechanism. Four of the bonds coordinating each *Al* octahedron are weakened by this mechanism and bonds *A1-O5* and *A2-O8* are strengthened (this is apparent in Table 9), also compensating for the weaker  ${}^{\text{Li}}\text{Li-O5}$  and  ${}^{\text{Li}}\text{Li-O8}$  bonds.

Fig. 11b shows the analogous mechanism for channel  $\text{Na}^+$  at *Na1*; note that Fig. 11b has a different orientation to Fig. 11a in order that the arrangement of *Be* and *Li* tetrahedra are the same in both figures. Channel  $\text{Na}^+$  at *Na1* bonds to *O3*, weakening the *O3-Si1* bonds (and the bond to *O6* that coordinates  $\text{Be}^{2+}$  at the *Be* site), with the result that the *Si1-O8* bond is strengthened and compensates for the weaker  ${}^{\text{Li}}\text{Li-O8}$  bond. The *O5* anion receives additional bond-valence from a bond out of the plane of Fig. 11b. Thus far, the effect of *Be-Li* order on the distribution of channel ( $\text{H}_2\text{O}$ ) has not been considered. The latter must occur at the *2a* site in

beryl (Figs. 3a,b) and by analogy at the 6a and 12c sites in pezzottaite (Figs. 8a,b). These mechanisms are apparent in the bond-valence table for pezzottaite (Table 12). Cations at Cs1, Cs2 and Na2 bond to O1 and O2 and  $S2-O1$  and  $S2-O2$  bond-valences reduce accordingly. The bond valence for  $S2-O5$  increases together with that of  $A1-O5$  to compensate for  $Li^+$  bonding to O5. Cations at Cs1 and Na1 bond to O3 and  $S1-O3$  bond-valences reduce accordingly. The bond valence for  $S1-O8$  increases together with that of  $A2-O8$  to compensate for  $Li^+$  bonding to O8.

#### Order of $Cs^+$ over Cs1 and Cs2

It is important to note that because the Cs sites are occupied by ( $Cs^+ + Rb^+$ ) and ( $H_2O$ ), we cannot assign real site occupancies because we have four scattering species (Cs, Rb, ( $H_2O$ ) and  $\square$ ) distributed over two sites. The case is similar for the Na sites which contain the scattering species Na, Ca and  $\square$ . Thus we may examine only the total scattering (expressed as  $Cs^+$  and  $Na^+$ ) ordered over the pairs of Cs and Na sites.

Fig. 12a shows the relative order of  $Cs^+$  over the Cs1 and Cs2 sites and Fig. 12b shows the relative order of  $Na^+$  over the Na1 and Na2 sites.  $Cs^+$  is strongly ordered at the Cs1 site with a well-developed linear correlation except for crystals P4 and P12.  $Na^+$  is disordered over the Na1 and Na2 sites, again with a well-developed linear correlation except for crystals P4 and P12. Inspection of Figs. 9 and 10 shows that crystals P4 and P12 differ from the other pezzottaites by having  $Li^+$  partly disordered between the Be and Li sites whereas the other pezzottaite crystals have the Be site completely occupied by  $Be^{2+}$  and the Li site occupied by  $Be^{2+}$  and  $Li^+$ . This means that crystals P4 and P12 have a beryl-like component in their structure in which  $Li^+$  occupies the Be site and there is only one Cs site and one Na site. The mechanism of local satisfaction of the valence-sum rule pictured in Fig. 11 indicates that  $Cs^+$  should preferentially occupy the Cs sites that are most locally associated with the ( $LiO_4$ ) tetrahedra, *i.e.* Cs1 (Fig. 8a,b), and ( $H_2O$ ) should preferentially occupy the Cs2 site that is locally associated with the ( $BeBeO_4$ ) tetrahedra.

#### Order of $Na^+$ over Na1 and Na2

Similarly,  $Na^+$  should occupy the Na sites that are most locally associated with the ( $LiO_4$ ) tetrahedra, *i.e.* Na1 (Fig. 8c,d). The ordering of  $Cs^+$  is stronger than the ordering of  $Na^+$  as the contrast between the numbers of next-nearest ( $LiO_4$ ) is greater for the Cs sites than for the Na sites (Fig. 8). The mixing of a beryl-like component into the ordering of  $Li^+$  and  $Be^{2+}$  (as in crystals P4 and P12) will decrease the drive for ordering of  $Cs^+$  and  $Na^+$  over the Cs and Na

sites and lead to the deviations from linearity shown in Fig. 12.

### Crystal-chemical constraints on channel constituents

Schematics of the sequence of the *Cs* and *Na* sites in a single channel in the beryl and pezzottaite structures are shown in Fig. 13 and the distances between sites in the refined pezzottaite structures are shown in Table 14. The distances listed in Table 14 are too short to allow ions to occur locally at both constituent sites, and this effect propagates along the channel to generate complicated constraints on the overall chemical variation in channel constituents.

#### *Possible channel arrangements in beryl*

These are shown in Fig. 13a: (a)  $\text{Cs}^+$  at *2a* forces vacancies at the two adjacent *2b* sites; (b) type-I ( $\text{H}_2\text{O}$ ) at *2a* forces vacancies at the two adjacent *2b* sites; (c)  $\text{Na}^+$  at *2b* forces type-II ( $\text{H}_2\text{O}$ ) at one adjacent *2a* site and a vacancy at the other adjacent *2a* site, and the type-II ( $\text{H}_2\text{O}$ ) at the adjacent *2a* site forces a vacancy at the adjacent *2b* site; (d) as (c) except oriented in the opposite direction along the *c*-axis.

Arrangements (c) and (d) strongly limit the amount of  $\text{Na}^+$  that can be incorporated in beryl: each  $\text{Na}^+$ –( $\text{H}_2\text{O}$ ) bonded pair also forces two vacancies at the adjacent *2a* and *2b* sites, and hence the maximum amount of  $\text{Na}^+$  that can be incorporated in beryl is 0.50 apfu with an associated 0.50 ( $\text{H}_2\text{O}$ ) pfu. Arrangement (a) provides a limit on the aggregate amount of Na and Cs: each  $\text{Cs}^+$  ion blocks two *2b* ( $\text{Na}^+$ ) sites and hence the maximum amount of Cs and Na obeys the constraint  $\text{Cs}^+ + 2\text{Na}^+ = 1$  apfu. Although arrangement (b) blocks two adjacent *2b* sites, *2b* is occupied only by  $\text{Na}^+$ , and occupancy of one of the blocked sites would change the type-I ( $\text{H}_2\text{O}$ ) to type-II ( $\text{H}_2\text{O}$ ) and generate arrangement (c) and (d).

#### *Possible channel arrangements in pezzottaite*

These are shown in Fig. 13b: although the lower symmetry and larger unit-cell in pezzottaite relative to beryl gives more distinct crystallographic arrangements, the number of crystal-chemical arrangements and the site separations are the same (Table 14). Both minerals have alternating *Cs* and *Na* sites along the *c*-axis and hence the constraints are the same: (e)  $\text{Cs}^+$  at *12c* (*Cs*1, Table 1) forces vacancies at the two adjacent *Na*1(*6b*) and *Na*2 (*12c*) sites, and (f)  $\text{Cs}^+$  at *6a* (*Cs*2, Table 1) forces vacancies at the two adjacent *Na*2 (*12c*) sites; (g) type-I ( $\text{H}_2\text{O}$ ) at *12c* (*Cs*1, Table 1) forces vacancies at the adjacent *Na*1(*6b*) and *Na*2 (*12c*) sites, and (h) type-I ( $\text{H}_2\text{O}$ ) at *6a* (*Cs*2) forces vacancies at the two adjacent *Na*2 (*12c*) sites; (i,j)  $\text{Na}^+$  at *6b* (*Na*1, Table 1) forces type-II ( $\text{H}_2\text{O}$ ) at the adjacent *Cs*1 (*12c*) and vacancies at the adjacent *Cs*1

(6a) and Na2 (12c) sites along both +c and -c; (k,l) Na<sup>+</sup> at 12c (Na2, Table 1) forces type-II (H<sub>2</sub>O) at the adjacent Cs1 site and vacancies at the adjacent Cs2 (6a) and Na1 (6b) sites along both +c and -c.

Although the details of the stereochemistry are more complicated in pezzottaite than in beryl, the compositional constraints are basically the same: (1) each Cs<sup>+</sup> (or Rb<sup>+</sup>) ion blocks two Na sites irrespective of whether Cs<sup>+</sup> (or Rb<sup>+</sup>) occupies Cs1 or Cs2 and hence the maximum amount of Cs<sup>+</sup> and Na<sup>+</sup> obeys the constraint  $Cs^{+} + Rb^{+} + 2Na^{+} = 1$  apfu; (2) at full occupancy of the Cs1 and Cs2 sites by Cs<sup>+</sup> + Rb<sup>+</sup>, there is no room for (H<sub>2</sub>O) in the channel and hence there cannot be any Na<sup>+</sup>, which is also in accord with the requirement of electroneutrality of the structure. Incidentally, if the Cs1 and Cs2 sites are completely occupied by Cs<sup>+</sup>, there is no reason why this composition should not have the beryl structure *sensu stricto*. Unlike beryl, pezzottaite seems to incorporate small amounts of Ca<sup>2+</sup> in the channels. This substitution adds an additional electroneutrality constraint to compositional variation in pezzottaite.

Inspection of Table 13 shows the presence of minor amounts of K<sup>+</sup> (0.005–0.019 apfu) in the channel of the pezzottaite structure: where exactly does K<sup>+</sup> occur? We may use the bond-valence parameters for K<sup>+</sup>–O<sup>2-</sup> (Gagné and Hawthorne, 2015) to consider this issue. If K<sup>+</sup> were to occur at the Na1 or Na2 sites, the incident bond-valence at K<sup>+</sup> would be ~1.8 vu; if K<sup>+</sup> were to occur at the Cs1 or Cs2 sites, the incident bond-valence at K<sup>+</sup> would be ~0.4 vu; neither of these possibilities satisfy the valence-sum rule and hence they may be ruled out. The valence-sum rule is satisfied for <sup>[5]</sup>K<sup>+</sup> by a K<sup>+</sup>–O<sup>2-</sup> distance of 2.688 Å which requires that K<sup>+</sup> occur at approximately 0 0 ±0.0326 and/or 0 0 0.1307/0.1959. There are various other possibilities if K<sup>+</sup> bonds to type-II (H<sub>2</sub>O) within the channel.

### The join beryl-pezzottaite

Fig. 14 shows the variation in (Cs<sup>+</sup> + Rb<sup>+</sup>) and (Na<sup>+</sup> + Ca<sup>2+</sup>) along the beryl-pezzottaite join for the structures reported here and for selected compositions from the literature. As discussed above, compositions lie below the line  $(Cs^{+} + Rb^{+}) + 2(Na^{+} + Ca^{2+}) = 1$  apfu (except for the incommensurate structures around  $(Cs^{+} + Rb^{+}) \approx 0.50$  apfu which will be discussed later), supporting the constraint that Na<sup>+</sup> and Ca<sup>2+</sup> bond to only one channel (H<sub>2</sub>O) group. The constraint  $(Cs^{+} + Rb^{+}) + 2(Na^{+} + Ca^{2+}) = 1$  apfu needs to be modified slightly to maintain electroneutrality:  $(Cs^{+} + Rb^{+}) + 2(Na^{+} + Ca^{2+}) = 1 - 2Ca^{2+}$  apfu. This is apparent from Fig. 14, which shows that the pezzottaite compositions tend to lie slightly below the line  $(Cs^{+} + Rb^{+}) + 2(Na^{+} + Ca^{2+}) = 1$  apfu due to the presence of small amounts of Ca<sup>2+</sup> (Table 13). Taking a value of Ca<sup>2+</sup> = 0.03 apfu (Table 13), the heavy black line in Fig. 14 indicates the maximum amount of

$\text{Na}^+ + \text{Ca}^{2+}$  allowed by a combination of channel-cation and ( $\text{H}_2\text{O}$ ) interactions and the constraint of electroneutrality, and this line passes through the data for pezzottaite.

The distribution of compositions across the beryl-pezzottaite join is very non-uniform. The maximum ( $\text{Na}^+ + \text{Ca}^{2+}$ ) content occurs for ( $\text{Cs}^+ + \text{Rb}^+$ ) contents close to zero and ( $\text{Na}^+ + \text{Ca}^{2+}$ ) contents are fairly uniform from 0.0–0.50 apfu typical of NYF (Niobium, Yttrium and Fluorine enriched) pegmatites (*sensu lato*) and other parageneses. Significant incorporation of  $\text{Cs}^+$  is typical of LCT (Lithium, Cesium and Tantalum enriched) pegmatites, but is also accompanied by the incorporation of significant  $\text{Na}^+$ . The result is a large area across the beryl-pezzottaite join in which beryl and pezzottaite compositions do not occur (or have not yet been found); this area is delimited by the dashed red line in Fig. 14. Is this blank area (1) the result of restricted source-rock compositions; (2) due to the fact that extreme fractionation enriches both  $\text{Cs}^+$  and  $\text{Na}^+$ ; or (3) the result of crystal-chemical factors: the aggregate ( $\text{Cs}^+ + \text{Rb}^+$ ) and ( $\text{Na}^+ + \text{Ca}^{2+}$ ) contents are restricted by the relation  $(\text{Cs}^+ + \text{Rb}^+) + 2(\text{Na}^+ + \text{Ca}^{2+}) = 1$  apfu that arises because of the requirement of channel  $\text{Na}^+$  to bond to one channel ( $\text{H}_2\text{O}$ ) group? A combination of all three factors is probably involved.

#### *Incommensurate structures*

What gives rise to the incommensurate structures at intermediate compositions? Fig. 5a shows how the channel constituents in beryl satisfy the local bond-valence requirements of the anions coordinating the *Be* site where it is occupied by  $\text{Li}^+$ . However, this mechanism addresses the local bond-valence requirements of only two of the four anions coordinating  $^{\text{Be}}\text{Li}^+$ . The other two anions of the ( $\text{BeO}_4$ ) tetrahedron containing  $\text{Li}^+$  face an adjacent channel: their bond-valence requirements must be satisfied by alkali cations in that adjacent channel. In this way, adjacent channels in the beryl structure affect each other. Inspection of Fig. 8a,b shows that where adjacent channels contain  $\text{Cs}^+$  at the same level along **c**, the local bond-valence requirements of the anions coordinating  $^{\text{Be}}\text{Li}^+$  are satisfied by the  $\text{Cs}^+$  in these adjacent channels, *i.e.* by □... $\text{Cs}^+$ ...□ arrangements. The situation where  $\text{Na}^+$  is involved in satisfying the local bond-valence requirements of the anions coordinating  $^{\text{Be}}\text{Li}^+$  is completely different. Inspection of Fig. 8c,d shows that the bond path from  $\text{Na}^+$  to ( $^{\text{Be}}\text{LiO}_4$ ) links only to one anion of the tetrahedron, unlike the case where  $\text{Cs}^+$  is the local channel constituent and has two bond paths to a specific Li-containing ( $\text{BeO}_4$ ) tetrahedron. In order for the two anions of the ( $^{\text{Be}}\text{LiO}_4$ ) tetrahedron in a specific channel to have their bond-valence requirements satisfied by channel  $\text{Na}^+$ , *Na* sites locally adjacent along **c** must be occupied (Figs. 15a,b). Where this is the case, the constraints outlined in Fig. 13a extend the channel arrangements involving  $\text{Na}^+$  beyond the length of the *c*-

dimension. This effect is shown in Figs. 15 and 16: (1) Na<sup>+</sup> occurs at the *Na* (2*b*) site both above and below the level of the (<sup>Be</sup>LiO<sub>4</sub>) tetrahedron; (2) each Na<sup>+</sup> must bond to a type-II (H<sub>2</sub>O) group each of which occupies a *Cs* (2*a*) site; (3) each type-II (H<sub>2</sub>O) group must have a vacancy on the side not bonded to Na<sup>+</sup>. This gives the channel sequence □...(H<sub>2</sub>O)–Na<sup>+</sup>–□–Na<sup>+</sup>–(H<sub>2</sub>O)...□ which is ~14 Å long (Fig. 16), much longer than the *c*-dimension. The unoccupied 2*a* and 2*b* sites that complete an ordered string of cations + vacancies can be occupied by □...□, Cs<sup>+</sup>...□, (H<sub>2</sub>O)...□ or (H<sub>2</sub>O)...Na<sup>+</sup> and these arrangements can point both ways along the *c*-axis. These arrangements break the translational symmetry of ~9.22 Å along *c* and the resultant arrangements will have a pseudo-repeat of approximately double this value, the exact value of the repeat depending on the occupancies of the pair of 2*a* and 2*b* sites that dominate in a particular channel (*i.e.* the structure is incommensurate along *c*). This will result in an approximate repeat of 18.52 Å along *c*. Adjacent channels will be disordered relative to each other and thus the *a*-dimensions remain ~9.22 Å and the space group is still *P6/mcc*.

Of course, this effect will not be apparent in compositions with negligible Li<sup>+</sup> (*e.g.* the bulk of the compositions marked by stars in Fig. 14) in which the incorporation of channel Na<sup>+</sup> is balanced by replacement of <sup>[6]</sup>Al<sup>3+</sup> by <sup>[6]</sup>(Mg,Fe<sup>2+</sup>).

### X-ray topography

Nanoscale variations in crystal texture may be characterized by X-ray topography. Liu *et al.* (2006) examined gem-quality pezzottaite from Madagascar using monochromatic synchrotron radiation to measure the variation in diffracted intensity for a specific reflection as a function of variation of angle away from its ideal diffraction angle; the variation in intensity as a function of angular displacement is known as a rocking curve. For a perfect crystal, the rocking curve will consist of a single peak centered on the ideal diffraction angle. Deviations from ideal crystallinity will result in an asymmetric peak or several closely spaced peaks depending on the character of the microtexture. Liu *et al.* (2006) collected rocking curves for the reflections (006), (0012) and (0018) for seven pezzottaite crystals. The rocking curves showed significant variation from sample to sample: some showed a single distorted peak indicating “fairly good crystallinity” and others showed a broad intensity with several maxima (Fig. 17). The presence of several maxima in Fig. 17 is consistent with our finding that pezzottaite grains commonly consist of heterogeneous intergrowths of twinned pezzottaite and Cs-rich beryl.

### Occurrence

The extreme enrichment of Cs in pezzottaite suggests that pezzottaite should occur in highly



fractionated LCT pegmatites. Simmons *et al.* (2004, page 116) stated that “in Madagascar, pezzottaite occurs in a pegmatite that has characteristics of both the LCT (Lithium-Cesium-Tantalum) and NYF (Niobium-Yttrium-Fluorine) families of the Rare-Element and Mirolitic pegmatite classes”. The Afghanistan occurrences are associated with large-scale LCT pegmatite fields. The most intensely investigated occurrence is in the Julianna pegmatitic system at Piława G´orna, Sudetes, SW Poland (Pieczka *et al.*, 2016), where similar to the Madagascar occurrence, the host pegmatite is of hybrid NYF-LCT character and pezzottaite occurs in rare highly fractionated LCT pods in more extensive NYF phases. Review of the development of pegmatite classifications over the past ~100 years (Müller *et al.*, 2022) has noted that pegmatites described as having a “mixed” or “hybrid” character have been particularly problematic due to their combined NYF and LCT mineralogical and chemical features. Their genetic interpretation is often ambiguous, at times leading to misidentification, and the classification of Wise *et al.* (2022) uses a much broader array of criteria while maintaining the useful aspects of previous classifications. The occurrences of pezzottaite highlight the complexity of the “hybrid-character” pegmatites and emphasize the need for detailed careful study such as that of the Julianna pegmatite (Pieczka *et al.*, 2016).

## Coda

- [1] All crystals with  $(Cs^+ + Rb^+) \geq \sim 0.5$  apfu are microscale mixtures of more than one structure although all crystals showed diffraction spots that appeared sharp and uniform to the eye.
- [2] Three distinct phases were identified with different diffraction characteristics: (1) hexagonal ( $P6/mcc$ ) Cs-rich beryl; (2) hexagonal-rhombohedral ( $R\bar{3}c$ ) twinned pezzottaite; (3) two crystals showed an approximate doubling of the beryl *c*-axis but the additional spots are incommensurate, and indexing gave *l* indices deviating from integer values by  $\pm 0.05$ – $0.10$ .
- [3] Note that the rhombohedral refinements do not explicitly account for the presence of an intergrown hexagonal component.
- [4] Two pezzottaite crystals with compositions close to 50% (with weak rhombohedral reflections) show some disorder of  $Li^+$  over the *Li* and *Be* sites whereas pezzottaite crystals with higher  $Cs^+$  (and  $Li^+$ ) content and strong rhombohedral reflections show the *Be* site occupied only by  $Be^{2+}$  and the *Li* site occupied by both  $Li^+$  and  $Be^{2+}$ .
- [5] The ordering of  $(Cs^+ + Rb^+)$  and  $(Na^+ + Ca^{2+})$  in pezzottaite is driven by the incident bond-valence requirements of the anions coordinating the  $(LiO_4)$  tetrahedron.
- [6] The occurrence of an incommensurate phase at intermediate compositions is due to the interaction of the species in adjacent columns of the  $P6/mcc$  beryl structure.



- [7] The valence-sum rule requires both  $\text{Na}^+$  and  $\text{Ca}^{2+}$  to bond to one channel (type-II) ( $\text{H}_2\text{O}$ ) group.
- [8] As a result of [7], the compositions along the beryl-pezzottaite join must lie below the line  $(\text{Cs}^+ + \text{Rb}^+) + 2(\text{Na}^+ + \text{Ca}^{2+}) = 1$  apfu. This relation is modified by the requirement of electroneutrality to become  $(\text{Cs}^+ + \text{Rb}^+) + 2(\text{Na}^+ + \text{Ca}^{2+}) = 1 - 2\text{Ca}^{2+}$  apfu.
- [9] There is a large area of the (ideally possible) beryl-pezzottaite compositional field that is (currently) unoccupied by analyzed compositions; the reason(s) for this are not well-understood.

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**Competing interests.** The author declares none.

**Supplementary material.** To view supplementary material for this article, please visit <https://doi.org/...>

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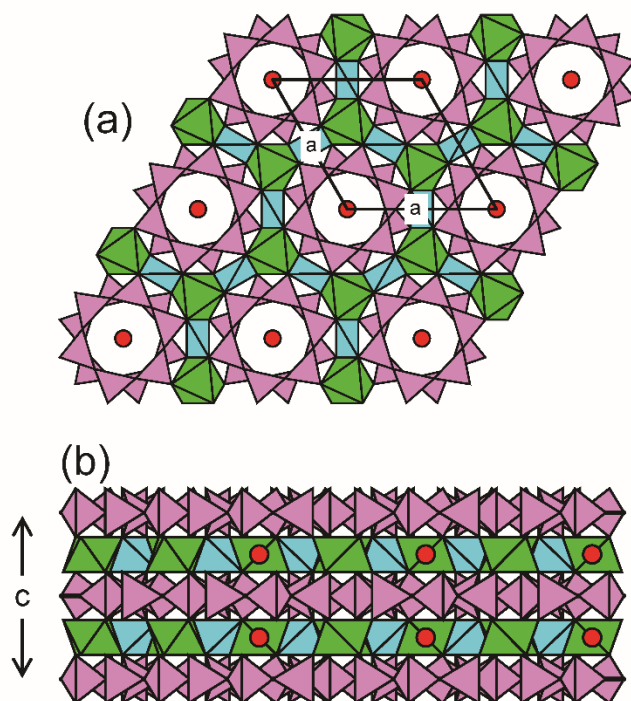
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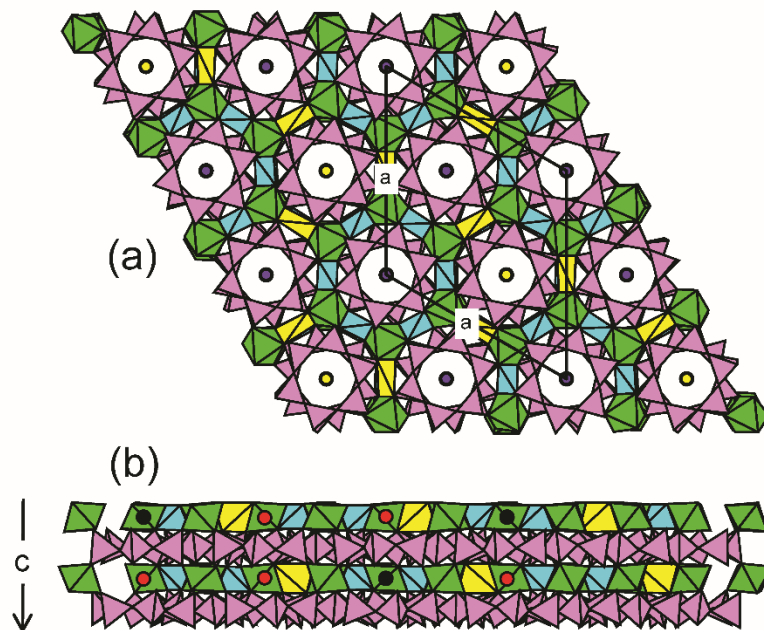
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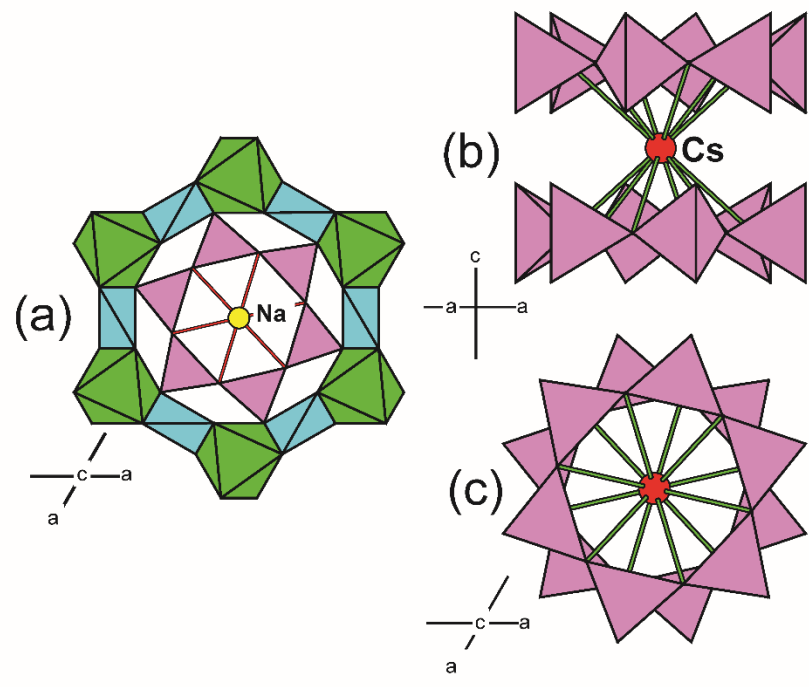
**Fig. 1.** The crystal structure of beryl (a) projected down the **c**-axis, and (b) viewed orthogonal to the **c**-axis; *Si* tetrahedra are mauve, *Be* tetrahedra are pale blue, *Al* octahedra are bright green, Cs atoms are red circles, Na atoms are concealed beneath the Cs atoms.



**Fig. 2.** The crystal structure of pezzottaite (a) projected down the **c**-axis, and (b) viewed orthogonal to the **c**-axis; colour scheme as in Fig. 1 plus Li tetrahedra are yellow and Na atoms are yellow.

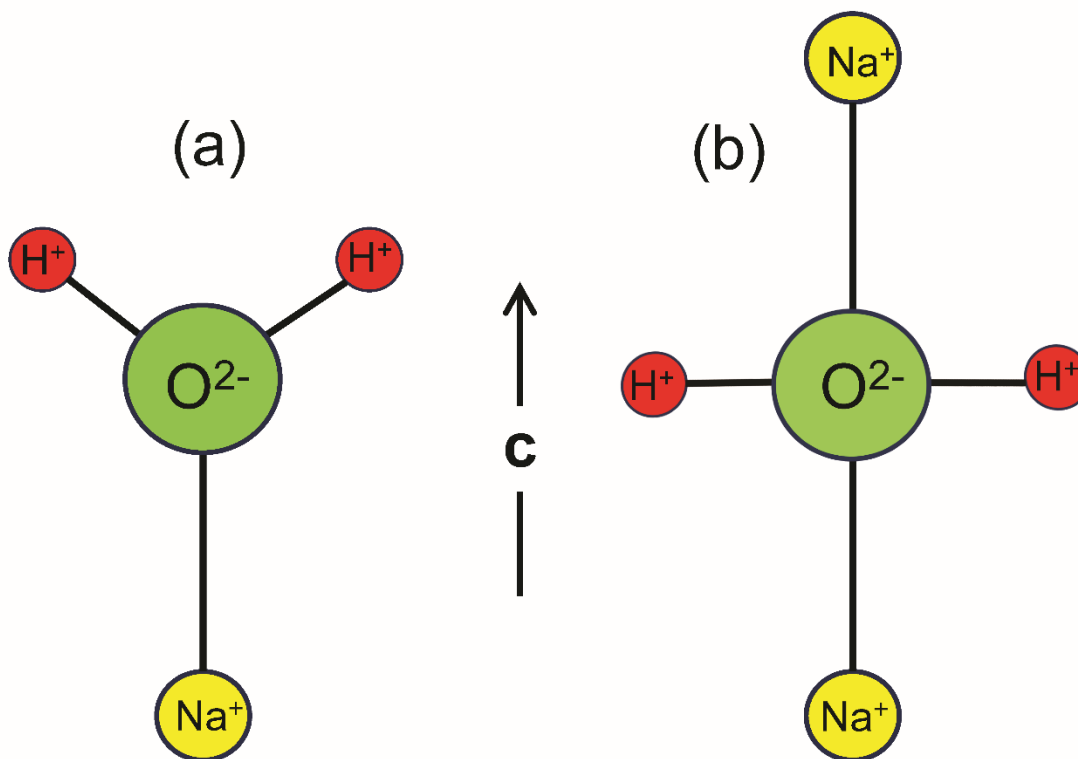
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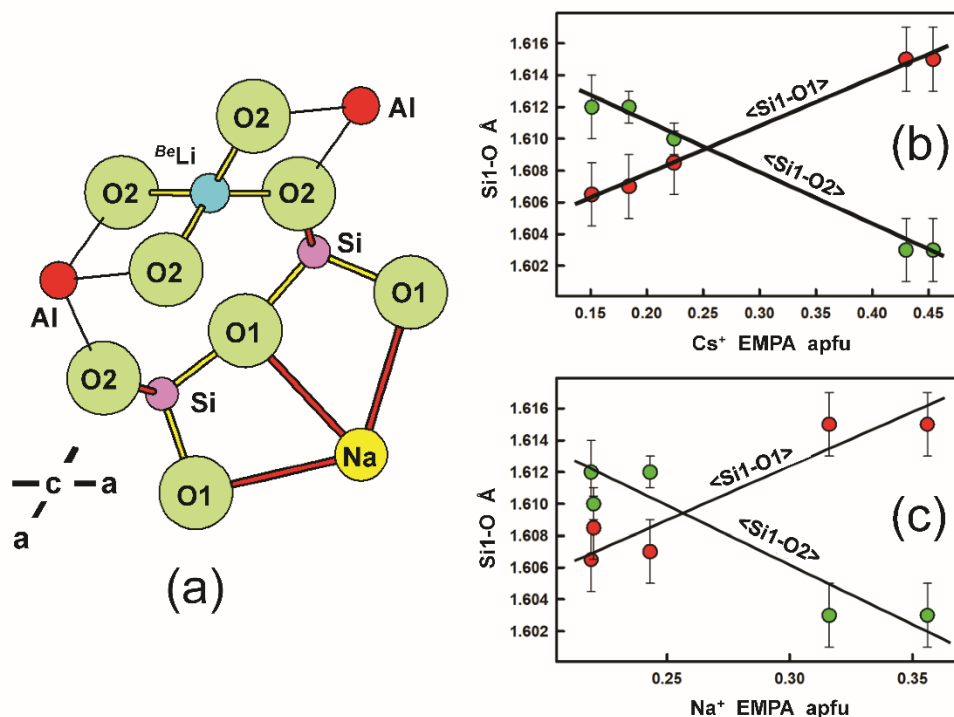


**Fig. 3.** The local environments of the channel cations in beryl: (a) Na<sup>+</sup>, (b), (c) Cs<sup>+</sup>; Na: yellow circle, other colours as in Fig. 1.

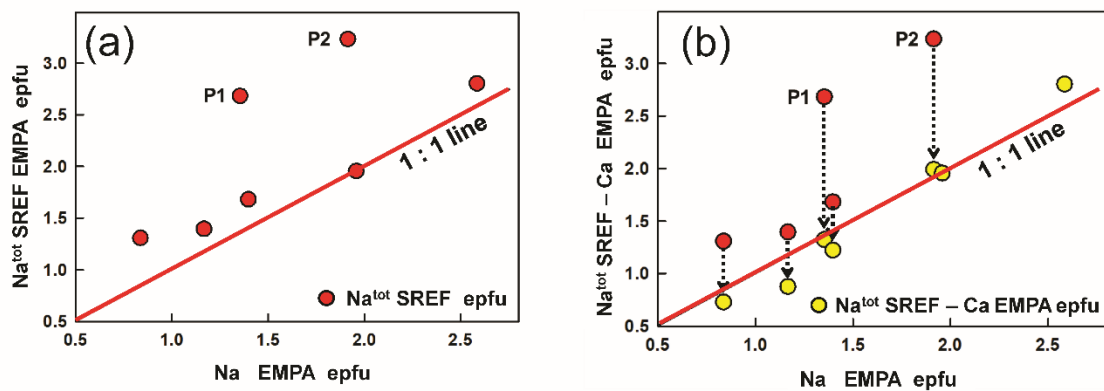
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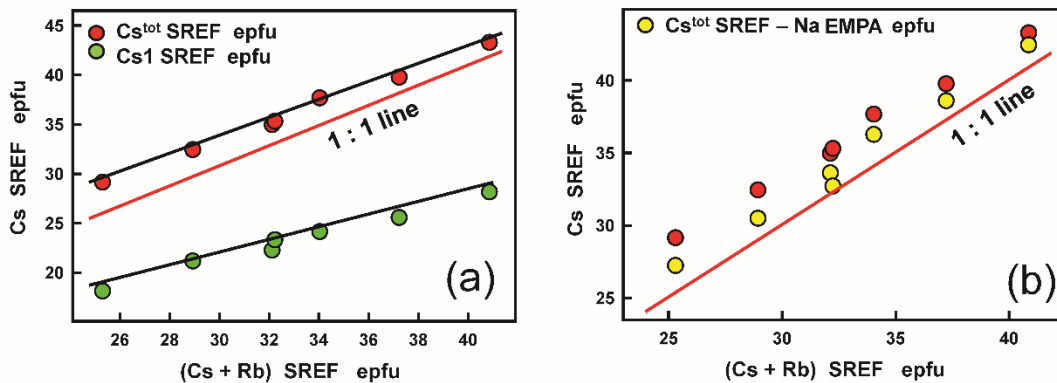
**Fig. 4.** Geometrically possible arrangements of the coordination of channel (H<sub>2</sub>O) by Na<sup>+</sup> ions; (a) bonded to one Na<sup>+</sup> ions with the 2-fold symmetry axis of the (H<sub>2</sub>O) group parallel to the **c**-axis; (b) bonded to two Na<sup>+</sup> ion with the 2-fold symmetry axis of the (H<sub>2</sub>O) group perpendicular to the **c**-axis; yellow circle: Na<sup>+</sup>; green circle: O<sup>2-</sup> ion of the (H<sub>2</sub>O) group; red circle: H<sup>+</sup> ion.



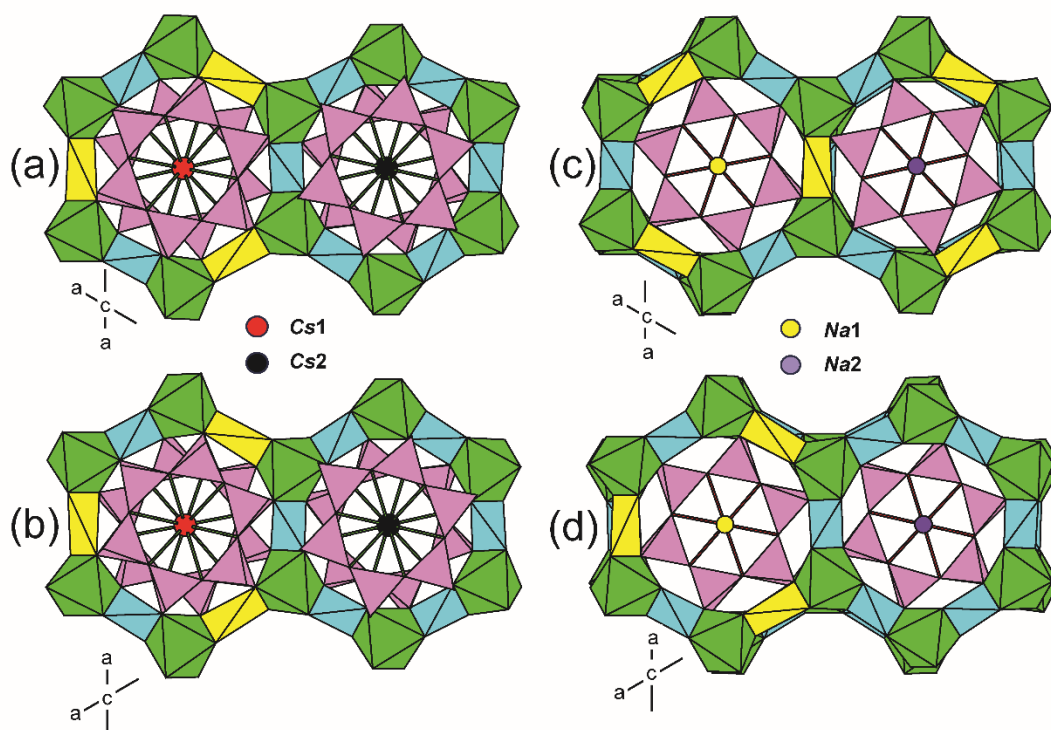
**Fig. 5.** (a) The local atom arrangement around the  $^{Be}Li$  and channel Na in beryl; the yellow bonds between  $^{Be}Li$  and O2 have a lower bond-valence than when the  $Be$  site is occupied by Be; Na in the channel bonds to O1, increasing the strength of the O1–Si bonds (red lines) and decreasing the strength of the Si–O2 bonds (yellow lines), allowing the O2 anion to accord with the valence-sum rule; other chemical bonds are shown by thin black lines; (b),(c) variation in the length of the Si–O1 bonds (red circles) and Si–O2 bonds (green circles) as a function of the amounts of channel alkalis in beryl.



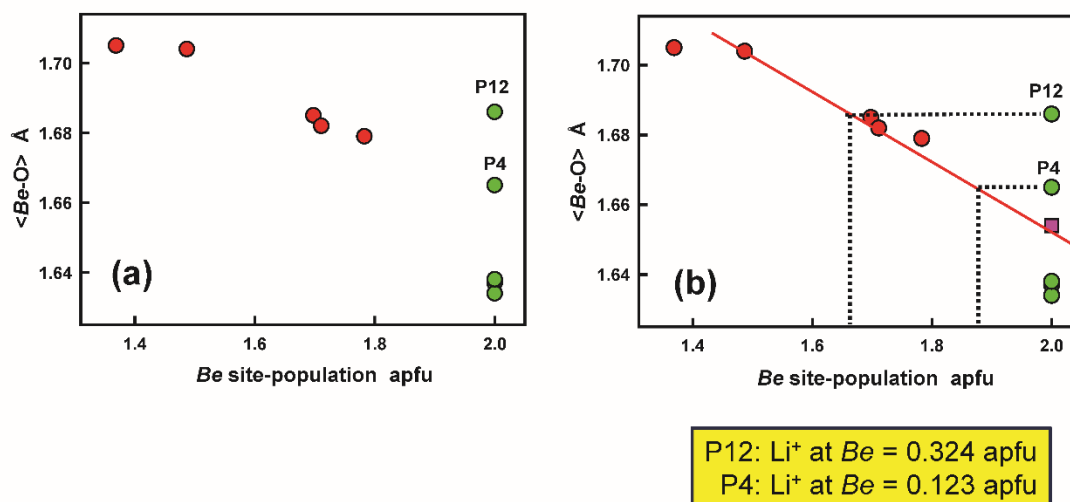
**Fig. 6.** (a) Scattering (in epfu) from the  $\text{Na}1 + \text{Na}2$  sites (red circles) versus the effective scattering from  $\text{Na}^+$  content determined by EMPA; (b) scattering (in epfu) from the  $\text{Na}1 + \text{Na}2$  sites corrected for the  $\text{Ca}^{2+}$  content of the crystal occupying the  $\text{Na}$  sites (yellow circles) versus the effective scattering from  $\text{Na}^+$  content determined by EMPA; the red line is the 1:1 relation.



**Fig. 7.** (a) Scattering (in epfu) from the  $Cs_1 + Cs_2$  sites (red circles) and from the  $Cs_1$  site (green circles) determined by SREF (Site-REFinement) *versus* effective scattering from the  $(Cs^+ + Rb^+)$  content determined by EMPA; (b) red circles: scattering (in epfu) from the  $Cs_1 + Cs_2$  sites determined by SREF; yellow circles: scattering (in epfu) from the  $Cs_1 + Cs_2$  sites minus the scattering from  $(H_2O)$  groups assuming  $Na^+ - O^{2-}$  arrangements for  $Na^+$  determined by EMPA; the black lines are fit 'by eye' to emphasize the linear correlation of the data and the red lines are the 1:1 relation.

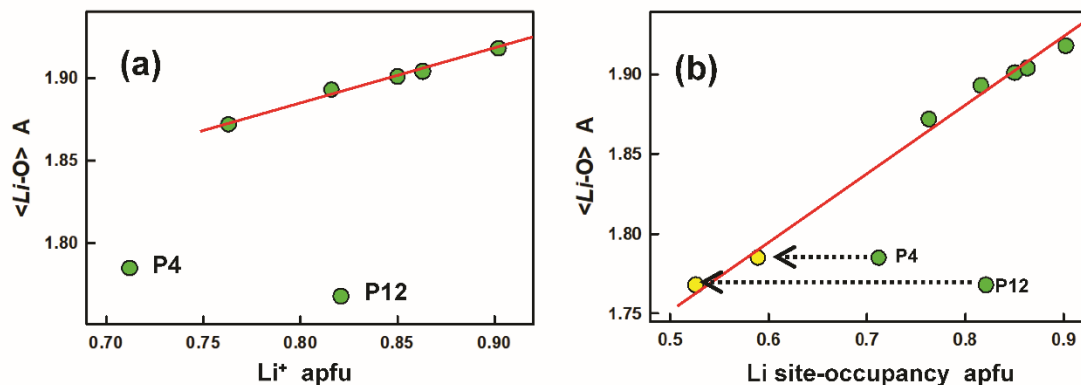


**Fig. 8.** The local environments of the channel cations in pezzottaite: (a,b) Cs<sup>+</sup>; (c,d) Na<sup>+</sup>; colours as indicated on figure, other colours as in Fig. 1. Note the difference in axis orientation between (a) and (b) and between (c) and (d); each pair of diagrams gives views of each arrangement along +**c** and along -**c**.



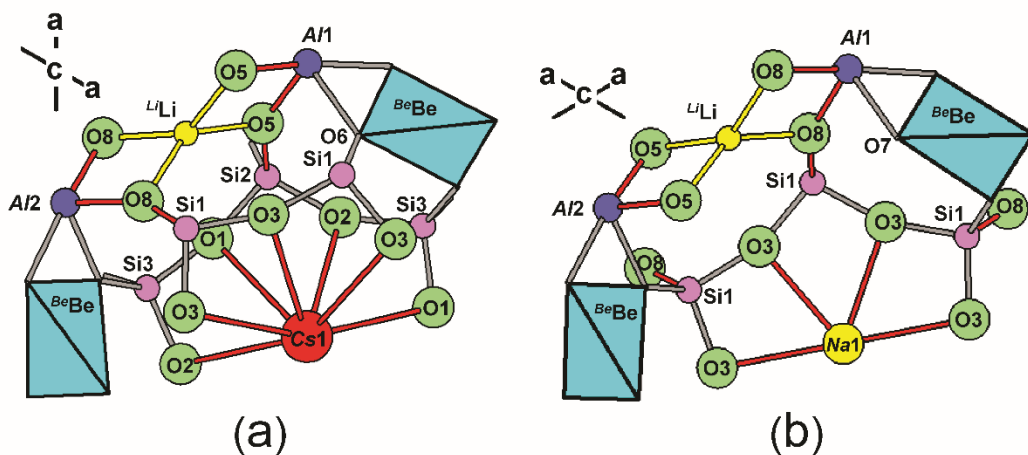
**Fig. 9.** (a)  $\langle Be-O \rangle$  distance as a function of assigned occupancies in beryl (red circles) and pezzottaite (green circles); (b) as in (a) with addition of (1) the relation of Sherriff *et al.* (1991) between  $\langle Be-O \rangle$  distance in beryl crystals as a function of the  $Be^{2+}$  content of the  $Be$  site in apfu, (2) the grand  $\langle Be-O \rangle$  distance in Li-free beryl crystals (pink square) from Gibbs *et al.* (1968) and Morosin (1972). The red line is drawn through the data for beryl and the dotted lines enable calculation of the Li content of the  $Be$  site in the weakly rhombohedral crystals P4 and P12.



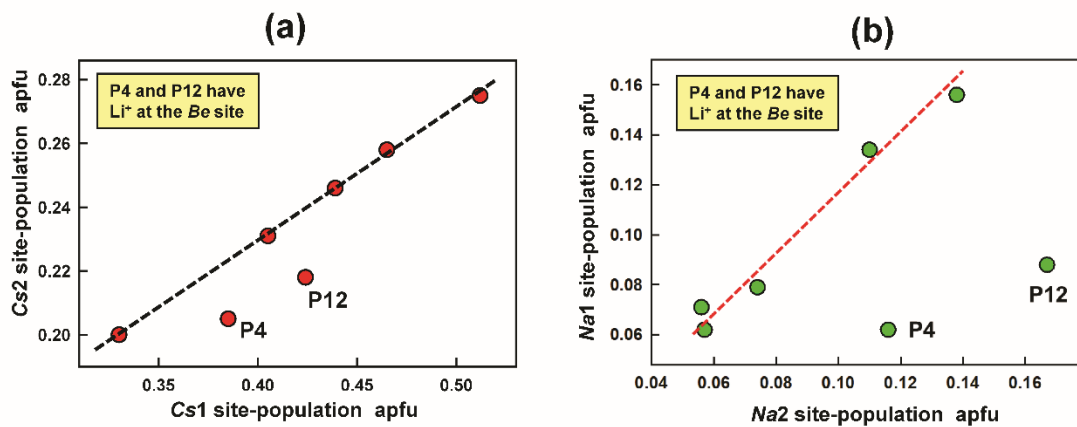


**Fig. 10.** (a)  $\langle Li-O \rangle$  distance as a function of assigned occupancies in pezzottaite (green circles); (b) as in (a) with the addition of (1) the Li content of the *Li* site in the weakly rhombohedral crystals P4 and P12 corrected for the Li occupying the *Be* site (indicated by yellow circles) as calculated from Fig. 5b, and (2) a red line indicating the resulting linear relation between the  $\langle Li-O \rangle$  distance and the re-assigned Li site-populations.

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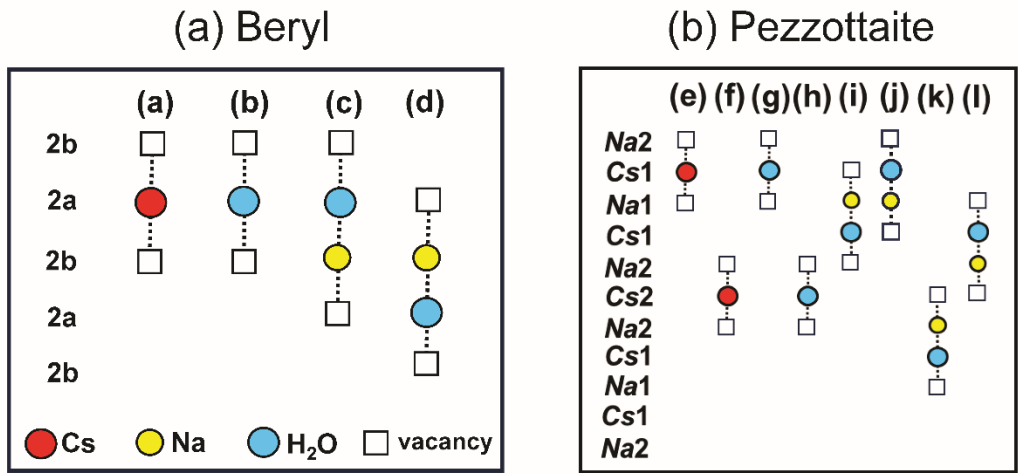


**Fig. 11.** The local atom arrangements around the  ${}^L\text{Li}^+$  and channel  $\text{Cs}^+$  and  $\text{Na}^+$  in pezzottaite; the yellow bonds  ${}^L\text{Li}-\text{O}5$  and  ${}^L\text{Li}-\text{O}8$  have lower bond-valences than where the  $Li$  site is occupied by  $\text{Be}^{2+}$ . (a)  $\text{Cs}^+$  in the channel at  $\text{Cs}1$  bonds to the  $\text{O}1$ ,  $\text{O}2$  and  $\text{O}3$  anions coordinating  $\text{Si}^{4+}$  via the  $\text{Cs}1-\text{O}$  bonds shown in red. The  $\text{O}1$ ,  $\text{O}2$  and  $\text{O}3$  anions therefore require less bond-valence from  $\text{Si}^{4+}$  and these bonds ( $\text{Si}1-\text{O}3$ ,  $\text{Si}1-\text{O}6$ ,  $\text{Si}2-\text{O}1$ ,  $\text{Si}2-\text{O}2$ ,  $\text{Si}3-\text{O}1$  and  $\text{Si}3-\text{O}2$ , shown in grey) weaken (lengthen). To maintain the valence-sum rule at the  $\text{Si}^{4+}$  ions,  $\text{Si}1-\text{O}8$  and  $\text{Si}2-\text{O}5$  (shown in red) increase their bond valence (shorten) which compensates for the occurrence of  $\text{Li}^+$  at the  $Li$  site which is occupied by  $\text{Be}^{2+}$  in  $\text{Cs}$ -free beryl. (b)  $\text{Na}^+$  in the channel at  $\text{Na}1$  bonds to  $\text{O}3$  and the valence-sum rule causes  $\text{O}3-\text{Si}1$  bonds (shown in grey) to decrease in bond valence (lengthen). In turn,  $\text{Si}1-\text{O}8$  increases its bond valence. A similar mechanism increases the bond valence of the  $\text{Si}2-\text{O}5$  bond in an adjacent channel (not shown) to compensate for the occurrence of  $\text{Li}^+$  at the  $Li$  site which is occupied by  $\text{Be}^{2+}$  in  $\text{Cs}$ -free beryl. For the  $Al$  octahedra,  $Al-\text{O}5$  and  $Al-\text{O}8$  bonds are stronger (shorter and shown in red) and other  $Al-\text{O}$  bonds are weaker (slightly longer and shown in grey) where the local  $Li$  site is occupied by  $\text{Li}^+$ .



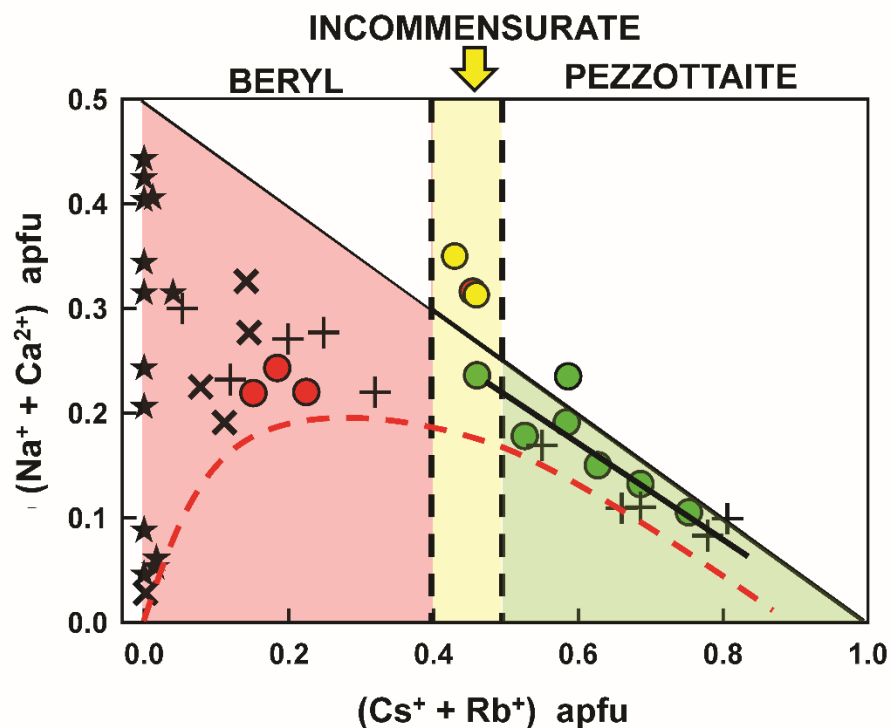
**Fig. 12.** Order of channel cations in pezzottaite; (a) (Cs<sup>+</sup> + Rb<sup>+</sup>) over Cs1 and Cs2; (b) (Na<sup>+</sup> + Ca<sup>2+</sup>) over Na1 and Na2. Note that P4 and P12 deviate from the linear relations shown by the dashed lines as Li<sup>+</sup> is disordered over the *Li* and *Be* sites (unlike the other crystals).

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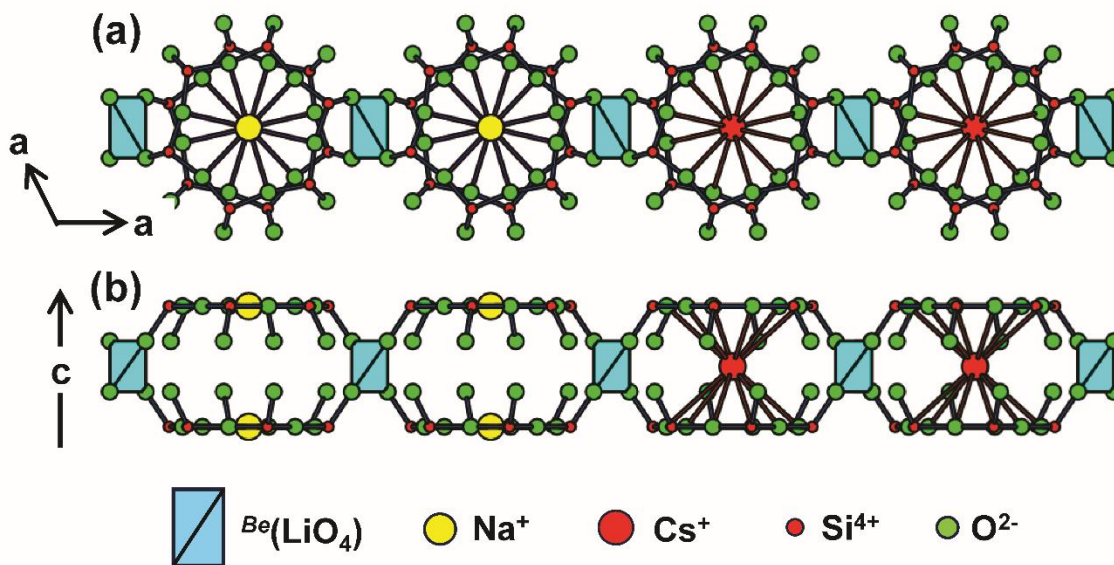


**Fig. 13.** Possible arrangements of channel cations and (H<sub>2</sub>O) groups in (a) beryl, and (b) pezzottaite; red circle: Cs<sup>+</sup>, yellow circle: Na<sup>+</sup>, blue circle: (H<sub>2</sub>O), □: vacancy.

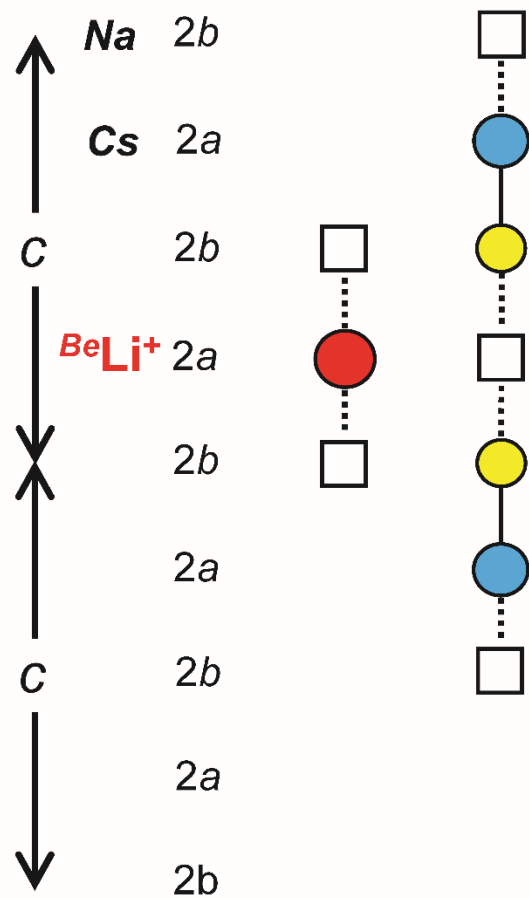
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**Fig. 14.** Variation in  $\text{Na}^+ + \text{Ca}^{2+}$  and  $\text{Cs}^+ + \text{Rb}^+$  (determined by EMPA) across the beryl-pezzottaite join. Data reported here are shown as circles: red circles: beryl; green circles: pezzottaite; yellow circles: incommensurate structures. Literature data are shown as crosses (Hawthorne and Černý, 1977; Sherriff *et al.*, 1991), stars (Aurischio *et al.*, 1998), plus signs (Pieczka *et al.*, 2016). The upper black diagonal line denotes the equation  $(\text{Cs}^+ + \text{Rb}^+) + 2(\text{Na}^+ + \text{Ca}^{2+}) = 1$  apfu; the lower black diagonal line denotes the maximum amount of  $\text{Na}^+ + \text{Ca}^{2+}$  allowed by a combination of channel-cation and  $(\text{H}_2\text{O})$  interactions and the constraint of electroneutrality. The coloured areas denote the presumed stability of the various phases. The curved dashed red line denotes the lower limit of observed chemical compositions.

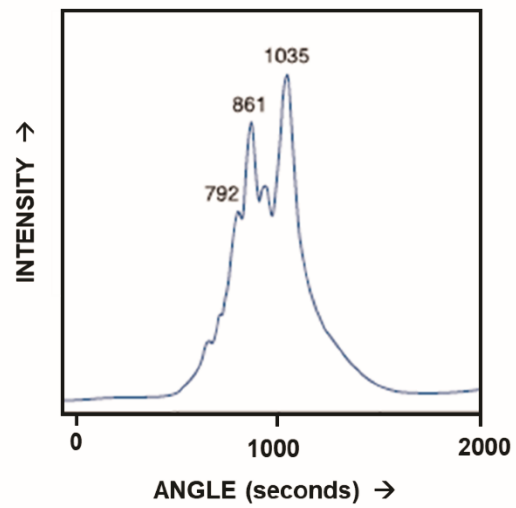


**Fig. 15.** Adjacent channel arrangements in beryl that satisfy the local bond-valence requirements of  $\text{Li}^+$  replacing  $\text{Be}^{2+}$  at the *Be* site, showing how the alkali cations  $\text{Na}^+$  and  $\text{Cs}^+$  give additional bond-valence to the anions of the  $(^{\text{Be}}\text{LiO}_4)$  tetrahedra required by the replacement of  $\text{Be}^{2+}$  by  $\text{Li}^+$ ; four of the six girdling  $(\text{BeO}_4)$  tetrahedra and several of the  $\text{O}^{2-}$  ions linked to  $\text{Si}^{4+}$  are omitted to avoid obscuring the view of the important features of these diagrams; (a) view down *c* showing how the channel cation in one channel provides additional bond-valence to two anions of the  $(^{\text{Be}}\text{LiO}_4)$  tetrahedron *via* the bonds of the  $(\text{SiO}_4)$  tetrahedra (as shown in Fig. 5), and what arrangements are required in adjacent channels to complete the mechanism for the entire  $(^{\text{Be}}\text{LiO}_4)$  tetrahedron; (b) view orthogonal to *c* showing how  $\text{Na}^+$  is required both above and below the level of the  $(\text{SiO}_4)$  tetrahedron to satisfy the bond-valence requirements for two of the anions of the  $(^{\text{Be}}\text{LiO}_4)$  tetrahedron, and how the arrangement in the adjacent channel may be the same (*i.e.* two  $\text{Na}^+$  cations) or may be a single  $\text{Cs}^+$  cation. Legend as in Fig. 13.



**Fig. 16.** Arrangements of  $Cs^+$  and  $Na^+$  in single channels conforming to the mechanisms shown in Fig. 15. Legend as in Fig. 13.

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**Fig. 17.** X-ray rocking curve for the gem-quality pezzottaite showing complex microstructure. Modified from Liu *et al.* (2006).

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**Table 1.** Wykoff positions, point symmetries and general coordinates for the beryl and pezzottaite structures.

	Wykoff position	Point symmetry	Coordinates
<b>Beryl</b>			
<i>Cs</i>	<i>2a</i>	6 2 2	0 0 $\frac{1}{4}$
<i>Na</i>	<i>2b</i>	6/ <i>m</i>	0 0 0
<i>Be</i>	<i>6f</i>	2 2 2	$\frac{1}{2}$ 0 $\frac{1}{4}$
<i>Al</i>	<i>4c</i>	3 2	$\frac{2}{3}$ $\frac{1}{3}$ $\frac{1}{4}$
<i>Si</i>	<i>12l</i>	<i>m</i>	<i>x y</i> 0
O1	<i>12l</i>	<i>m</i>	<i>x y</i> 0
O2	<i>24m</i>	1	<i>x y z</i>
<b>Pezzottaite</b>			
<i>Cs</i> 1	<i>12c</i>	3	0 0 <i>z</i>
<i>Cs</i> 2	<i>6a</i>	–3	0 0 $\frac{1}{4}$
<i>Na</i> 1	<i>6b</i>	–3	0 0 0
<i>Na</i> 2	<i>12c</i>	3	0 0 <i>z</i>
<i>Be</i>	<i>36f</i>	1	<i>x y z</i>
<i>Li</i>	<i>18e</i>	2	<i>x</i> 0 $\frac{1}{4}$
<i>Al</i> 1	<i>18e</i>	2	<i>x</i> 0 $\frac{1}{4}$
<i>Al</i> 2	<i>18e</i>	2	<i>x</i> 0 $\frac{1}{4}$
<i>Si</i> 1	<i>36f</i>	1	<i>x y z</i>
<i>Si</i> 2	<i>36f</i>	1	<i>x y z</i>
<i>Si</i> 3	<i>36f</i>	1	<i>x y z</i>
O(1–9)	<i>36f</i>	1	<i>x y z</i>

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**Table 2.** Miscellaneous data for beryl-pezzottaite pertaining to data collection and structure refinement.

Sample	Symmetry*	Crystal size (mm)	<i>a</i>	<i>c</i>	<i>V</i>	<i>Z</i>	Source†
P1	R	0.12 sphere	15.9619(3)	27.8325(6)	6141.2(4)	18	F.P.
P2	R	0.14 sphere	15.9662(4)	27.8147(7)	6140.6(5)	18	F.P.
P3	H	0.11 sphere	9.2239(3)	9.2330(3)	680.30(7)	2	B.L.
P4	R(w)	0.04 x 0.14 x 0.14	15.9687(3)	27.8112(6)	6141.7(4)	18	P.F.D.
P5	R	0.04 x 0.13 x 0.14	15.9651(4)	27.8237(7)	6141.7(5)	18	P.F.D.
P6	R	0.10 sphere	15.9659(3)	27.8485(6)	6147.8(4)	18	F.P.
P7	R	0.14 sphere	15.9628(4)	27.8447(7)	6144.6(5)	18	F.P.
P8	H	0.12 x 0.12 x 0.16	9.2176(3)	9.2414(3)	679.99(6)	2	F.P.
P9	I	0.15 sphere	9.2188(3)**	9.2753(3)**	682.67(6)**	–	H.O.
P10	H	0.13 sphere	9.2187(3)	9.2785(3)	682.89(7)	2	H.O.
P11	H	0.17 sphere	9.2200(3)	9.2769(3)	682.96(6)	2	H.O.
P12	R(w)	0.17 sphere	15.9673(4)	27.8579(7)	6150.9(5)	18	H.O.
P13	I	0.16 sphere	–	–	–	–	H.O.
P14	H	0.16 sphere	9.2170(3)	9.2391(3)	679.73(6)	2	H.O.

\* R = rhombohedral, R(w) = weak rhombohedral, H = hexagonal, I = incommensurate;

\*\* ignoring  $hk\ell/2$  reflections;

† F.P. = Federico Pezzotta, B.L. = Brendan Laurs, P.F.D. = purchased from dealer, H.O. = Herbert Obodda

**Table 3.** Details of data collection and refinement for beryl structures.

	P3	P8	P10	P11	P14
Absorption coefficient ( $\text{mm}^{-1}$ )	1.72	1.71	2.18	2.23	1.60
$F(000)$	569.4	572.0	593.5	595.2	568.3
$D_{\text{calc.}}$ ( $\text{g/cm}^3$ )	2.839	2.858	2.970	2.981	2.836
Total number of reflections	5382	6657	5440	6667	6066
Number of unique reflections	356	356	358	358	356
Number of unique $ F  > 4\sigma F$	356	356	356	358	356
$R_{\text{int}}$ (%)	1.56	1.67	1.55	2.00	1.67
$R_{\text{obs}}$ (%)	2.91	2.36	2.65	2.63	2.47
$R_{\text{all}}$ (%)	2.91	2.36	2.67	2.63	2.47
Goodness of fit on $F^2$	1.562	1.267	1.241	1.227	1.250

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**Table 4.** Atom positions and displacement parameters ( $\text{\AA}^2$ ) for crystals of the beryl-pezzottaite series with space-group symmetry  $P6/mcc$ .

Site	x	y	z	$U^{11}$	$U^{22}$	$U^{33}$	$U^{23}$	$U^{13}$	$U^{12}$	$U_{eq}$
<b>P3</b>										
Cs	0	0	$\frac{1}{4}$	0.0388(12)	0.0388(12)	0.0353(15)	0	0	0.0194(6)	0.0376(9)
Na	0	0	0	0.021(5)	0.021(5)	0.038(8)	0	0	0.011(3)	0.027(5)
Si	0.38906(10)	0.11890(9)	0	0.0061(4)	0.0059(4)	0.0062(4)	0	0	0.0033(3)	0.0059(3)
Al	$\frac{2}{3}$	$\frac{1}{3}$	$\frac{1}{4}$	0.0096(4)	0.0094(4)	0.0093(6)	0	0	0.0048(2)	0.0095(3)
Be	$\frac{1}{2}$	0	$\frac{1}{4}$	0.0098(16)	0.0061(20)	0.0081(19)	0	0	0.0030(10)	0.0084(9)
O1	0.3043(3)	0.2346(3)	0	0.0138(11)	0.0099(10)	0.0224(11)	0	0	0.0087(9)	0.0142(5)
O2	0.49794(19)	0.1472(2)	0.14468(18)	0.0151(7)	0.0160(7)	0.0125(7)	-0.0055(6)	-0.0069(6)	0.0101(6)	0.0135(4)
<b>P8</b>										
Cs	0	0	$\frac{1}{4}$	0.0359(7)	0.0359(7)	0.0326(8)	0	0	0.0180(3)	0.0350(5)
Na	0	0	0	0.021(4)	0.021(4)	0.044(7)	0	0	0.010(2)	0.029(4)
Si	0.38975(7)	0.11991(7)	0	0.0069(3)	0.0067(3)	0.0072(3)	0	0	0.0036(2)	0.0068(2)
Al	$\frac{2}{3}$	$\frac{1}{3}$	$\frac{1}{4}$	0.0071(3)	0.0071(3)	0.0069(5)	0	0	0.0036(2)	0.0070(3)
Be	$\frac{1}{2}$	0	$\frac{1}{4}$	0.0116(12)	0.0085(16)	0.0106(15)	0	0	0.0042(8)	0.0106(7)
O1	0.3035(2)	0.2345(2)	0	0.0148(8)	0.0115(8)	0.0245(9)	0	0	0.0097(7)	0.0160(4)
O2	0.49819(16)	0.14823(16)	0.14454(14)	0.0174(6)	0.0185(6)	0.0141(4)	-0.0069(5)	-0.0080(4)	0.0118(5)	0.0155(3)
<b>P10</b>										
Cs	0	0	$\frac{1}{4}$	0.0354(5)	0.0354(5)	0.0247(5)	0	0	0.0177(2)	0.0319(4)
Na	0	0	0	0.017(3)	0.017(3)	0.047(6)	0	0	0.0085(15)	0.027(3)
Si	0.39090(9)	0.12207(9)	0	0.0077(3)	0.0077(3)	0.0077(3)	0	0	0.0041(3)	0.0076(2)
Al	$\frac{2}{3}$	$\frac{1}{3}$	$\frac{1}{4}$	0.0083(4)	0.0083(4)	0.0062(5)	0	0	0.0042(2)	0.0076(3)
Be	$\frac{1}{2}$	0	$\frac{1}{4}$	0.0120(15)	0.009(2)	0.012(2)	0	0	0.0047(10)	0.0113(9)
O1	0.3010(3)	0.2341(3)	0	0.0152(10)	0.0123(9)	0.0315(12)	0	0	0.0100(8)	0.0182(5)
O2	0.4979(2)	0.1500(2)	0.14397(17)	0.0239(7)	0.0256(8)	0.0169(6)	-0.0111(6)	-0.0118(6)	0.0170(6)	0.0200(4)

**Table 4.** continued

Site	x	y	z	$U^{11}$	$U^{22}$	$U^{33}$	$U^{23}$	$U^{13}$	$U^{12}$	$U_{eq}$
<b>P11</b>										
Cs	0	0	¼	0.0343(4)	0.0343(4)	0.0250(5)	0	0	0.0171(2)	0.0312(4)
Na	0	0	0	0.018(3)	0.018(3)	0.048(6)	0	0	0.0087(16)	0.028(3)
Si	0.39086(8)	0.12208(8)	0	0.0074(3)	0.0074(3)	0.0085(3)	0	0	0.0040(3)	0.0076(2)
Al	2/3	1/3	¼	0.0080(5)	0.0080(5)	0.0065(6)	0	0	0.0040(2)	0.0075(4)
Be	½	0	¼	0.0130(15)	0.0102(19)	0.0118(18)	0	0	0.0052(10)	0.0120(8)
O1	0.3009(3)	0.2341(3)	0	0.0152(9)	0.0125(9)	0.0328(11)	0	0	0.0104(8)	0.0187(5)
O2	0.49779(19)	0.1499(2)	0.1441(2)	0.0237(7)	0.0261(8)	0.0172(7)	-0.0112(6)	-0.0120(6)	0.0172(6)	0.0202(4)
<b>P14</b>										
Cs	0	0	¼	0.0382(8)	0.0382(8)	0.0335(9)	0	0	0.0191(4)	0.0366(6)
Na	0	0	0	0.023(3)	0.023(3)	0.044(6)	0	0	0.0117(17)	0.030(3)
Si	0.38950(7)	0.11951(7)	0	0.0073(3)	0.0072(3)	0.0075(3)	0	0	0.0038(2)	0.0073(2)
Al	2/3	1/3	¼	0.0077(3)	0.0077(3)	0.0072(5)	0	0	0.0039(2)	0.0075(3)
Be	½	0	¼	0.0122(12)	0.0094(15)	0.0107(14)	0	0	0.0047(7)	0.0110(7)
O1	0.3042(2)	0.2346(2)	0	0.0156(8)	0.0118(7)	0.0239(9)	0	0	0.0102(6)	0.0156(4)
O2	0.49833(14)	0.14797(16)	0.14463(14)	0.0168(6)	0.0185(6)	0.0139(5)	-0.0062(4)	-0.0073(4)	0.0114(4)	0.0152(3)

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**Table 5.** Selected interatomic distances (Å) for crystals of the beryl-pezzottaite series with space-group symmetry *P6/mcc*.

<b>P3</b>			<b>P8</b>			<b>P10</b>		
Si-O1		1.607(2)	Si-O1		1.608(2)	Si-O1		1.616(2)
Si-O1a		1.606(2)	Si-O1a		1.609(2)	Si-O1a		1.614(2)
Si-O2	x2	<u>1.612(2)</u>	Si-O2	x2	<u>1.610(1)</u>	Si-O2	x2	<u>1.603(2)</u>
<Si-O>		1.609	<Si-O>		1.609	<Si-O>		1.609
Al-O2	x6	1.909(2)	Al-O2	x6	1.903(1)	Al-O2	x6	1.902(2)
Be/Li-O2	x4	1.679(2)	Be/Li-O2	x4	1.685(1)	Be/Li-O2	x4	1.705(2)
Cs-O1	x12	3.437(2)	Cs-O1	x12	3.434(1)	Cs-O1	x12	3.427(2)
Na-O1	x6	2.547(2)	Na-O1	x6	2.540(2)	Na-O1	x6	2.524(2)
2a-2b	x2	2.308(0)	2a-2b	x2	2.310(0)	2a-2b	x2	2.320(0)
<b>P11</b>			<b>P14</b>					
Si-O1		1.615(2)	Si-O1		1.605(2)			
Si-O1a		1.615(2)	Si-O1a		1.609(2)			
Si-O2	x2	<u>1.603(2)</u>	Si-O2	x2	<u>1.612(1)</u>			
<Si-O>		1.609	<Si-O>		1.610			
Al-O2	x6	1.902(2)	Al-O2	x6	1.904(1)			
Be/Li-O2	x4	1.704(2)	Be/Li-O2	x4	1.682(1)			
Cs-O1	x12	3.427(2)	Cs-O1	x12	3.437(1)			
Na-O1	x6	2.523(2)	Na-O1	x6	2.545(2)			
2a-2b	x2	2.320(0)	2a-2b	x2	2.310(0)			

Equivalent positions: a:  $y$ ,  $-x+z$ ,  $-z$ .

**Table 6.** Refined site-populations (apfu) for beryl structures.

Site	Wyk.	P3	P8	P10	P11	P14
Cs	2a	0.246(3)	0.319(3)	0.501(3)	0.521(3)	0.278(3)
Na	2b	0.27(2)	0.266(13)	0.323(3)	0.338(14)	0.298(14)

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**Table 7.** Bond-valence\* table for beryl P10.

	<i>Na</i>	<i>Cs</i>	<i>Be</i>	<i>Al</i>	<i>Si</i>	$\Sigma$
O1	0.045 <sup>x6↓</sup>	0.032 <sup>x12↓</sup>			1.021 1.026	2.160
O2			0.388 <sup>x4↓</sup>	0.503 <sup>x6↓</sup>	1.055 <sup>x2↓</sup>	1.946
$\Sigma$	0.269**	0.384	1.552	3.018	4.157	

\*Bond-valence parameters from Gagné and Hawthorne (2015); note that the bond valences are long range and are weighted by the site populations;

\*\*omitting bonds to (H<sub>2</sub>O).

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**Table 8.** Details of data collection and refinement for pezzottaite structures.

	P1	P2	P4	P5	P6	P7	P12
Absorption coefficient ( $\text{mm}^{-1}$ )	2.55	2.26	2.41	2.66	2.92	2.76	2.55
$F(000)$	5457.5	5357.7	5395.1	5480.9	5573.8	5513.5	5460.1
$D_{\text{calc.}}$ ( $\text{g/cm}^3$ )	3.051	2.985	3.011	3.067	3.126	3.088	3.047
No. of reflections to calculate cell dimensions	7354	6548	6261	6256	6431	5684	5744
Number of unique reflections	2004	2007	2005	2003	2005	2001	2005
Number of $ F  > 4\sigma F$	1907	1885	1730	1836	1860	1887	1658
$R_{\text{merge}}$ (%)							
$R_{\text{obs}}$ (%)	3.82	3.59	5.99	3.93	3.74	3.31	5.83
$R_{\text{all}}$ (%)	4.01	3.79	6.53	4.26	4.09	3.49	6.44
Goodness of fit on $F^2$	1.265	1.159	1.185	1.262	1.283	1.168	1.198

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**Table 9.** Atom positions and displacement parameters ( $\text{\AA}^2$ ) for crystals of the beryl-pezzottaite series with space-group symmetry  $R\bar{3}c$ .

Site	X	y	z	$U^{11}$	$U^{22}$	$U^{33}$	$U^{23}$	$U^{13}$	$U^{12}$	$U_{eq}$		
				<b>P1</b>								
Cs1	0	0	0.08186(2)	0.0253(3)	0.0253(3)	0.0203(3)	0	0	0.01263(13)	0.0236(2)		
Cs2	0	0	¼	0.0375(4)	0.0375(4)	0.0229(4)	0	0	0.01876(18)	0.0326(3)		
Na1	0	0	0	0.0021(15)								
Na2	0	0	0.1629(5)	0.014(5)	0.014(5)	0.038(9)	0	0	0.007(2)	0.022(4)		
Li	0.5033(5)	0	¼	0.0142(12)								
Be	0.3282(2)	0.1623(3)	0.24915(10)	0.0077(6)								
Si1	0.04448(5)	0.21956(4)	-0.00122(3)	0.0045(3)	0.0044(3)	0.0051(3)	0.0004(3)	0.0007(3)	0.0021(2)	0.00475(18)		
Si2	0.44655(4)	0.16366(4)	-0.00035(3)	0.0050(3)	0.0040(3)	0.0051(3)	0.0001(3)	0.0001(3)	0.0026(2)	0.00456(18)		
Si3	0.61570(5)	0.11348(4)	-0.00149(3)	0.0034(3)	0.0045(3)	0.0049(3)	-0.0001(3)	0.0003(3)	0.0019(2)	0.00430(18)		
Al1	0.33276(6)	0	¼	0.0052(4)	0.0052(5)	0.0030(5)	-0.0001(3)	-0.00006(15)	0.0026(3)	0.0045(3)		
Al2	0.67320(8)	0	¼	0.0042(4)	0.0041(5)	0.0077(6)	-0.0003(3)	-0.00017(16)	0.0021(3)	0.0053(3)		
O1	0.48331(13)	0.27776(13)	0.99286(8)	0.0104(8)	0.0056(8)	0.0138(10)	0.0004(7)	0.0016(7)	0.0050(7)	0.0095(4)		
O2	0.54623(13)	0.16029(13)	0.99909(8)	0.0090(8)	0.0104(8)	0.0117(8)	0.0005(7)	-0.0006(7)	0.0073(7)	0.0093(4)		
O3	0.11949(13)	0.17871(13)	0.00569(8)	0.0093(8)	0.0104(8)	0.0099(9)	0.0005(7)	-0.0018(7)	0.0072(7)	0.0089(4)		
O4	0.39045(14)	0.26899(13)	0.11771(6)	0.0097(9)	0.0047(8)	0.0038(7)	-0.0015(6)	-0.0022(6)	0.0045(7)	0.0057(4)		
O5	0.27273(14)	0.37624(14)	0.04332(7)	0.0099(9)	0.0077(9)	0.0101(8)	0.0035(7)	-0.0026(7)	0.0042(7)	0.0093(4)		
O6	0.28103(13)	0.21030(13)	0.05121(7)	0.0078(8)	0.0060(8)	0.0046(8)	-0.0003(6)	-0.0040(6)	0.0052(7)	0.0054(4)		
O7	0.04343(14)	0.45245(13)	0.04720(7)	0.0084(9)	0.0078(8)	0.0070(8)	0.0011(6)	0.0017(6)	0.0042(7)	0.0077(4)		
O8	0.04987(15)	0.28224(13)	0.04406(7)	0.0086(9)	0.0081(8)	0.0085(8)	-0.0023(6)	0.0002(7)	0.0031(7)	0.0089(4)		
O9	0.39514(14)	0.13070(15)	0.05134(7)	0.0064(8)	0.0076(9)	0.0085(8)	0.0026(7)	0.0029(6)	0.0033(7)	0.0076(4)		

**Table 9.** continued

Site	x	y	z	$U^{11}$	$U^{22}$	$U^{\beta 3}$	$U^{\beta 3}$	$U^{13}$	$U^{12}$	$U_{eq}$	
					<b>P2</b>						
Cs1	0	0	0.08199(2)	0.0273(3)	0.0273(3)	0.0220(4)	0	0	0.01364(15)	0.0255(3)	
Cs2	0	0	¼	0.0372(4)	0.0372(4)	0.0238(4)	0	0	0.01862(18)	0.0328(3)	
Na1	0	0	0	0.0059(13)							
Na2	0	0	0.1636(3)	0.024(4)	0.024(4)	0.029(6)	0	0	0.012(2)	0.026(3)	
Li	0.5029(4)	0	¼	0.0150(10)							
Be	0.32878(18)	0.1630(3)	0.24922(9)	0.0088(5)							
Si1	0.04543(5)	0.21962(4)	−0.00096(2)	0.0057(3)	0.0053(3)	0.0057(3)	0.0003(2)	0.0011(2)	0.0026(2)	0.00565(17)	
Si2	0.44658(4)	0.16372(4)	−0.00016(2)	0.0058(3)	0.0048(3)	0.0054(3)	−0.0001(2)	0.0000(2)	0.0029(2)	0.00520(17)	
Si3	0.61576(4)	0.11354(4)	−0.00134(2)	0.0045(3)	0.0054(3)	0.0052(3)	−0.0001(2)	0.0000(2)	0.0026(2)	0.00499(17)	
Al1	0.33287(5)	0	¼	0.0055(4)	0.0057(4)	0.0053(5)	0.0000(3)	0.00001(13)	0.0028(2)	0.0055(3)	
Al2	0.67233(7)	0	¼	0.0066(4)	0.0059(4)	0.0052(5)	−0.0003(3)	−0.00014(13)	0.0029(2)	0.0060(3)	
O1	0.48404(12)	0.27798(11)	0.99379(7)	0.0127(7)	0.0063(7)	0.0160(8)	0.0011(6)	0.0025(6)	0.0057(6)	0.0112(3)	
O2	0.54556(11)	0.15938(12)	0.99945(6)	0.0103(7)	0.0120(7)	0.0140(8)	0.0007(6)	−0.0001(6)	0.0085(6)	0.0108(3)	
O3	0.12013(12)	0.17854(12)	0.00481(7)	0.0106(7)	0.0114(7)	0.0148(8)	0.0004(6)	−0.0026(6)	0.0077(6)	0.0112(3)	
O4	0.38932(12)	0.26821(12)	0.11779(6)	0.0109(7)	0.0057(7)	0.0065(7)	−0.0005(5)	−0.0020(5)	0.0047(6)	0.0075(3)	
O5	0.27166(13)	0.37698(13)	0.04391(7)	0.0121(8)	0.0096(8)	0.0136(8)	0.0045(6)	−0.0050(6)	0.0029(6)	0.0129(4)	
O6	0.28149(11)	0.21077(11)	0.05088(6)	0.0085(7)	0.0074(7)	0.0071(7)	−0.0018(5)	−0.0035(5)	0.0056(6)	0.0070(3)	
O7	0.04444(13)	0.45255(11)	0.04741(6)	0.0112(8)	0.0088(7)	0.0085(7)	0.0013(5)	0.0020(6)	0.0054(6)	0.0093(3)	
O8	0.05219(16)	0.28234(12)	0.04454(7)	0.0164(9)	0.0104(8)	0.0109(8)	−0.0023(6)	0.0038(6)	0.0041(7)	0.0137(4)	
O9	0.39379(13)	0.12929(14)	0.05102(6)	0.0109(7)	0.0108(8)	0.0101(7)	0.0033(6)	0.0039(6)	0.0071(6)	0.0099(4)	

**Table 9.** continued

Site	$x$	$y$	$z$	$U^{11}$	$U^{22}$	$U^{33}$	$U^{23}$	$U^{13}$	$U^{12}$	$U_{eq}$	
					<b>P4</b>						
Cs1	0	0	0.08248(4)	0.0282(4)	0.0282(4)	0.0224(5)	0	0	0.01408(19)	0.0263(3)	
Cs2	0	0	¼	0.0354(6)	0.0354(6)	0.0254(7)	0	0	0.0177(3)	0.0321(5)	
Na1	0	0	0	0.001(5)							
Na2	0	0	0.1654(10)	0.017(7)	0.015(7)	0.067(17)	0	0	0.008(3)	0.033(7)	
Li	0.5001(7)	0	¼	0.078(15)							
Be	0.3307(4)	0.1639(5)	0.2495(2)	0.0126(9)							
Si1	0.04690(8)	0.21964(7)	-0.00032(4)	0.0069(5)	0.0054(5)	0.0067(5)	0.0005(5)	-0.0011(5)	0.0027(4)	0.0065(3)	
Si2	0.44671(7)	0.16335(7)	0.00018(4)	0.0055(5)	0.0048(5)	0.0069(5)	-0.0027(4)	0.0011(5)	0.0026(4)	0.0057(2)	
Si3	0.61644(8)	0.11346(7)	-0.00113(4)	0.0040(5)	0.0064(5)	0.0061(5)	-0.0007(5)	-0.0025(4)	0.0024(4)	0.0056(3)	
Al1	0.33316(11)	0	¼	0.0087(8)	0.0077(9)	0.0053(8)	0.0006(6)	0.0003(3)	0.0038(5)	0.0073(5)	
Al2	0.66980(12)	0	¼	0.0063(7)	0.0033(9)	0.0062(8)	-0.0010(6)	-0.0005(3)	0.0016(4)	0.0056(4)	
O1	0.4857(2)	0.2778(2)	0.99688(16)	0.0138(15)	0.0052(13)	0.0342(19)	0.0031(16)	0.0037(16)	0.0062(12)	0.0171(7)	
O2	0.5444(2)	0.1572(2)	0.99948(13)	0.0124(14)	0.0142(14)	0.0189(15)	0.0021(15)	0.0042(16)	0.0097(12)	0.0138(6)	
O3	0.1217(2)	0.1790(2)	0.00300(15)	0.0116(14)	0.0136(15)	0.0249(17)	0.0047(15)	0.0032(16)	0.0087(12)	0.0157(7)	
O4	0.3873(3)	0.2682(3)	0.11799(12)	0.014(2)	0.021(2)	0.0077(14)	0.0042(13)	-0.0064(12)	0.0066(16)	0.0153(8)	
O5	0.2702(3)	0.3803(3)	0.04605(14)	0.025(2)	0.012(2)	0.0216(18)	0.0099(13)	-0.0122(15)	0.0029(16)	0.0223(10)	
O6	0.2822(2)	0.2139(3)	0.04995(12)	0.0092(18)	0.023(2)	0.0101(15)	-0.0113(13)	-0.0066(11)	0.0065(18)	0.0146(8)	
O7	0.0480(3)	0.4525(2)	0.04759(12)	0.017(2)	0.0116(18)	0.0116(15)	0.0020(12)	0.0026(12)	0.0108(18)	0.0119(8)	
O8	0.0601(3)	0.2821(2)	0.04617(13)	0.019(2)	0.010(2)	0.0159(16)	-0.0041(12)	0.0081(14)	-0.0011(15)	0.0190(9)	
O9	0.3898(3)	0.1246(3)	0.04946(12)	0.0164(19)	0.0141(18)	0.0155(15)	0.0088(12)	0.0079(12)	0.0135(17)	0.0128(8)	

**Table 9.** continued

Site	x	y	z	$U^{11}$	$U^{22}$	$U^{\beta 3}$	$U^{\rho 3}$	$U^{13}$	$U^{12}$	$U_{eq}$
<b>P5</b>										
Cs1	0	0	0.08187(2)	0.0258(3)	0.0258(3)	0.0204(3)	0	0	0.01291(13)	0.0240(2)
Cs2	0	0	¼	0.0373(4)	0.0373(4)	0.0228(4)	0	0	0.01866(18)	0.0325(3)
Na1	0	0	0	0.003(3)						
Na2	0	0	0.1633(6)	0.006(6)	0.006(6)	0.025(11)	0	0	0.003(3)	0.012(6)
Li	0.5032(5)	0	¼	0.013(1)						
Be	0.3283(2)	0.1625(3)	0.24923(11)	0.0078(6)						
Si1	0.04472(6)	0.21944(5)	-0.00092(3)	0.0044(3)	0.0046(3)	0.0048(3)	0.0012(3)	0.0003(3)	0.0022(2)	0.00462(19)
Si2	0.44658(5)	0.16363(5)	-0.00011(3)	0.0048(3)	0.0039(3)	0.0051(3)	-0.0020(3)	-0.0009(3)	0.0025(2)	0.00444(19)
Si3	0.61581(5)	0.11344(5)	-0.00159(3)	0.0033(3)	0.0046(3)	0.0039(3)	0.0008(3)	-0.0007(3)	0.0019(2)	0.00398(19)
Al1	0.33286(6)	0	¼	0.0054(5)	0.0056(6)	0.0042(6)	-0.0001(3)	-0.00003(16)	0.0028(3)	0.0051(3)
Al2	0.67277(8)	0	¼	0.0039(5)	0.0035(6)	0.0054(6)	-0.0004(3)	-0.00018(16)	0.0018(3)	0.0043(3)
O1	0.48365(14)	0.27771(13)	0.99316(8)	0.0112(8)	0.0052(8)	0.0125(10)	0.0012(7)	0.0018(7)	0.0049(7)	0.0093(4)
O2	0.54617(13)	0.16012(14)	0.99938(8)	0.0091(8)	0.0116(8)	0.0115(9)	-0.0008(8)	0.0004(9)	0.0080(7)	0.0095(4)
O3	0.11990(14)	0.17885(14)	0.00535(8)	0.0080(8)	0.0109(8)	0.0133(10)	0.0007(8)	-0.0007(8)	0.0070(7)	0.0098(4)
O4	0.39010(14)	0.26896(14)	0.11764(7)	0.0098(9)	0.0054(8)	0.0039(8)	-0.0017(6)	-0.0038(7)	0.0046(8)	0.0060(4)
O5	0.27270(16)	0.37672(15)	0.04360(8)	0.0105(9)	0.0068(9)	0.0103(9)	0.0053(7)	-0.0019(7)	0.0037(8)	0.0095(4)
O6	0.28112(13)	0.21070(14)	0.05112(7)	0.0064(9)	0.0068(9)	0.0043(8)	-0.0018(6)	-0.0052(6)	0.0042(7)	0.0054(4)
O7	0.04382(15)	0.45259(14)	0.04726(7)	0.0108(10)	0.0078(9)	0.0068(8)	0.0008(7)	0.0011(7)	0.0055(8)	0.0081(4)
O8	0.05050(17)	0.28212(14)	0.04424(7)	0.0110(10)	0.0086(9)	0.0085(9)	-0.0013(7)	0.0017(7)	0.0033(8)	0.0101(5)
O9	0.39492(15)	0.13038(16)	0.05122(7)	0.0080(9)	0.0083(10)	0.0085(8)	0.0031(7)	0.0028(7)	0.0046(7)	0.0080(4)

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**Table 9.** continued

Site	<i>x</i>	<i>y</i>	<i>z</i>	$U_{11}$	$U_{22}$	$U_{33}$	$U_{23}$	$U_{13}$	$U_{12}$	$U_{eq}$	
					<b>P6</b>						
Cs1	0	0	0.08169(2)	0.0242(2)	0.0242(2)	0.0188(3)	0	0	0.01212(11)	0.02242(18)	
Cs2	0	0	¼	0.0378(3)	0.0378(3)	0.0219(4)	0	0	0.01891(17)	0.0325(3)	
Na1	0	0	0	0.002(4)							
Na2	0	0	0.1621(10)	0.027(12)	0.027(12)	0.032(17)	0	0	0.013(6)	0.028(10)	
Li	0.5038(5)	0	¼	0.013(1)							
Be	0.3278(2)	0.1621(3)	0.24917(11)	0.0073(6)							
Si1	0.04378(5)	0.21938(5)	−0.00114(3)	0.0039(3)	0.0044(3)	0.0047(3)	0.0007(3)	0.0003(3)	0.0020(2)	0.00441(18)	
Si2	0.44652(5)	0.16355(5)	−0.00022(3)	0.0048(3)	0.0041(3)	0.0049(3)	−0.0008(3)	0.0000(3)	0.0025(3)	0.00446(18)	
Si3	0.61581(5)	0.11345(5)	−0.00179(3)	0.0033(3)	0.0047(3)	0.0036(3)	0.0002(3)	−0.0004(3)	0.0018(2)	0.00398(18)	
Al1	0.33274(6)	0	¼	0.0048(5)	0.0048(6)	0.0044(6)	0.0002(3)	0.00012(17)	0.0023(3)	0.0046(3)	
Al2	0.67378(8)	0	¼	0.0039(4)	0.0039(6)	0.0059(6)	−0.0003(3)	−0.00016(17)	0.0019(3)	0.0045(3)	
O1	0.48301(14)	0.27760(13)	0.99221(7)	0.0098(9)	0.0043(8)	0.0099(10)	−0.0002(7)	0.0005(7)	0.0041(7)	0.0077(4)	
O2	0.54698(13)	0.16120(13)	0.99918(8)	0.0075(8)	0.0099(8)	0.0110(8)	−0.0010(8)	−0.0008(8)	0.0068(7)	0.0084(4)	
O3	0.11922(14)	0.17886(14)	0.00613(8)	0.0074(8)	0.0099(8)	0.0101(10)	0.0001(7)	−0.0015(7)	0.0069(7)	0.0080(4)	
O4	0.39123(14)	0.26943(14)	0.11763(7)	0.0088(9)	0.0047(8)	0.0038(8)	−0.0016(6)	−0.0028(6)	0.0044(8)	0.0053(4)	
O5	0.27330(15)	0.37599(15)	0.04300(7)	0.0085(9)	0.0066(9)	0.0093(9)	0.0028(7)	−0.0007(7)	0.0047(8)	0.0077(4)	
O6	0.28085(14)	0.20995(13)	0.05137(7)	0.0074(9)	0.0053(9)	0.0036(8)	−0.0002(6)	−0.0042(6)	0.0048(8)	0.0047(4)	
O7	0.04285(15)	0.45265(14)	0.04719(7)	0.0086(9)	0.0061(9)	0.0073(9)	0.0004(7)	0.0004(7)	0.0039(8)	0.0072(4)	
O8	0.04847(15)	0.28184(14)	0.04385(7)	0.0054(9)	0.0082(9)	0.0070(8)	−0.0012(7)	−0.0004(7)	0.0031(7)	0.0070(4)	
O9	0.39639(14)	0.13190(15)	0.05158(7)	0.0052(9)	0.0052(9)	0.0073(8)	0.0016(7)	0.0009(7)	0.0018(7)	0.0062(4)	

**Table 9.** continued

Site	x	y	z	$U_{11}$	$U_{22}$	$U_{33}$	$U_{23}$	$U_{13}$	$U_{12}$	$U_{eq}$	
					<b>P7</b>						
Cs1	0	0	0.08184(2)	0.0254(2)	0.0254(2)	0.0203(3)	0	0	0.01272(10)	0.02373(18)	
Cs2	0	0	¼	0.0369(3)	0.0369(3)	0.0226(3)	0	0	0.01847(14)	0.0322(2)	
Na1	0	0	0	0.002(3)							
Na2	0	0	0.1633(7)	0.005(7)	0.005(7)	0.038(14)	0	0	0.003(3)	0.016(7)	
Li	0.5033(3)	0	¼	0.0127(9)							
Be	0.32815(17)	0.1622(2)	0.24918(8)	0.0080(5)							
Si1	0.04439(4)	0.21941(4)	-0.00112(2)	0.0055(3)	0.0053(3)	0.0055(3)	0.00022(18)	0.00063(19)	0.00257(19)	0.00547(16)	
Si2	0.44657(4)	0.16354(4)	-0.00027(2)	0.0055(3)	0.0050(3)	0.0055(3)	-0.00004(19)	0.00027(18)	0.00288(19)	0.00523(16)	
Si3	0.61589(4)	0.11348(4)	-0.00155(2)	0.0043(2)	0.0051(3)	0.0052(3)	-0.00006(18)	0.00004(19)	0.00219(18)	0.00494(16)	
Al1	0.33277(40)	0	¼	0.0049(3)	0.0049(4)	0.0054(5)	0.0002(2)	0.00011(12)	0.00244(19)	0.0050(2)	
Al2	0.67315(6)	0	¼	0.0056(3)	0.0050(4)	0.0062(5)	-0.0003(2)	-0.00014(12)	0.00248(19)	0.0057(2)	
O1	0.48342(11)	0.27765(10)	0.99283(6)	0.0121(6)	0.0049(8)	0.0151(8)	0.0006(5)	0.0025(5)	0.0053(5)	0.0102(3)	
O2	0.54653(10)	0.16048(11)	0.99916(6)	0.0079(6)	0.0117(6)	0.0130(7)	-0.0004(6)	-0.0012(5)	0.0076(5)	0.0097(3)	
O3	0.11956(10)	0.17879(11)	0.00570(6)	0.0079(6)	0.0111(6)	0.0133(7)	0.0004(5)	-0.0021(5)	0.0068(5)	0.0099(3)	
O4	0.39084(11)	0.26936(10)	0.11785(6)	0.0099(7)	0.0062(6)	0.0067(6)	-0.0011(5)	-0.0030(5)	0.0045(5)	0.0074(3)	
O5	0.27324(11)	0.37668(11)	0.04316(6)	0.0105(7)	0.0092(7)	0.0113(7)	0.0040(5)	-0.0016(5)	0.0047(5)	0.0104(3)	
O6	0.28082(10)	0.21029(10)	0.05108(6)	0.0083(6)	0.0073(6)	0.0078(7)	-0.0017(5)	-0.0037(5)	0.0049(5)	0.0073(3)	
O7	0.04321(11)	0.45244(10)	0.04739(5)	0.0096(6)	0.0081(6)	0.0074(6)	0.0011(5)	0.0024(5)	0.0045(5)	0.0084(3)	
O8	0.04982(13)	0.28229(11)	0.04421(6)	0.0127(7)	0.0102(7)	0.0096(7)	-0.0021(5)	0.0022(5)	0.0054(6)	0.0110(3)	
O9	0.39524(11)	0.13075(12)	0.05145(5)	0.0095(6)	0.0093(7)	0.0076(7)	0.0024(5)	0.0030(5)	0.0054(5)	0.0085(3)	

**Table 9.** continued

Site	x	y	z	$U_{11}$	$U_{22}$	$U_{33}$	$U_{23}$	$U_{13}$	$U_{12}$	$U_{eq}$	
					<b>P12</b>						
Cs1	0	0	0.08291(3)	0.0284(3)	0.0284(3)	0.0204(4)	0	0	0.01422(16)	0.0258(3)	
Cs2	0	0	¼	0.0377(6)	0.0377(6)	0.0273(7)	0	0	0.0188(3)	0.0342(5)	
Na1	0	0	0	0.031(6)							
Na2	0	0	0.1668(6)	0.010(4)	0.010(4)	0.057(9)	0	0	0.0050(19)	0.026(4)	
Li	0.4983(8)	0	0	0.013(3)							
Be	0.3314(4)	0.1633(5)	0.24994(19)	0.0121(8)							
Si1	0.04712(8)	0.21961(7)	-0.00026(5)	0.0075(5)	0.0077(5)	0.0086(5)	0.0004(5)	-0.0011(5)	0.0033(4)	0.0082(3)	
Si2	0.44676(7)	0.16253(7)	0.00013(4)	0.0067(5)	0.0054(5)	0.0073(4)	-0.0021(5)	0.0007(5)	0.0021(4)	0.0069(2)	
Si3	0.61719(7)	0.11344(7)	-0.00076(5)	0.0052(5)	0.0068(5)	0.0090(5)	-0.0004(5)	-0.0010(4)	0.0020(4)	0.0075(2)	
Al1	0.33326(11)	0	¼	0.0091(7)	0.0102(9)	0.0067(7)	0.0024(6)	0.0012(3)	0.0051(5)	0.0086(4)	
Al2	0.66907(12)	0	¼	0.0081(7)	0.0034(8)	0.0071(7)	-0.0016(6)	-0.0008(3)	0.0016(4)	0.0067(4)	
O1	0.4873(2)	0.2779(2)	0.99825(17)	0.0186(15)	0.0042(12)	0.0378(19)	0.0019(16)	0.0071(17)	0.0069(12)	0.0197(7)	
O2	0.5447(2)	0.1566(2)	0.99913(15)	0.0136(14)	0.0145(14)	0.0290(17)	-0.0013(16)	-0.0006(17)	0.0089(12)	0.0182(6)	
O3	0.1215(2)	0.1788(2)	0.00242(16)	0.0110(14)	0.0162(15)	0.0343(19)	0.0044(16)	0.0019(17)	0.0089(12)	0.0196(7)	
O4	0.3861(2)	0.2682(3)	0.11840(12)	0.016(2)	0.0185(19)	0.0108(14)	0.0038(13)	-0.0088(12)	0.0018(15)	0.0181(9)	
O5	0.2701(3)	0.3816(3)	0.04663(13)	0.029(2)	0.0115(19)	0.0190(17)	0.0119(13)	-0.0139(15)	0.0016(15)	0.0236(9)	
O6	0.2821(2)	0.2153(3)	0.04906(12)	0.0128(19)	0.031(2)	0.0154(15)	-0.0174(14)	-0.0094(12)	0.012(2)	0.0189(9)	
O7	0.0500(3)	0.4526(3)	0.04769(13)	0.024(2)	0.019(2)	0.0179(16)	0.0053(13)	0.0042(14)	0.012(2)	0.0195(9)	
O8	0.0615(3)	0.2810(3)	0.04673(14)	0.026(2)	0.016(2)	0.0228(18)	-0.0044(14)	0.0118(16)	0.0011(16)	0.0255(10)	
O9	0.3893(3)	0.1229(3)	0.04895(13)	0.022(2)	0.023(2)	0.0194(16)	0.0124(14)	0.0091(14)	0.016(2)	0.0197(9)	



**Table 10.** Selected interatomic distances (Å) for crystals of the beryl-pezzottaite series with space-group symmetry  $R\bar{3}c$ .

<b>P1</b>					
<i>Si1</i> –O3	1.636(2)	<i>Al1</i> –O4g x2	1.926(2)	<i>Cs1</i> –O1j x3	3.381(2)
<i>Si1</i> –O3a	1.632(2)	<i>Al1</i> –O5g x2	1.825(2)	<i>Cs1</i> –O2j x3	3.386(2)
<i>Si1</i> –O6a	1.632(2)	<i>Al1</i> –O6g x2	1.926(2)	<i>Cs1</i> –O3 x3	3.291(2)
<i>Si1</i> –O8	1.585(2)	< <i>Al1</i> –O>	1.892	<i>Cs1</i> –O3k x3	3.503(2)
< <i>Si1</i> –O>	1.621			< <i>Cs1</i> –O>	3.391
		<i>Al2</i> –O7g x2	1.936(2)		
<i>Si2</i> –O1b	1.621(2)	<i>Al2</i> –O8g x2	1.845(2)	<i>Cs2</i> –O1j x6	3.619(2)
<i>Si2</i> –O2b	1.619(2)	<i>Al2</i> –O9h x2	1.937(2)	<i>Cs2</i> –O2j x6	3.393(2)
<i>Si2</i> –O5c	1.592(2)	< <i>Al2</i> –O>	1.906	< <i>Cs2</i> –O>	3.506
<i>Si2</i> –O9	1.609(2)				
< <i>Si2</i> –O>	1.610	<i>Be</i> –O4g	1.645(4)	<i>Na1</i> –O3 x6	2.522(2)
		<i>Be</i> –O6g	1.629(4)		
<i>Si3</i> –O1d	1.605(2)	<i>Be</i> –O7i	1.643(4)	<i>Na2</i> –O1j x3	2.601(2)
<i>Si3</i> –O2b	1.618(2)	<i>Be</i> –O9g	1.627(4)	<i>Na2</i> –O2j x3	2.454(2)
<i>Si3</i> –O4e	1.623(2)	< <i>Be</i> –O>	1.637	< <i>Na2</i> –O>	2.528
<i>Si3</i> –O7f	1.607(2)				
< <i>Si3</i> –O>	1.613	<i>Li</i> –O5g x2	1.887(6)		
		<i>Li</i> –O8g x2	1.915(6)		
		< <i>Li</i> –O>	1.901		
<b>P2</b>					
<i>Si1</i> –O3	1.631(2)	<i>Al1</i> –O4g x2	1.925(2)	<i>Cs1</i> –O1j x3	3.387(2)
<i>Si1</i> –O3a	1.628(2)	<i>Al1</i> –O5g x2	1.834(2)	<i>Cs1</i> –O2j x3	3.400(2)
<i>Si1</i> –O6a	1.633(2)	<i>Al1</i> –O6g x2	1.926(2)	<i>Cs1</i> –O3 x3	3.308(2)
<i>Si1</i> –O8	1.584(2)	< <i>Al1</i> –O>	1.895	<i>Cs1</i> –O3k x3	3.488(2)
< <i>Si1</i> –O>	1.619			< <i>Cs1</i> –O>	3.396
		<i>Al2</i> –O7g x2	1.934(2)		
<i>Si2</i> –O1b	1.620(2)	<i>Al2</i> –O8g x2	1.853(2)	<i>Cs2</i> –O1j x6	3.593(2)
<i>Si2</i> –O2b	1.616(2)	<i>Al2</i> –O9h x2	1.935(2)	<i>Cs2</i> –O2j x6	3.395(2)
<i>Si2</i> –O5c	1.596(2)	< <i>Al2</i> –O>	1.907	< <i>Cs2</i> –O>	3.494
<i>Si2</i> –O9	1.605(2)				
< <i>Si2</i> –O>	1.610	<i>Be</i> –O4g	1.646(4)	<i>Na1</i> –O3 x6	2.521(2)
		<i>Be</i> –O6g	1.632(3)		
<i>Si3</i> –O1d	1.604(2)	<i>Be</i> –O7i	1.644(3)	<i>Na2</i> –O1j x3	2.591(2)
<i>Si3</i> –O2b	1.616(2)	<i>Be</i> –O9g	1.631(3)	<i>Na2</i> –O2j x3	2.467(2)
<i>Si3</i> –O4e	1.624(2)	< <i>Be</i> –O>	1.638	< <i>Na2</i> –O>	2.529
<i>Si3</i> –O7f	1.607(2)				
< <i>Si3</i> –O>	1.613	<i>Li</i> –O5g x2	1.859(5)		
		<i>Li</i> –O8g x2	1.884(5)		
		< <i>Li</i> –O>	1.872		

Table 10. continued

P4					
<i>Si</i> 1–O3	1.623(3)	<i>Al</i> 1–O4g x2	1.908(4)	<i>Cs</i> 1–O1j x3	3.415(4)
<i>Si</i> 1–O3a	1.617(3)	<i>Al</i> 1–O5g x2	1.848(4)	<i>Cs</i> 1–O2j x3	3.413(3)
<i>Si</i> 1–O6a	1.637(3)	<i>Al</i> 1–O6g x2	1.900(3)	<i>Cs</i> 1–O3 x3	3.359(4)
<i>Si</i> 1–O8	1.581(4)	< <i>Al</i> 1–O>	1.885	<i>Cs</i> 1–O3k x3	3.471(4)
< <i>Si</i> 1–O>	1.614			< <i>Cs</i> 1–O>	3.415
		<i>Al</i> 2–O7g x2	1.930(3)		
<i>Si</i> 2–O1b	1.612(3)	<i>Al</i> 2–O8g x2	1.893(4)	<i>Cs</i> 2–O1j x6	3.515(4)
<i>Si</i> 2–O2b	1.612(3)	<i>Al</i> 2–O9h x2	1.930(4)	<i>Cs</i> 2–O2j x6	3.417(4)
<i>Si</i> 2–O5c	1.613(4)	< <i>Al</i> 2–O>	1.918	< <i>Cs</i> 2–O>	3.466
<i>Si</i> 2–O9	1.589(3)				
< <i>Si</i> 2–O>	1.607	<i>Be</i> –O4g	1.664(8)	<i>Na</i> 1–O3 x6	2.530(3)
		<i>Be</i> –O6g	1.654(8)		
<i>Si</i> 3–O1d	1.607(3)	<i>Be</i> –O7i	1.677(7)	<i>Na</i> 2–O1j x3	2.565(3)
<i>Si</i> 3–O2b	1.616(3)	<i>Be</i> –O9g	1.667(7)	<i>Na</i> 2–O2j x3	2.497(3)
<i>Si</i> 3–O4e	1.629(3)	< <i>Be</i> –O>	1.665	< <i>Na</i> 2–O>	2.531
<i>Si</i> 3–O7f	1.589(3)				
< <i>Si</i> 3–O>	1.610	<i>Li</i> –O5g x2	1.770(9)		
		<i>Li</i> –O8g x2	1.800(9)		
		< <i>Li</i> –O>	1.785		
P5					
<i>Si</i> 1–O3	1.634(2)	<i>Al</i> 1–O4g x2	1.923(2)	<i>Cs</i> 1–O1j x3	3.382(2)
<i>Si</i> 1–O3a	1.628(2)	<i>Al</i> 1–O5g x2	1.825(2)	<i>Cs</i> 1–O2j x3	3.393(2)
<i>Si</i> 1–O6a	1.639(2)	<i>Al</i> 1–O6g x2	1.923(2)	<i>Cs</i> 1–O3 x3	3.299(2)
<i>Si</i> 1–O8	1.580(2)	< <i>Al</i> 1–O>	1.890	<i>Cs</i> 1–O3k x3	3.499(2)
< <i>Si</i> 1–O>	1.620			< <i>Cs</i> 1–O>	3.393
		<i>Al</i> 2–O7g x2	1.936(2)		
<i>Si</i> 2–O1b	1.620(2)	<i>Al</i> 2–O8g x2	1.846(2)	<i>Cs</i> 2–O1j x6	3.609(2)
<i>Si</i> 2–O2b	1.619(2)	<i>Al</i> 2–O9h x2	1.940(2)	<i>Cs</i> 2–O2j x6	3.389(2)
<i>Si</i> 2–O5c	1.597(2)	< <i>Al</i> 2–O>	1.908	< <i>Cs</i> 2–O>	3.499
<i>Si</i> 2–O9	1.601(2)				
< <i>Si</i> 2–O>	1.609	<i>Be</i> –O4g	1.647(4)	<i>Na</i> 1–O3 x6	2.525(2)
		<i>Be</i> –O6g	1.632(4)		
<i>Si</i> 3–O1d	1.607(2)	<i>Be</i> –O7i	1.645(4)	<i>Na</i> 2–O1j x3	2.596(2)
<i>Si</i> 3–O2b	1.619(2)	<i>Be</i> –O9g	1.629(4)	<i>Na</i> 2–O2j x3	2.456(2)
<i>Si</i> 3–O4e	1.629(2)	< <i>Be</i> –O>	1.638	< <i>Na</i> 2–O>	2.527
<i>Si</i> 3–O7f	1.603(2)				
< <i>Si</i> 3–O>	1.615	<i>Li</i> –O5g x2	1.905(6)		
		<i>Li</i> –O8g x2	1.880(6)		
		< <i>Li</i> –O>	1.893		

Table 10. continued

P6					
<i>Si</i> 1–O3	1.640(2)	<i>Al</i> 1–O4g x2	1.930(2)	<i>Cs</i> 1–O1j x3	3.377(2)
<i>Si</i> 1–O3a	1.632(2)	<i>Al</i> 1–O5g x2	1.823(2)	<i>Cs</i> 1–O2j x3	3.383(2)
<i>Si</i> 1–O6a	1.638(2)	<i>Al</i> 1–O6g x2	1.929(2)	<i>Cs</i> 1–O3 x3	3.282(2)
<i>Si</i> 1–O8	1.580(2)	< <i>Al</i> 1–O>	1.894	<i>Cs</i> 1–O3k x3	3.511(2)
< <i>Si</i> 1–O>	1.623			< <i>Cs</i> 1–O>	3.388
		<i>Al</i> 2–O7g x2	1.939(2)		
<i>Si</i> 2–O1b	1.624(2)	<i>Al</i> 2–O8g x2	1.845(2)	<i>Cs</i> 2–O1j x6	3.636(2)
<i>Si</i> 2–O2b	1.623(2)	<i>Al</i> 2–O9h x2	1.942(2)	<i>Cs</i> 2–O2j x6	3.383(2)
<i>Si</i> 2–O5c	1.593(2)	< <i>Al</i> 2–O>	1.909	< <i>Cs</i> 2–O>	3.510
<i>Si</i> 2–O9	1.604(2)				
< <i>Si</i> 2–O>	1.611	<i>Be</i> –O4g	1.648(4)	<i>Na</i> 1–O3 x6	2.524(2)
		<i>Be</i> –O6g	1.627(4)		
<i>Si</i> 3–O1d	1.607(2)	<i>Be</i> –O7i	1.638(4)	<i>Na</i> 2–O1j x3	2.605(2)
<i>Si</i> 3–O2b	1.621(2)	<i>Be</i> –O9g	1.624(4)	<i>Na</i> 2–O2j x3	2.442(2)
<i>Si</i> 3–O4e	1.627(2)	< <i>Be</i> –O>	1.634	< <i>Na</i> 2–O>	2.524
<i>Si</i> 3–O7f	1.605(2)				
< <i>Si</i> 3–O>	1.615	<i>Li</i> –O5g x2	1.906(6)		
		<i>Li</i> –O8g x2	1.929(6)		
		< <i>Li</i> –O>	1.918		
P7					
<i>Si</i> 1–O3	1.635(2)	<i>Al</i> 1–O4g x2	1.929(2)	<i>Cs</i> 1–O1j x3	3.380(2)
<i>Si</i> 1–O3a	1.630(2)	<i>Al</i> 1–O5g x2	1.827(2)	<i>Cs</i> 1–O2j x3	3.386(2)
<i>Si</i> 1–O6a	1.631(2)	<i>Al</i> 1–O6g x2	1.928(1)	<i>Cs</i> 1–O3 x3	3.292(2)
<i>Si</i> 1–O8	1.588(2)	< <i>Al</i> 1–O>	1.895	<i>Cs</i> 1–O3k x3	3.505(2)
< <i>Si</i> 1–O>	1.621			< <i>Cs</i> 1–O>	3.391
		<i>Al</i> 2–O7g x2	1.933(1)		
<i>Si</i> 2–O1b	1.622(2)	<i>Al</i> 2–O8g x2	1.841(2)	<i>Cs</i> 2–O1j x6	3.600(2)
<i>Si</i> 2–O2b	1.621(2)	<i>Al</i> 2–O9h x2	1.937(2)	<i>Cs</i> 2–O2j x6	3.390(2)
<i>Si</i> 2–O5c	1.588(2)	< <i>Al</i> 2–O>	1.904	< <i>Cs</i> 2–O>	3.495
<i>Si</i> 2–O9	1.610(2)				
< <i>Si</i> 2–O>	1.610	<i>Be</i> –O4g	1.651(3)	<i>Na</i> 1–O3 x6	2.523(2)
		<i>Be</i> –O6g	1.632(3)		
<i>Si</i> 3–O1d	1.606(2)	<i>Be</i> –O7i	1.640(3)	<i>Na</i> 2–O1j x3	2.599(2)
<i>Si</i> 3–O2b	1.619(1)	<i>Be</i> –O9g	1.628(3)	<i>Na</i> 2–O2j x3	2.450(2)
<i>Si</i> 3–O4e	1.619(2)	< <i>Be</i> –O>	1.638	< <i>Na</i> 2–O>	2.525
<i>Si</i> 3–O7f	1.612(2)				
< <i>Si</i> 3–O>	1.614	<i>Li</i> –O5g x2	1.895(4)		
		<i>Li</i> –O8g x2	1.913(5)		
		< <i>Li</i> –O>	1.904		

Table 10. continued

P12					
<i>Si</i> 1–O3	1.620(3)	<i>Al</i> 1–O4g x2	1.903(4)	<i>Cs</i> 1–O1j x3	3.416(4)
<i>Si</i> 1–O3a	1.617(3)	<i>Al</i> 1–O5g x2	1.854(4)	<i>Cs</i> 1–O2j x3	3.405(4)
<i>Si</i> 1–O6a	1.622(3)	<i>Al</i> 1–O6g x2	1.896(3)	<i>Cs</i> 1–O3 x3	3.377(4)
<i>Si</i> 1–O8	1.582(4)	< <i>Al</i> 1–O>	1.884	<i>Cs</i> 1–O3k x3	3.468(4)
< <i>Si</i> 1–O>	1.610			< <i>Cs</i> 1–O>	3.417
		<i>Al</i> 2–O7g x2	1.928(3)		
<i>Si</i> 2–O1b	1.619(3)	<i>Al</i> 2–O8g x2	1.905(4)	<i>Cs</i> 2–O1j x6	3.474(4)
<i>Si</i> 2–O2b	1.613(3)	<i>Al</i> 2–O9h x2	1.925(4)	<i>Cs</i> 2–O2j x6	3.430(4)
<i>Si</i> 2–O5c	1.612(3)	< <i>Al</i> 2–O>	1.920	< <i>Cs</i> 2–O>	3.452
<i>Si</i> 2–O9	1.585(4)				
< <i>Si</i> 2–O>	1.608	<i>Be</i> –O4g	1.672(7)	<i>Na</i> 1–O3 x6	2.526(3)
		<i>Be</i> –O6g	1.665(4)		
<i>Si</i> 3–O1d	1.609(3)	<i>Be</i> –O7i	1.710(7)	<i>Na</i> 2–O1j x3	2.502(3)
<i>Si</i> 3–O2b	1.617(3)	<i>Be</i> –O9g	1.696(7)	<i>Na</i> 2–O2j x3	2.540(1)
<i>Si</i> 3–O4e	1.620(3)	< <i>Be</i> –O>	1.686	< <i>Na</i> 2–O>	2.865
<i>Si</i> 3–O7f	1.586(4)				
< <i>Si</i> 3–O>	1.607	<i>Li</i> –O5g x2	1.740(10)		
		<i>Li</i> –O8g x2	1.796(10)		
		< <i>Li</i> –O>	1.768		

Equivalent positions: a:  $x-y, x, -z$ ; b:  $x, y, z-1$ ; c:  $y, -x+y, -z$ ; d:  $-y+1, x-y, z-1$ ; e:  $y+\frac{1}{3}, x-\frac{1}{3}, -z+\frac{1}{6}$ ; f:  $x-y+1, x, -z$ ; g:  $-x+\frac{2}{3}, -y+\frac{1}{3}, -z+\frac{1}{3}$ ; h:  $y+\frac{2}{3}, -x+y+\frac{1}{3}, -z+\frac{1}{3}$ ; i:  $x+\frac{1}{3}, x-y+\frac{2}{3}, z+\frac{1}{6}$ ; j:  $-y+\frac{1}{3}, -x+\frac{2}{3}, z-\frac{5}{6}$ ; k:  $-x, -y, -z$ .

**Table 11.** Refined site-populations (apfu) for pezzottaite structures.

Site	Wyk.	P1	P2	P4	P5	P6	P7	P12
Cs1	12c	0.405(1)	0.330(1)	0.385(2)	0.439(2)	0.512(1)	0.465(1)	0.424(2)
Cs2	6a	0.231(1)	0.200(1)	0.205(1)	0.246(1)	0.275(1)	0.258(1)	0.218(1)
Na1	6b	0.134(4)	0.156(4)	0.062(6)	0.079(7)	0.062(4)	0.071(4)	0.088(7)
Na2	12c	0.110(7)	0.138(7)	0.116(10)	0.074(7)	0.057(8)	0.056(7)	0.167(9)

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**Table 12.** Bond-valence\* table for pezzottaite P6.

	Cs1	Cs2	Na1	Na2	Li	Be	Al1	Al2	Si1	Si2	Si3	Σ
O1	0.055 <sup>x3↓</sup>	0.031 <sup>x6↓</sup>		0.010 <sup>x3↓</sup>						1.000	1.045	2.141
O2	0.055 <sup>x3↓</sup>	0.059 <sup>x6↓</sup>		0.015 <sup>x3↓</sup>						1.003	1.005	2.137
O3	0.070 <sup>x3↓</sup> 0.040 <sup>x3↓</sup>		0.026 <sup>x6↓</sup>						0.960 0.980			2.076
O4						0.478	0.468 <sup>x2↓</sup>				0.992	1.938
O5					0.269 <sup>x2↓</sup>		0.616 <sup>x2↓</sup>			1.083		1.968
O6						0.513	0.469 <sup>x2↓</sup>		0.965			1.947
O7						0.495		0.457 <sup>x2↓</sup>			1.050	2.002
O8					0.259 <sup>x2↓</sup>			0.582 <sup>x2↓</sup>	1.120			1.961
O9						0.519		0.454 <sup>x2↓</sup>		1.053		2.026
Σ	0.660	0.540	0.156	0.075	1.056	2.005	3.106	2.986	4.025	4.139	4.092	

\*Bond-valence parameters from Gagné and Hawthorne (2015).

**Table 13.** Chemical composition (wt%) and unit formulae (apfu) of beryl-pezzottaite crystals.

	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10	P11	P12	P13	P14
SiO <sub>2</sub>	56.57	58.12	62.20	57.45	56.56	55.07	55.91	61.27	58.08	58.45	58.07	57.39	58.30	61.12
Al <sub>2</sub> O <sub>3</sub>	16.04	16.49	17.13	16.22	16.08	15.64	15.89	17.39	16.50	16.59	16.51	16.31	16.58	17.52
Na <sub>2</sub> O	0.60	0.87	1.17	0.88	0.62	0.36	0.51	1.16	1.75	1.79	1.58	1.16	1.57	1.28
Cs <sub>2</sub> O	12.91	10.45	3.68	11.80	13.32	15.55	14.39	5.36	9.74	9.82	10.31	13.15	10.47	4.40
Rb <sub>2</sub> O	–	–	–	–	0.37	0.45	0.40	–	–	0.06	–	–	–	–
K <sub>2</sub> O	0.05	0.04	0.08	0.06	0.12	0.11	0.14	0.07	–	0.02	–	–	–	0.05
CaO	0.60	0.56	0.00	0.00	0.20	0.25	0.23	–	–	0.01	–	–	–	–
BeO*	8.44	9.03	11.54	9.12	8.58	8.02	8.30	10.83	8.96	8.95	8.99	8.68	9.02	10.91
Li <sub>2</sub> O*	1.99	1.84	0.84	1.69	1.91	2.06	2.00	1.15	1.88	1.93	1.86	1.95	1.87	1.10
Total	97.20	97.39	97.31**	97.22	97.76	97.51	97.77	97.23	96.91	97.62	97.32	98.64	97.81	96.38
Si	5.997	5.996	5.999	6.002	5.994	5.995	5.994	5.996	5.995	5.996	5.994	5.994	5.993	5.984
Al	0.003	0.004	0.001	–	0.006	0.005	0.006	0.004	0.005	0.004	0.006	0.006	0.007	0.016
ΣT(1)	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000
Al	2.001	2.001	2.000†	1.997	2.002	2.002	2.002	2.002	2.002	2.002	2.002	2.002	2.002	2.006
Na	0.123	0.174	0.219	0.178	0.127	0.076	0.106	0.220	0.350	0.356	0.316	0.235	0.313	0.243
Cs	0.584	0.460	0.151	0.526	0.602	0.722	0.658	0.224	0.429	0.430	0.454	0.586	0.459	0.184
Rb	–	–	–	–	0.025	0.031	0.028	–	–	0.004	–	–	–	–
K	0.007	0.005	0.010	0.008	0.016	0.015	0.019	0.009	–	0.003	–	–	–	0.006
Ca	0.068	0.062	0.000	0.000	0.023	0.029	0.026	–	–	0.001	–	–	–	–
Sum channel	0.782	0.701	0.380	0.712	0.793	0.873	0.837	0.453	0.779	0.795	0.770	0.821	0.772	0.433
Be	2.150	2.237	2.674	2.288	2.184	2.098	2.137	2.547	2.221	2.205	2.230	2.179	2.228	2.567
Li	0.850	0.763	0.326	0.712	0.816	0.902	0.863	0.453	0.779	0.795	0.770	0.821	0.772	0.433
ΣT(2)	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000

\*Calculated by stoichiometry; \*\* includes FeO 0.67 wt%; † includes FeO 0.054 apfu.

**Table 14.** Alkali-alkali distances in the channel of the pezzottaite structures.

	P1	P2	P4	P5	P6	P7	P12
Cs1–Na1	2.278(1)	2.281(1)	2.294(1)	2.278(1)	2.275(1)	2.279(1)	2.309(1)
Cs1–Na2	2.26(1)	2.271(9)	2.31(3)	2.27(2)	2.24(3)	2.27(2)	2.34(2)
Cs2–Na2 x2	2.42(1)	2.402(9)	2.35(3)	2.41(2)	2.45(3)	2.42(2)	2.32(2)
Na1–Cs1 x2	2.278(1)	2.281(1)	2.294(1)	2.278(1)	2.275(1)	2.279(1)	2.309(1)
Na2–Cs1	2.26(1)	2.278(9)	2.31(3)	2.27(2)	2.24(3)	2.27(2)	2.34(2)
Na2–Cs2	2.42(1)	2.402(9)	2.35(3)	2.41(2)	2.45(3)	2.42(2)	2.32(2)

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